

Part 1: Design, Models, Perception

Information Visualization Mini-Course
TECS Week 2008

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Information Visualization

- visual representation of abstract data
 - computer-generated, often interactive

Interactivity

- static images
 - 10,000 years
 - art, graphic design
- moving images
 - 100 years
 - cinematography
- interactive graphics
 - 20 years
 - computer graphics, human-computer interaction

Information Visualization

- visual representation of abstract data
 - computer-generated, often interactive
 - help human perform some task more effectively

Information Visualization

- visual representation of abstract data
 - computer-generated, can be interactive
 - help human perform some task more effectively
- bridging many fields
 - graphics: drawing in realtime
 - cognitive psych: finding appropriate representation
 - HCI: using task to guide design and evaluation
- external representation
 - reduces load on working memory
 - offload cognition
 - familiar example: multiplication/division

External Representation: multiplication

paper	mental buffer
57	
x 48	

External Representation: multiplication

paper	mental buffer
5	
57	
x 48	[7*8=56]

6	

External Representation: multiplication

paper	mental buffer
5	
57	
x 48	[5*8=40 + 5 = 45]

456	

External Representation: multiplication

paper	mental buffer
2	
57	
x 48	[7*4=28]

456	
8	

External Representation: multiplication

paper	mental buffer
2	
57	
x 48	[5*4=20+2=22]

456	
228	

External Representation: multiplication

paper	mental buffer
57	
x 48	

1	
456	
228	

36	[8 + 5 = 13]

External Representation: multiplication

paper	mental buffer
57	
x 48	

456	
228	

2736	

Information Visualization

- visual representation of abstract data
 - computer-generated, can be interactive
 - help human perform some task more effectively
- bridging many fields
 - graphics: drawing in realtime
 - cognitive psych: finding appropriate representation
 - HCI: using task to guide design and evaluation
- external representation
 - reduces load on working memory
 - offload cognition
 - familiar example: multiplication/division
 - infos example: topic graphs

External Representation: Topic Graphs

[Gödel, Escher, Bach, Hofstadter 1979]

Turing - Halting problem
Halting problem - Infinity
Paradoxes - Infinity
Infinity - Lewis Carroll
Infinity - Unpredictably long searches
Infinity - Recursion
Infinity - Zeno
Infinity - **Paradoxes**
Lewis Carroll - Zeno
Lewis Carroll - Wordplay

Halting problem - Decision procedures
BloP and FloP - AI
Halting problem - Unpredictably long searches
BloP and FloP - Unpredictably long searches
BloP and FloP - Recursion
Tarski - Truth vs. provability
Tarski - Epimenides
Tarski - Undecidability
Paradoxes - Self-ref

External Representation: Topic Graphs

- offload cognition to visual systems
- minimal attention to read answer



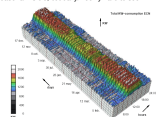
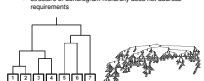
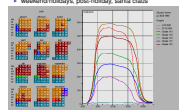
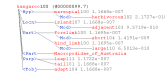

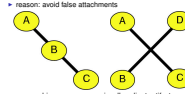

External Rep: Automatic Layout

manual: hours, days automatic: seconds



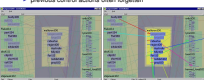
[Gödel, Escher, Bach, Hofstadter 70]

ed. (Gemaner et al 92)

<h3>Mini-Course Outline</h3> <ul style="list-style-type: none"> Part 1: Monday morning <ul style="list-style-type: none"> Intro Design Studies Models Perception Part 2: Monday afternoon <ul style="list-style-type: none"> Color Space, Layers, and Ordering Statistical Graphics Part 3: Thursday afternoon <ul style="list-style-type: none"> Multiples and Interaction Navigation and Zooming Focus-Context Part 4: Friday morning <ul style="list-style-type: none"> High Dimensional Data Graphs and Trees User Studies <p>[van Wijk and van Selow, Cluster and Calendar based Visualization of Time Series Data, InfoVis09, http://www.win.tue.nl/~vsew/ckc.pdf]</p>	<h3>Design Studies</h3> <ul style="list-style-type: none"> two concrete infovis examples <ul style="list-style-type: none"> before presenting theoretical models design study: infovis solution for specific application <ul style="list-style-type: none"> carry out task analysis in target domain derive design requirements justify choices of visual encoding and interaction build prototype (refine until satisfied) <p>[van Wijk and van Selow, Cluster and Calendar based Visualization of Time Series Data, InfoVis09, http://www.win.tue.nl/~vsew/ckc.pdf]</p>	<h3>Cluster-Calendar, van Wijk</h3> <p>van Wijk and van Selow, Cluster and Calendar based Visualization of Time Series Data, Proc. InfoVis 09, http://www.win.tue.nl/~vsew/ckc.pdf</p> <ul style="list-style-type: none"> data: N (value, time) pairs <ul style="list-style-type: none"> N large: 50K tasks <ul style="list-style-type: none"> find standard day patterns find how patterns distributed over year, week, season find outliers from standard daily patterns want overview first, then detail on demand possibilities <ul style="list-style-type: none"> predictive mathematical models <ul style="list-style-type: none"> details lost, multiscale not addressed scale-space approaches (wavelet, fourier, fractal) <ul style="list-style-type: none"> hard to interpret, known scales lost 3D extruded mountain: x hours, y value, z days <ul style="list-style-type: none"> 3D often pretty but not useful <p>[van Wijk and van Selow, Cluster and Calendar based Visualization of Time Series Data, InfoVis09, http://www.win.tue.nl/~vsew/ckc.pdf]</p>	<h3>3D Problems</h3> <ul style="list-style-type: none"> occlusion, perspective distortion seasonal visible, but daily/weekly hard to see  <p>[van Wijk and van Selow, Cluster and Calendar based Visualization of Time Series Data, InfoVis09, http://www.win.tue.nl/~vsew/ckc.pdf]</p>
<h3>Create Clusters</h3> <ul style="list-style-type: none"> create derived variable by transforming raw data use day as fundamental unit based on task analysis hierarchical clustering, merging most similar days but not interesting to show dendrogram directly <ul style="list-style-type: none"> structure of dendrogram hierarchy does not address requirements  <p>[van Wijk and van Selow, Cluster and Calendar based Visualization of Time Series Data, InfoVis09, http://www.win.tue.nl/~vsew/ckc.pdf]</p>	<h3>Link Curves and Calendar</h3> <ul style="list-style-type: none"> show clusters as linked curves-calendars in 2D site patterns <ul style="list-style-type: none"> office hours, fridays in/and summer, school break weekend/holidays, post-holiday, santa claus  <p>[van Wijk and van Selow, Cluster and Calendar based Visualization of Time Series Data, InfoVis09, http://www.win.tue.nl/~vsew/ckc.pdf]</p>	<h3>Lessons</h3> <ul style="list-style-type: none"> derived variable: clusters challenges of naive 3D usage linked displays traditional visual representation of time: calendar clear task analysis guided choices <ul style="list-style-type: none"> reject standard 3D extrusion reject standard dendrogram critique <ul style="list-style-type: none"> colors not maximally discriminable 	<h3>Linguistic Networks, Munzner</h3> <p>Munzner, Gumbeliere, and Robertson, Constellation: A Visualization Tool for Linguistic Queries from MindNet, Proc. InfoVis 09, http://graphics.stanford.edu/papers/infovis</p> <ul style="list-style-type: none"> data: MindNet query results definition graph from dictionary entry sentence <ul style="list-style-type: none"> nodes: word senses links: relation types 
<h3>Semantic Network</h3> <ul style="list-style-type: none"> definition graphs used as building blocks unify shared words large network <ul style="list-style-type: none"> millions of nodes grammar checking now, translation future global structure known: dense probes return local info 	<h3>Path Query</h3> <ul style="list-style-type: none"> best N paths between two words words on path itself <pre> topopen111--dawn--ofrcal10111--804--debrt111--204--debrt111--804--eal1110 </pre> <ul style="list-style-type: none"> definition graphs used in computation <pre> topopen1110111 (nodeid) topen1110 e sharp-tailed_groove111 point111 e pitta1110 partidge1110 lpsn1110 lo sharp-tailed_groove1110 newe1110 newe botall1110 botall1110 sbocae1110 botocae1110sbocae1110 </pre>	<h3>Task: Plausibility Checking</h3> <ul style="list-style-type: none"> paths ordered by computed plausibility researcher hand-checks results <ul style="list-style-type: none"> high-ranking paths believable? believable paths high-ranked? are stop words all filtered out? 	<h3>Window Flipping Problem</h3> 
<h3>Goal</h3> <ul style="list-style-type: none"> create a unified view of relationships between paths and definition graphs <ul style="list-style-type: none"> shared words are key thousands of words (pot millions) special purpose algorithm debugging tools <ul style="list-style-type: none"> not understand structure of English 	<h3>Constellation Video</h3>	<h3>Traditional Graph Layout</h3> <ul style="list-style-type: none"> avoid crossings using careful spatial positioning reason: avoid false attachments  <p>[Munzner, Interactive Visualization of Large Graphs and Networks (PhD thesis), Stanford University, 2006, http://graphics.stanford.edu/papers/munzner_thesis]</p>	<h3>Information Visualization Approach</h3> <ul style="list-style-type: none"> encode domain-specific attribute with spatial position <ul style="list-style-type: none"> why? spatial position is strongest perceptual cue plausibility gradient from left to right novel layout algorithm using curvilinear grid <ul style="list-style-type: none"> paths as backbone, attach definition graphs many crossings for long-distance prey links  <p>[http://graphics.stanford.edu/papers/munzner_thesis]</p>

Visual Layering

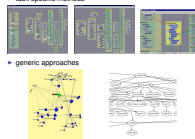
- avoid **perception** of attachments with visual layers
- interactively highlight sets of boxes and edges
 - perceptual channels: size, saturation, brightness
- avoid hidden state of visible/invisible toggle
 - implicit assumption: if not visible, doesn't exist
 - previous control actions often forgotten



[http://graphics.stanford.edu/papers/munzner_thesis]

Task-Oriented Design Success

- task-specific methods
 - Color
 - Space, Layers, and Ordering
 - Statistical Graphics
- generic approaches
 - Color
 - Space, Layers, and Ordering
 - Statistical Graphics



[http://graphics.stanford.edu/papers/munzner_thesis]

Lessons

- spatial position as strongest perceptual cue
- interactive visual layering, avoiding hidden state
- custom application vs. generic toolkits
 - critique
 - effort of custom application vs. generic toolkits

Design Studies: Reading

Cluster and Calendar based Visualization of Time Series Data.
 Jarke J. van Wijk and Edward R. van Selow
 Proc. InfoVis 99, pp 4-9
<http://www.win.tue.nl/~vanwijk/vjw.pdf>

Constellation: A Visualization Tool For Linguistic Queries from MindJet.
 Tamara Munzner, François Guimaraes, and George Robertson.
 Proc. InfoVis 99, p 132-135.
<http://graphics.stanford.edu/papers/const>

Constellation: Linguistic Semantic Networks
 Tamara Munzner
 Interactive Visualization of Large Graphs and Networks (PhD thesis) Chapter 5, Stanford University, 2000, pp 87-122
http://graphics.stanford.edu/papers/munzner_thesis

Design Studies: Further Reading

Process and Pitfalls in Writing Information Visualization Research Papers.
 Tamara Munzner, book chapter to appear.
<http://www.usc.edu/~imm/course/infvis/readings/pitfalls.pdf>

Exploratory visualization of array-based comparative genomic hybridization.
 Robert Kincaid, Amir Ben-Dor, and Zohar Yakhini
 Information Visualization 2(4):176-190, 2005. *Palgrave Macmillan*

Thematics in Search of Trends, Patterns, and Relationships.
 Susan Hare, Beth Heister, and Lucy Newell
 Proc. InfoVis 2000, pp 116-123


Vizster: Visualizing Online Social Networks.
 Jeffrey Heer and Deborah Buihler
 Proc. InfoVis 2005, pp 39-48
<http://peer.org/publications/2005-Vizster-InfoVis.pdf>

Visual Analysis of Historic Hanoi Violation Patterns.
 Chris Weaver, David Fyfe, Anthony Robinson, Derrick W. Hildebrandt, Donna J. Pruzgel and Alan M. MacIsaac
 Information Visualization 6(1):38-103, 2007.
http://www.gisworld.gov.au/publications/2006/Weaver_060103.pdf

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 - Focus+Context
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 - Graphs and Trees
 - User Studies

Visualization Big Picture



task

data

visual out

physical input (ctrl, mouse, etc)

domain

interaction

semantics

input/output

processing algorithms

range

visual out

visual out

mapping

visual encoding


visual metaphor

Mapping

- input
 - data semantics
 - use domain knowledge
- output
 - visual encoding
 - visual/graphical/perceptual/retinal channels/attributes/dimensions/variables
 - use human perception
- processing
 - algorithms
 - handle computational constraints

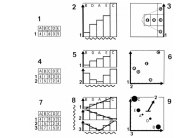
Bertin: Semiology of Graphics

- geometric primitives: marks
 - points, lines, areas, volumes
- attributes: visual/retinal variables
 - parameters control mark appearance
 - separable channels flowing from retina to brain
- X,Y
 - position
- Z
 - size
 - gray-scale
 - color
 - texture
 - orientation
 - shape



[Bertin, Semiology of Graphics, 1967 Gauthier-Villars, 1968 Elsevier]

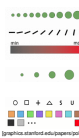
Design Space = Visual Metaphors



[Bertin, Semiology of Graphics, 1967 Gauthier-Villars, 1968 Elsevier]

Data Types

- continuous (quantitative)
 - 10 inches, 17 inches, 23 inches
- ordered (ordinal)
 - small, medium, large
 - days: Sun, Mon, Tue, ...
- categorical (nominal)
 - apples, oranges, bananas



[graphics.stanford.edu/papers/pitfalls]

Channel Ranking Varies by Data Type

- spatial position best for all types

Quantitative	Ordinal	Nominal
Position	Position	Position
Length	Density	Flow
Angle	Saturation	Texture
Slope	Flow	Connection
Area	Texture	Containment
Volume	Connection	Density
Density	Containment	Saturation
Saturation	Length	Angle
Texture	Slope	Slope
Connection	Area	Area
Containment	Volume	Volume
Shape	Shape	Area

[Marking: Automating the Design of Graphical Presentations of Relational Information. ACM TOG 5:2, 1986]

Mackinlay/Card Model

- data variables
 - 1D, 2D, 3D, 4D, 5D, etc
- data types
 - nominal, ordered, quantitative
- marks
 - point, line, area, surface, volume
 - geometric primitives
- retinal properties
 - size, brightness, color, texture, orientation, shape...
 - parameters that control the appearance of geometric primitives
 - separable channels of information flowing from retina to brain

[Card, Mackinlay, and Shneiderman, Chapter 1. Readings in Information Visualization: Using Vision to Think. Morgan Kaufmann 1998.]

Shneiderman's Data+Tasks Taxonomy

- data
 - 1D, 2D, 3D, temporal, nD, trees, networks
 - (flat and documents - Hanshan)
- tasks
 - overview, zoom, filter, details-on-demand,
 - relate, history, extract
 - data alone not enough
 - what do you need to do?
- mantra: overview first, zoom and filter, details on demand

[Shneiderman, The Eyes Have It: A Task by Data Type Taxonomy for Information Visualizations]

Amar/Eagan/Stasko Task Taxonomy

- low-level tasks
 - retrieve value, filter, compute derived value,
 - find extremum, sort, determine range,
 - characterize distribution, find anomalies,
 - cluster, correlate
- standardized set for better comparison between papers

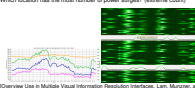
[Amar, Eagan, and Stasko, Low-Level Components of Analytic Activity in Information Visualization. Proc. InfoVis 05]

Control Room Example

Which location has the highest power surge for the given time period? (first extreme y-dimension)

A fault occurred at the beginning of this recording, and resulted in a temporary power surge. Which location is affected the earliest? (first extreme x-dimension)

Which location has the most number of power surges? (extreme count)



[Dierwies Use in Multiple Visual Information Presentation Interfaces. Lam, Munzner and Kincaid. Proc. InfoVis 2007]

Data Types and Conceptual Models

- from raw data model
 - 17, 25, 4, 28.6
 - (floats)
- to conceptual model of semantics
 - (temperature)
- consider task
 - making toast
 - classifying showers
 - finding anomalies in local weather patterns
- to determine data type
 - burned vs. not burned (N)
 - hot, warm, cold (C)
 - continuous to 4 sig figures (D)

[Rethinking Visualization: A High-Level Taxonomy, Melanie Tory and Torsten Moller, Proc. InfoVis 2004, pp. 151-158.]

Combinatorics of Encodings

- challenge
 - pick the best encoding from exponential number of possibilities ($n = 1$)ⁿ
 - if using n visual channels
- Principle of Consistency
 - properties of the image should match properties of data
- Principle of Importance Ordering
 - encode most important information in most effective way

Automatic Design

Mackinlay, Automating the Design of Graphical Presentations of Relational Information, ACM TOG 5:2, 1985

- APT system: pick encoding automatically given data
 - limited set of encodings: scatterplots, barline charts
- Expressiveness Criterion
 - Set of facts expressible in visual language if sentences (visualizations) in language express all facts in data, and only facts in data.
- Effectiveness
 - A visualization is more effective than another visualization if information conveyed by one visualization is more readily perceived than information in other.
- subject of the next section

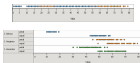
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- APT system: pick encoding automatically given data
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- Expressiveness Criterion
 - Set of facts expressible in visual language if sentences (visualizations) in language express all facts in data, and only facts in data.
- consider the failure cases...

Cannot Express the Facts

- A 1 → N relation cannot be expressed in a single horizontal dot plot because multiple tuples are mapped to the same position



[Hamanah, graphics.stanford.edu/courses/cs448b-04-winter/lectures/encoding]

Expresses Facts Not in the Data

- length interpreted as quantitative value
 - Thus length says something untrue about nominal data

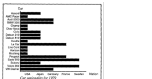


Fig. 1. A portion of a bar chart for the White House. The length of the bars suggests a difference in the number of people who visited the White House in 1994.

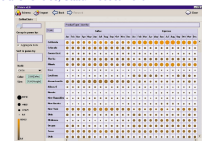
[Mackinlay, Automating the Design of Graphical Presentations of Relational Information, ACM TOG 5:2, 1985]

Polaris/Tableau

Polaris: A System for Query, Analysis and Visualization of Multi-dimensional Relational Databases, Chris Stone, Diane Tang and Pat Hanrahan, IEEE TVCG 8(1), Jan 2000

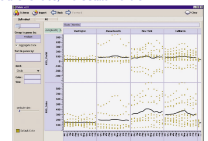
- table cell graphical elements, not just numbers
- user drag and drop exploration of marks/channels
 - instead of automatic selection
- table algebra ⇒ interactive interface ops
 - formal language
- commercialized via www.tableausoftware.com

Polaris: Circles, State/Product-Month



[Polaris: A System for Query, Analysis and Visualization of Multi-dimensional Relational Databases, Chris Stone, Diane Tang and Pat Hanrahan, IEEE TVCG 8(1), Jan 2000]

Polaris: Circles, Profit/State-Months



[Polaris: A System for Query, Analysis and Visualization of Multi-dimensional Relational Databases, Chris Stone, Diane Tang and Pat Hanrahan, IEEE TVCG 8(1), Jan 2000]

Models: Reading

Semiology of Graphics, Jacques Berth, Gauthier-Villars 1967, EHESS 1998

Automating the Design of Graphical Presentations of Relational Information, Jack Mackinlay, ACM Transaction on Graphics, vol. 5, no. 2, April 1986, pp. 110-141.

Chapter 1. Reading in Information Visualization: Using Vision to Think, Stuart Card, Jack Mackinlay, and Ben Shneiderman, Morgan Kaufmann 1989.

The Eyes Have It: A Task by Data Type Taxonomy for Information Visualizations Ben James Eagan, and John Stasko, Proc. InfoVis 01 [https://www.cs.gatech.edu/~john.stasko/papers/infovis01.pdf]

Low-Level Components of Analytic Activity in Information Visualization, Robert Aron, James Eagan, and John Stasko, Proc. InfoVis 01 [https://www.cs.gatech.edu/~john.stasko/papers/infovis01.pdf]

Rethinking Visualization: A High-Level Taxonomy, Melanie Tory and Torsten Moller, Proc. InfoVis 2004, pp. 151-158

[webhome.cs.uvic.ca/~tory/publications/infovis04.pdf]

Polaris: A System for Query, Analysis and Visualization of Multi-dimensional Relational Databases, Chris Stone, Diane Tang and Pat Hanrahan, IEEE TVCG 8(1), January 2000

[graphics.stanford.edu/courses/polaris/]

Models: Further Reading

The Grammar of Graphics, Leland Wilkinson, Springer-Verlag 1999

The Structure of the Information Visualization Design Space Stuart Card and Jack Mackinlay, Proc. InfoVis 97 [https://www.cs.gatech.edu/~stcard/papers/infovis97.pdf]

A Function-Based Data Model for Visualization, Lloyd Tienahm, Visualization 1999 Late Breaking Hot Topics

Multivariate Visualization Using Data Cubes, Chris Stone, Diane Tang and Pat Hanrahan, Proc. InfoVis 2002

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 - Graphics and Trees
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Human Perception

- sensors/transducers
 - psychophysics: determine characteristics
- relative judgements: strong
- absolute judgements: weak
- different optimizations than most machines
 - eyes are not cameras
 - perceptual dimensions not 1D array
 - brains are not hard disks

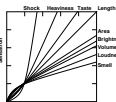
Psychophysical Measurement

- JND: just noticeable difference
- increment where human detects change
- average to create 'subjective' scale
- low level perception more uniform than high-level cognition across subjects

Nonlinear Perception of Magnitudes

sensory modalities **not** equally discriminable

Stevens' Power Law: $I = S^p$



[Stevens, On the Theory of Scales of Measurement, Science 122:2684, 1946]

Dimensional Dynamic Range

- linewidth: limited discriminability



[jocopa_murdi.net/maps/maps2/14/Geography.html]

Dimensional Ranking: Studies

- spatial position best for all types

Quantitative	Ordinal	Nominal
Position	Position	Position
Length	Density	Hue
Angle	Saturation	Texture
Shape	Hue	Connection
Area	Texture	Containment
Volume	Connection	Density
Density	Containment	Saturation
Saturation	Length	Shape
Hue	Angle	Length
Texture	Slope	Area
Connection	Area	Slope
Containment	Volume	Area
Shape	Shape	Volume

[Mackinlay, Advancing the Design of Graphical Presentations of Relational Information, ACM TDB 2.2, 1986]

Cleveland: Perceptual Studies

Cleveland and McGee, Graphical Perception: Theory, Experimentation and the Application to the Development of Graphical Models. J. Am. Stat. Assoc. 79:387, pp. 531-554, 1984.

Mackinlay	Cleveland (quant)
position	position along common scale
length	position along nonaligned scales
angle	length, direction, angle
slope	
area	area
volume	volume, curvature
density	shading, color saturation
saturation	
hue	
texture	
connection	
containment	
shape	

Weber's Law

- ratio of increment threshold to background intensity is constant
 - relative judgements within modality

$$\frac{\Delta I}{I} = K$$

- Cleveland example: frame increases accuracy

Graphical Perception: Theory, Experimentation and the Application to the Development of Graphical Models, William S. Cleveland, Robert McGill, J. Am. Stat. Assoc. 79:387, pp. 531-554, 1984.

Preattentive Visual Dimensions

- color (hue) alone: preattentive
 - attentional system not invoked
 - search speed independent of distractor count

- demo

[Chris Healey, Preattentive Processing, www.csc.ncsu.edu/faculty/healey/PP/PP.html]

Many Preattentive Visual Dimensions

hue
shape
texture
length
width
size
orientation
curvature
intersection
intensity
flicker
direction of motion
stereoscopic depth
light direction, ...

[www.csc.ncsu.edu/faculty/healey/PP/PP.html]

Not All Dimensions Preattentive

parallelism

[www.csc.ncsu.edu/faculty/healey/PP/PP.html]

Preattentive Visual Dimensions

- color alone: preattentive
- shape alone: preattentive

- combined hue and shape (demo)
 - requires attention
 - search speed linear with distractor count

[www.csc.ncsu.edu/faculty/healey/PP/PP.html]

Separable vs. Integral Dimensions

- only some dimensions separable

color location color motion color shape size orientation x-size y-size red-green yellow-blue

[Colin Ware, Information Visualization: Perception for Design, Morgan Kaufmann 1998.]

Perception: Readings

On the Theory of Scales of Measurement. S. S. Stevens. Science 103:2054, 1946

Graphical Perception: Theory, Experimentation and the Application to the Development of Graphical Models. William S. Cleveland, Robert McGill, J. Am. Stat. Assoc. 79:387, pp. 531-554, 1984.

Information Visualization: Perception for Design. Chapter 5: Visual Attention and Information That Pops Out. Colin Ware. Morgan Kaufmann, 2004 (2nd edition).

Perception in Visualization. Christopher G. Healey. <http://www.csc.ncsu.edu/faculty/healey/PP/>