



University of British Columbia
CPSC 414 Computer Graphics

Lighting

Week 5, Mon 29 Sep 2003

- recap: picking, light sources
- lighting

News

- continue signup for project 1 demo slots
- extra TA hours in labs
 - Monday 10-2, 4-5:30
 - Tuesday 11-1
 - Wednesday 10-1, 4-5:30
 - Thursday 11-1
- normal lab hours
 - Wed 1-3

Picking Select/Hit recap

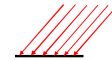
- assign (hierarchical) integer key/name(s)
- small region around cursor as new viewport



- redraw in selection mode
 - equivalent to casting pick “tube”
 - store keys, depth for drawn objects in hit list
- examine hit list
 - usually use frontmost, but up to application

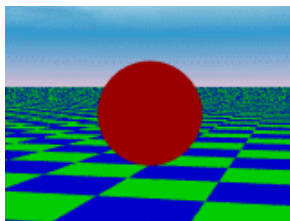
Light Sources recap

- directional/parallel lights
 - point at infinity: $(x,y,z,0)^T$
- point lights
 - finite position: $(x,y,z,1)^T$
- spotlights
 - position, direction, angle
- ambient lights



Ambient Light Sources

- scene lit only with an ambient light source



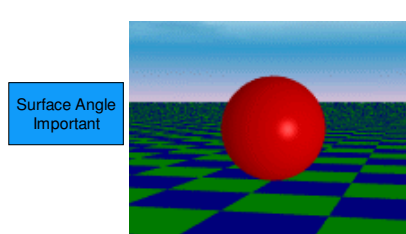
Light Position
Not Important

Viewer Position
Not Important

Surface Angle
Not Important

Directional Light Sources

- scene lit with directional and ambient light



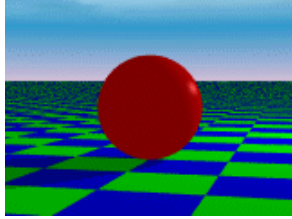
Light Position
Not Important

Viewer Position
Not Important

Point Light Sources

- scene lit with ambient and point light source

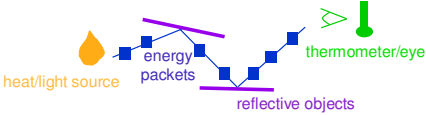
Light Position Important



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Illumination as Radiative Transfer

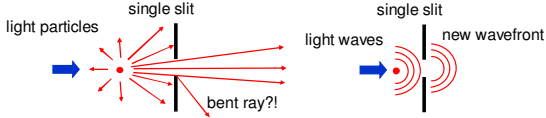
- radiative heat transfer approximation
 - substitute light for heat
 - light as packets of energy (photons)
 - particles not waves
 - model light transport as packet flow



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Light Transport Assumptions

- geometrical optics (light is photons not waves)
 - no diffraction



- no polarization (some sunglasses)
 - light of all orientations gets through
- no interference (packets don't interact)
 - interference demo: <http://www.falstad.com/ripple>
 - which visual effects does this preclude?

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Light Transport Assumptions II

- color approximated by discrete wavelengths
 - quantized approx of dispersion (rainbows)
 - quantized approx of fluorescence (cycling vests)
- no propagation media (surfaces in vacuum)
 - no atmospheric scattering (fog, clouds)
 - some tricks to simulate explicitly
 - no refraction (mirages)

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Light Transport Assumptions III

- light travels in straight line
 - no gravity lenses
- superposition (lights can be added)
 - no nonlinear reflection models
 - nonlinearity handled separately

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Illumination

- transport of energy from light sources to surfaces & points
 - includes *direct* and *indirect illumination*

Images by Henrik Wann Jensen

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Components of Illumination

- two components: light sources and surface properties
- light sources (or *emitters*)
 - spectrum of emittance (i.e., color of the light)
 - geometric attributes
 - position
 - direction
 - shape
 - directional attenuation
 - polarization

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Components of Illumination

- surface properties
 - reflectance spectrum (i.e., color of the surface)
 - subsurface reflectance
 - geometric attributes
 - position
 - orientation
 - micro-structure



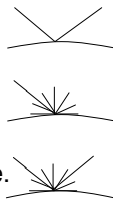
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Types of Reflection

- *specular* (a.k.a. *mirror* or *regular*) reflection causes light to propagate without scattering.
- *diffuse* reflection sends light in all directions with equal energy.
- *mixed* reflection is a weighted combination of specular and diffuse.



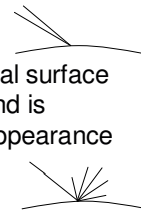
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Types of Reflection

- *retro-reflection* occurs when incident energy reflects in directions close to the incident direction, for a wide range of incident directions.
- *gloss* is the property of a material surface that involves mixed reflection and is responsible for the mirror like appearance of rough surfaces.



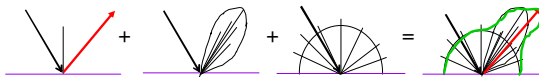
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Reflectance Distribution Model

- most surfaces exhibit complex reflectances
 - vary with incident and reflected directions.
 - model with combination



specular + glossy + diffuse =
reflectance distribution

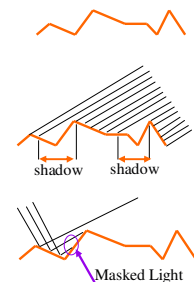
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Surface Roughness

- at a microscopic scale, all real surfaces are rough
- cast shadows on themselves
- “mask” reflected light:

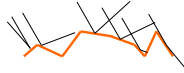


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Surface Roughness



- notice another effect of roughness:
 - each “microfacet” is treated as a perfect mirror.
 - incident light reflected in different directions by different facets.
 - end result is mixed reflectance.
 - smoother surfaces are more specular or glossy.
 - random distribution of facet normals results in diffuse reflectance.

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Physics of Reflection

- ideal diffuse reflection
 - very rough surface at the microscopic level
 - real-world example: chalk
 - microscopic variations mean incoming ray of light equally likely to be reflected in any direction over the hemisphere



– what does the reflected intensity depend on?

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Lambert's Cosine Law

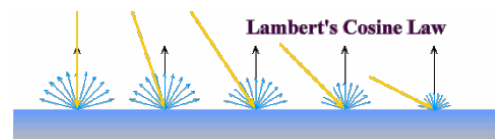
- ideal diffuse surface reflection
 - the energy reflected by a small portion of a surface from a light source in a given direction is proportional to the cosine of the angle between that direction and the surface normal
- reflected intensity
 - independent of viewing direction
 - depends on surface orientation wrt light
- often called *Lambertian surfaces*

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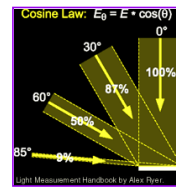
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Lambert's Law



intuitively: cross-sectional area of the “beam” intersecting an element of surface area is smaller for greater angles with the normal.



Light Measurement Handbook by Alex Rykiel

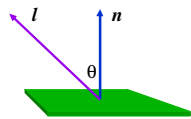
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Computing Diffuse Reflection

- angle between surface normal and incoming light is *angle of incidence*:
 - k_d : diffuse component
 - “surface color”



$$I_{\text{diffuse}} = k_d I_{\text{light}} \cos \theta$$

- in practice use vector arithmetic

$$I_{\text{diffuse}} = k_d I_{\text{light}} (\mathbf{n} \cdot \mathbf{l})$$

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Diffuse Lighting Examples

- Lambertian sphere from several lighting angles:



- need only consider angles from 0° to 90°
 - why?
 - demo: Brown exploratory on reflection


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Specular Reflection

- shiny surfaces exhibit *specular reflection*
 - polished metal
 - glossy car finish



diffuse



diffuse plus specular

- specular highlight*
 - bright spot from light shining on a specular surface
- view dependent
 - highlight position is function of the viewer's position

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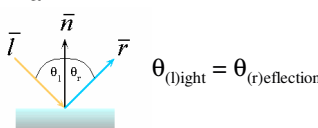
Physics of Reflection

- at the microscopic level a specular reflecting surface is very smooth
- thus rays of light are likely to bounce off the microgeometry in a mirror-like fashion
- the smoother the surface, the closer it becomes to a perfect mirror

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Optics of Reflection

- reflection follows *Snell's Law*:
 - incoming ray and reflected ray lie in a plane with the surface normal
 - angle the reflected ray forms with surface normal equals angle formed by incoming ray and surface normal

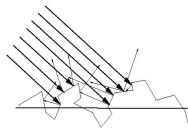


$\theta_{(l)ight} = \theta_{(r)eflection}$

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Non-Ideal Specular Reflectance

- Snell's law applies to perfect mirror-like surfaces, but aside from mirrors (and chrome) few surfaces exhibit perfect specularity
- how can we capture the "softer" reflections of surface that are glossy rather than mirror-like?
 - one option: model the microgeometry of the surface and explicitly bounce rays off of it
 - or...



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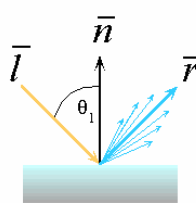
Empirical Approximation

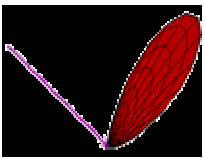
- we expect most reflected light to travel in direction predicted by Snell's Law
- but because of microscopic surface variations, some light may be reflected in a direction slightly off the ideal reflected ray
- as angle from ideal reflected ray increases, we expect less light to be reflected

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Empirical Approximation

- angular falloff




- how might we model this falloff?

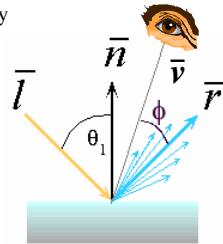
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Phong Lighting

- most common lighting model in computer graphics

$$I_{\text{specular}} = k_s I_{\text{light}} (\cos \phi)^{n_{\text{shiny}}}$$

- n_{shiny} : purely empirical constant, varies the rate of falloff
- no physical basis, works ok in practice



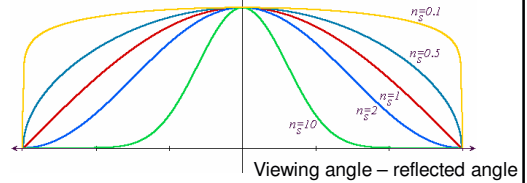
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Phong Lighting: The n_{shiny} Term

- Phong reflectance term drops off with divergence of viewing angle from ideal reflected ray



- what does this term control, visually?

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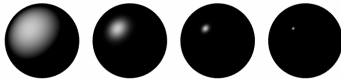
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Phong Examples

varying I



varying n_{shiny}



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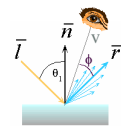
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Calculating Phong Lighting

- compute cosine term of Phong lighting with vectors

$$I_{\text{specular}} = k_s I_{\text{light}} (\mathbf{v} \cdot \mathbf{r})^{n_{\text{shiny}}}$$

- \mathbf{v} : unit vector towards viewer
- \mathbf{r} : ideal reflectance direction
- k_s : specular component
 - highlight color



- how to efficiently calculate \mathbf{r} ?

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Calculating The \mathbf{R} Vector

$\mathbf{P} = \mathbf{N} \cos \theta$ = projection of \mathbf{L} onto \mathbf{N}

$$\mathbf{P} + \mathbf{S} = \mathbf{R}$$

$$\mathbf{N} \cos \theta + \mathbf{S} = \mathbf{R}$$

$$\mathbf{S} = \mathbf{P} - \mathbf{L} = \mathbf{N} \cos \theta - \mathbf{L}$$

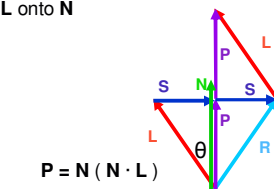
$$\mathbf{N} \cos \theta + (\mathbf{N} \cos \theta - \mathbf{L}) = \mathbf{R}$$

$$2 (\mathbf{N} \cos \theta) - \mathbf{L} = \mathbf{R}$$

$$\cos \theta = \mathbf{N} \cdot \mathbf{L}$$

$$2 (\mathbf{N} (\mathbf{N} \cdot \mathbf{L})) - \mathbf{L} = \mathbf{R}$$

\mathbf{N} and \mathbf{R} are unit length!



$$\mathbf{P} = \mathbf{N} (\mathbf{N} \cdot \mathbf{L})$$

$$2 \mathbf{P} = \mathbf{R} + \mathbf{L}$$

$$2 \mathbf{P} - \mathbf{L} = \mathbf{R}$$

$$2 (\mathbf{N} (\mathbf{N} \cdot \mathbf{L})) - \mathbf{L} = \mathbf{R}$$

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The Phong Lighting Model

- combine ambient, diffuse, specular components

$$I_{\text{total}} = k_a I_{\text{ambient}} + \sum_{i=1}^{\text{\#lights}} I_i (k_d (\mathbf{n} \cdot \mathbf{l}_i) + k_s (\mathbf{v} \cdot \mathbf{r}_i)^{n_{\text{shiny}}})$$

- commonly called *Phong lighting*

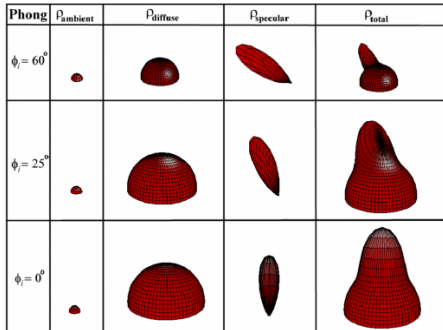
- once per light
- once per color component

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Phong Lighting: Intensity Plots



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Blinn-Phong Model

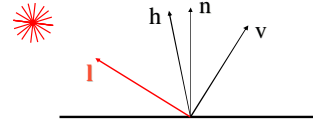
- variation with better physical interpretation

- Jim Blinn, 1977

- \mathbf{h} : halfway vector

- highlight occurs when \mathbf{h} near \mathbf{n}

$$I_{\text{out}}(\mathbf{x}) = k_s \cdot (\mathbf{h} \cdot \mathbf{n})^{n_{\text{shiny}}} \cdot I_{\text{in}}(\mathbf{x}); \text{ with } \mathbf{h} = (\mathbf{l} + \mathbf{v}) / 2$$



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Lighting Review

- lighting models
 - ambient
 - normals don't matter
 - Lambert/diffuse
 - angle between surface normal and light
 - Phong/specular
 - surface normal, light, and viewpoint

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Anisotropy

- so far we've been considering *isotropic* materials.
 - reflection and refraction invariant with respect to rotation of the surface about the surface normal vector.
 - for many materials, reflectance and transmission are dependent on this azimuth angle: *anisotropic* reflectance/transmission.
 - examples?

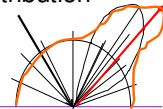
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BRDF

- Bidirectional Reflectance Distribution Function
- $\rho(\mathbf{x}, \omega_i, \omega_o)$
 - \mathbf{x} is the position.
 - $\omega_i = (\theta_i, \phi_i)$ represents the incoming direction. (elevation, azimuth)
 - $\omega_o = (\theta_o, \phi_o)$ represents the outgoing direction (elevation, azimuth)



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Properties of the BRDF

- dependent on both incoming and outgoing directions: *bidirectional*.
- always positive: *distribution function*.
- invariant to exchange of incoming/outgoing directions: *reciprocity principal*.
- in general, BRDFs are anisotropic.

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Dimensionality of BRDF

- function of position (3D), incoming, outgoing directions (4 angles), wavelength, and polarization.
 - thus, a 9D function!
 - usually simplify:
 - ignore polarization (geometric optics!).
 - sometimes ignore wavelength.
 - assume uniform material (ignore position).
 - isotropic reflectance makes one angle go away.