



University of British Columbia
CPSC 414 Computer Graphics

Advanced Rendering
Final Review

Week 13, Wed 26 Nov 2003

News

- proj 3 demo signup continues
 - record carefully, do **not** miss your demo slot!
- policy clarification
 - cannot use code from web for anything except low-level utilities like file loading (image files, object files)
 - must cite in writeup all web pages that were major inspiration

Schedule: Lab Hours for P3

- Mon Dec 1
 - AG 10-12, AW 12-2
- Tue Dec 2
 - AG 10-12, AW 12-2, TM 2-4
- Wed Dec 3
 - AW 1-2, PZ 2-4
- Thu Dec 4
 - AG 11-1
- Fri Dec 5
 - AG 10-11, PZ 11-1

Schedule: Lectures

- Wed (today)
 - advanced rendering, final review
- Fri
 - (finish review?), other graphics courses
 - evaluations, graphics in movies
 - Pixar shorts

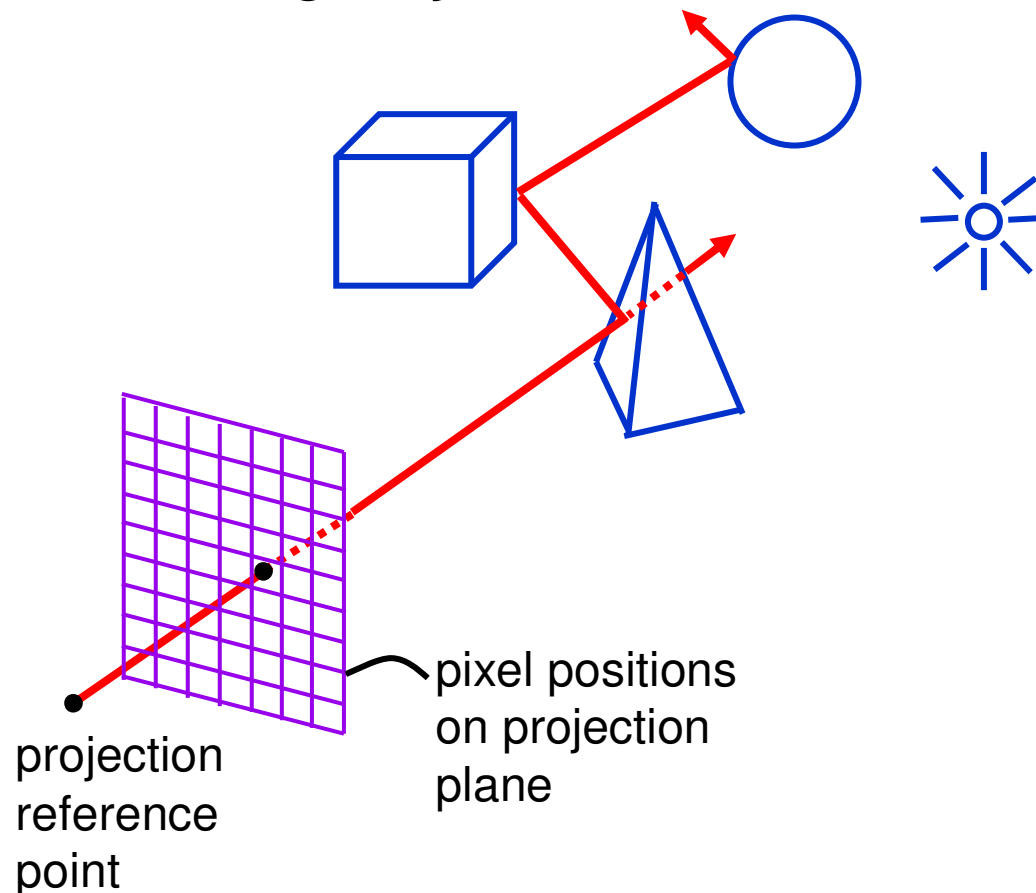


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Advanced Rendering

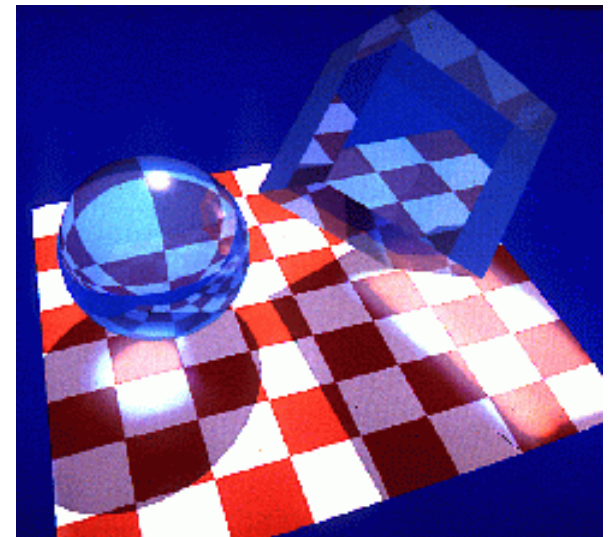
Ray Tracing

- cast a ray from the viewer's eye through each pixel
- compute intersection of ray with objects from scene
- closest intersecting object determines color



Recursive Ray Tracing

- cast ray from intersected object to light sources and determine shadow/lighting conditions
- also spawn secondary rays
 - reflection rays and refraction rays
 - use surface normal as guide (angle of incidence equals angle of reflection)
 - if another object is hit, determine the light it illuminates by recursing through ray tracing
- view-dependent

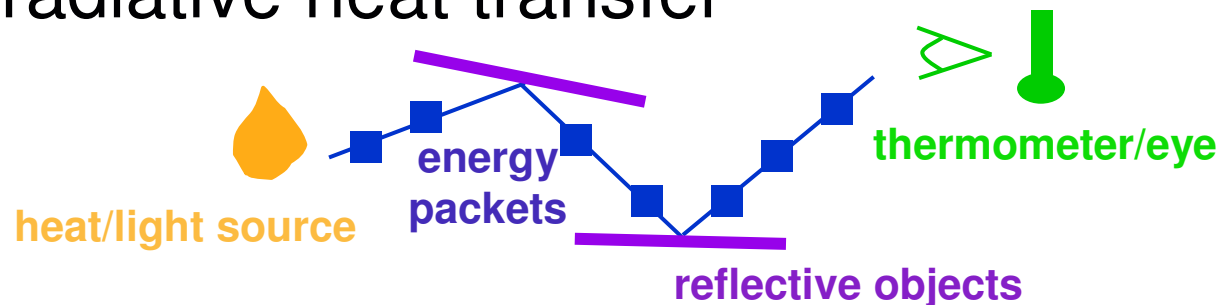


Radiosity

- rate at which energy emitted or reflected by a surface
 - conserve light energy in a volume
 - model light transport until convergence
 - solution captures diffuse-diffuse bouncing of light

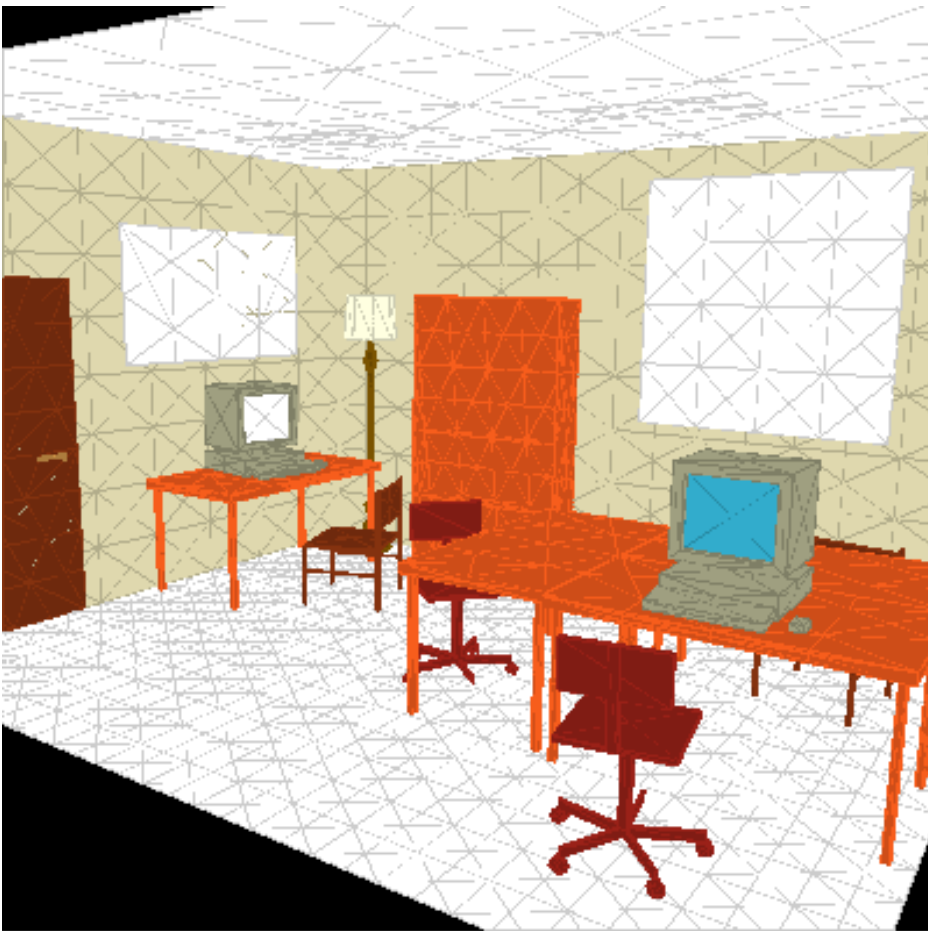


- recall radiative heat transfer



Radiosity

- divide surfaces into small patches
- check “form factor” between all patch pairs ($n \times n$ matrix)
- view-independent



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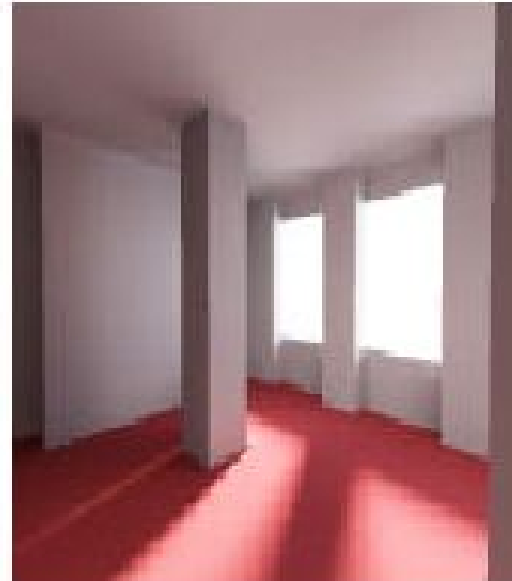
Comparison

- ray-tracing: great specular, approx diffuse
- radiosity: great diffuse, ignore specular
- advanced hybrids: combine them

raytraced

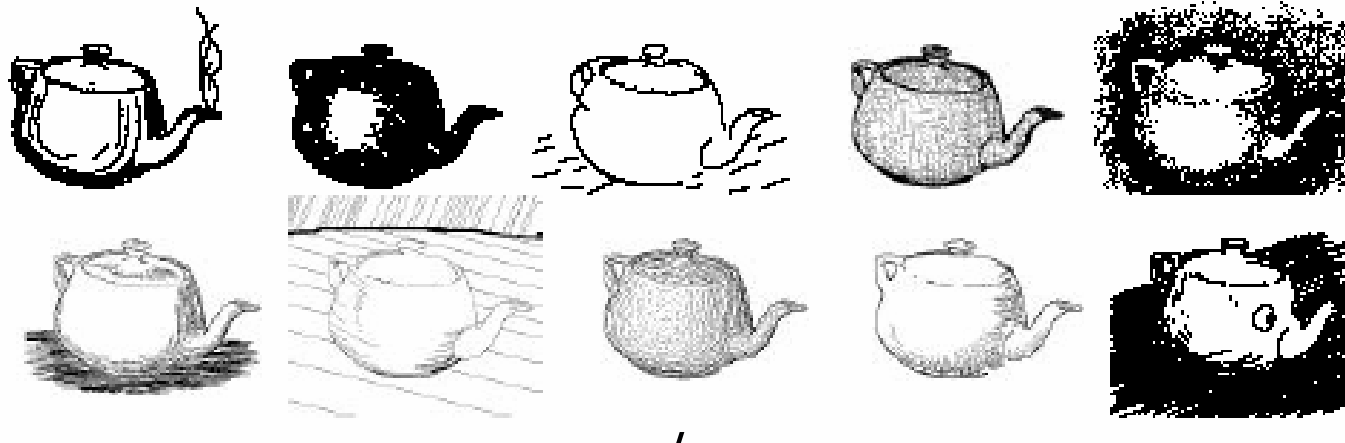
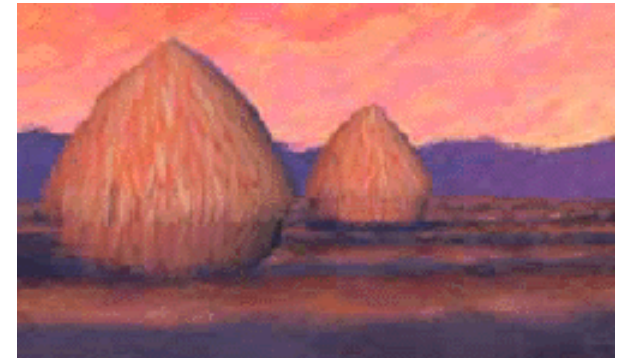
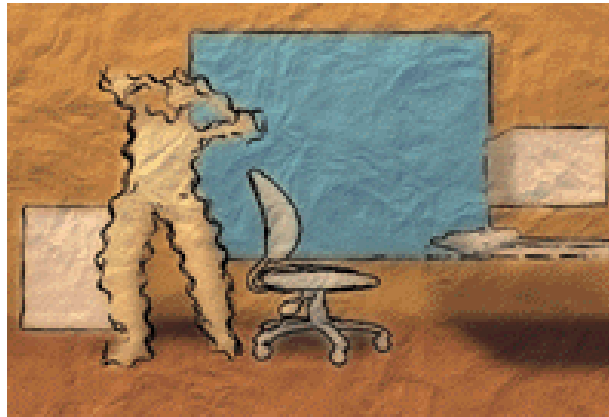


radiosity



Non-Photorealistic Rendering

- look of hand-drawn sketches or paintings



www.red3d.com/cwr/npr/

NPRQuake



www.cs.wisc.edu/graphics/Gallery/NPRQuake

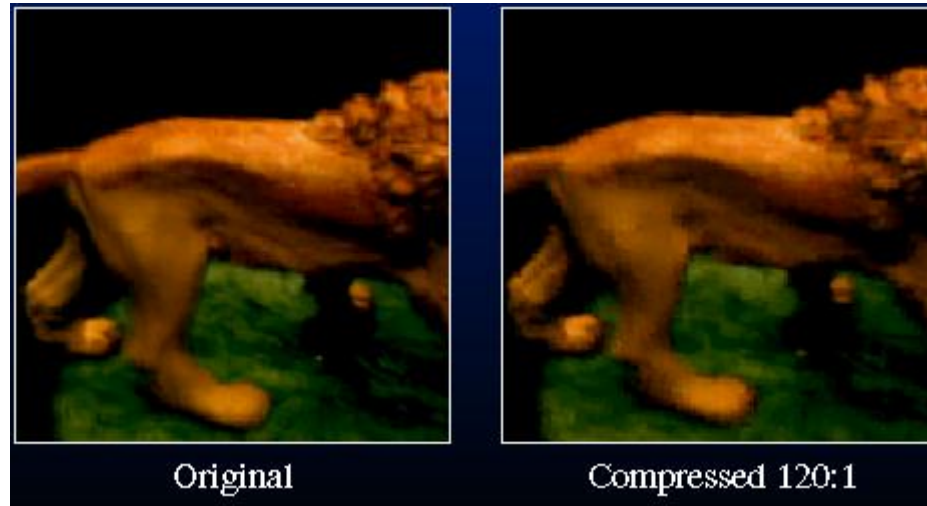
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Image-Based Rendering

- store and access only pixels
 - no geometry, no light simulation, etc!
 - massive compression possible (120:1)



- display time not tied to scene complexity
 - expensive rendering or real photographs



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Final Review

Logistics

- LSK 200, noon-3pm Tue Dec 9
- policies
 - must have student photo ID face up on desk
 - cannot take exam without photo ID
 - one piece of 8.5"x11" paper allowed
 - both sides handwritten
 - no other books or notes
 - nonprogrammable calculator OK
 - if you finish in last 15 minutes, stay put

Topics Covered

- rendering pipeline
- modelling transformations
- viewing transformations
- projections
- display lists
- picking
- lighting/shading
- rasterization/scan conversion
- sampling/antialiasing
- animation
- texturing
- clipping
- quaternions
- visibility
- color
- visualization
- displays
- procedural approaches
- curves
- advanced rendering

Midterm Covered, **Less Emphasis**

- rendering pipeline
 - modelling transformations
 - viewing transformations
 - projections
 - display lists
 - picking
 - lighting/shading
 - rasterization/scan conversion
 - sampling/antialiasing
 - animation
 - for these, look at midterm review notes
 - Week 7 Wed (16 Oct)
- texturing
 - clipping
 - quaternions
 - visibility
 - color
 - visualization
 - displays
 - procedural approaches
 - curves
 - advanced rendering

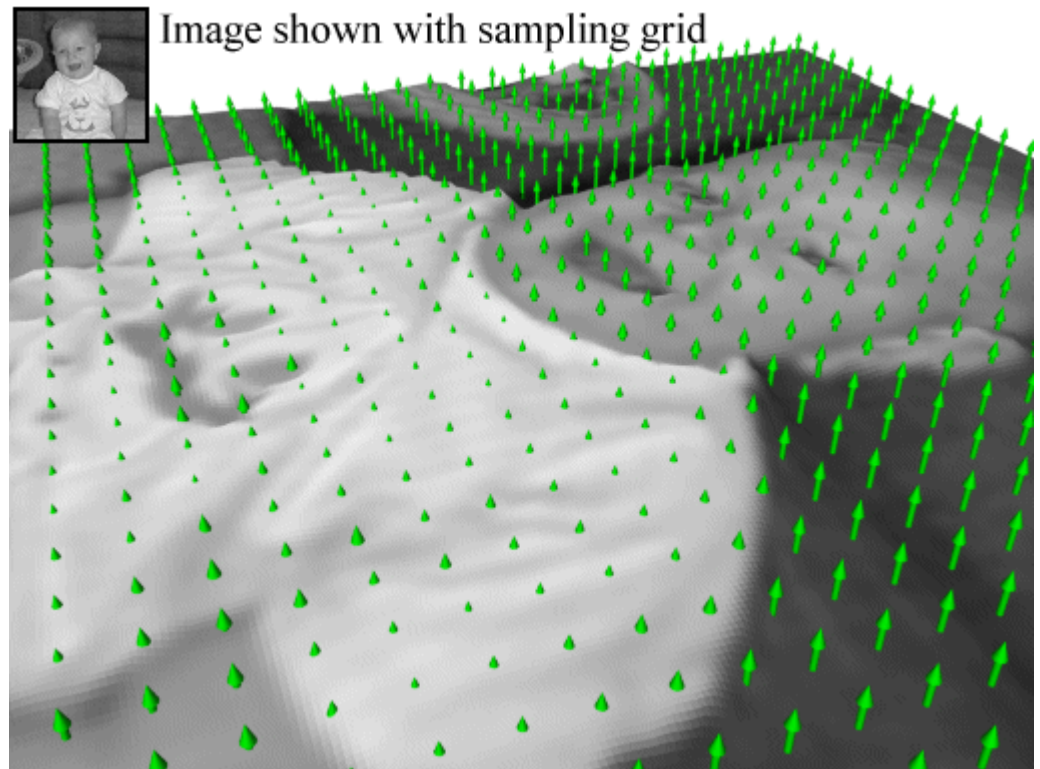
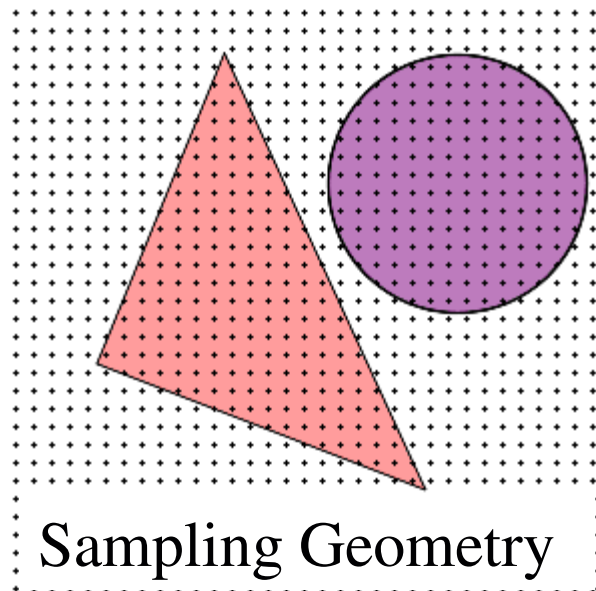


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Sampling and Antialiasing

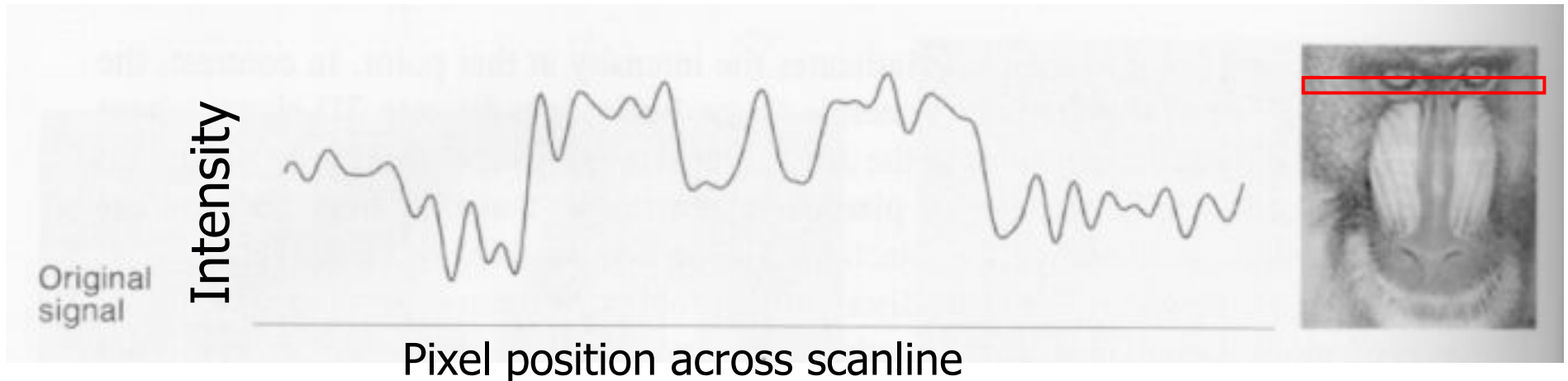
Point Sampling

- multiply sample grid by image intensity to obtain a discrete set of points, or samples.



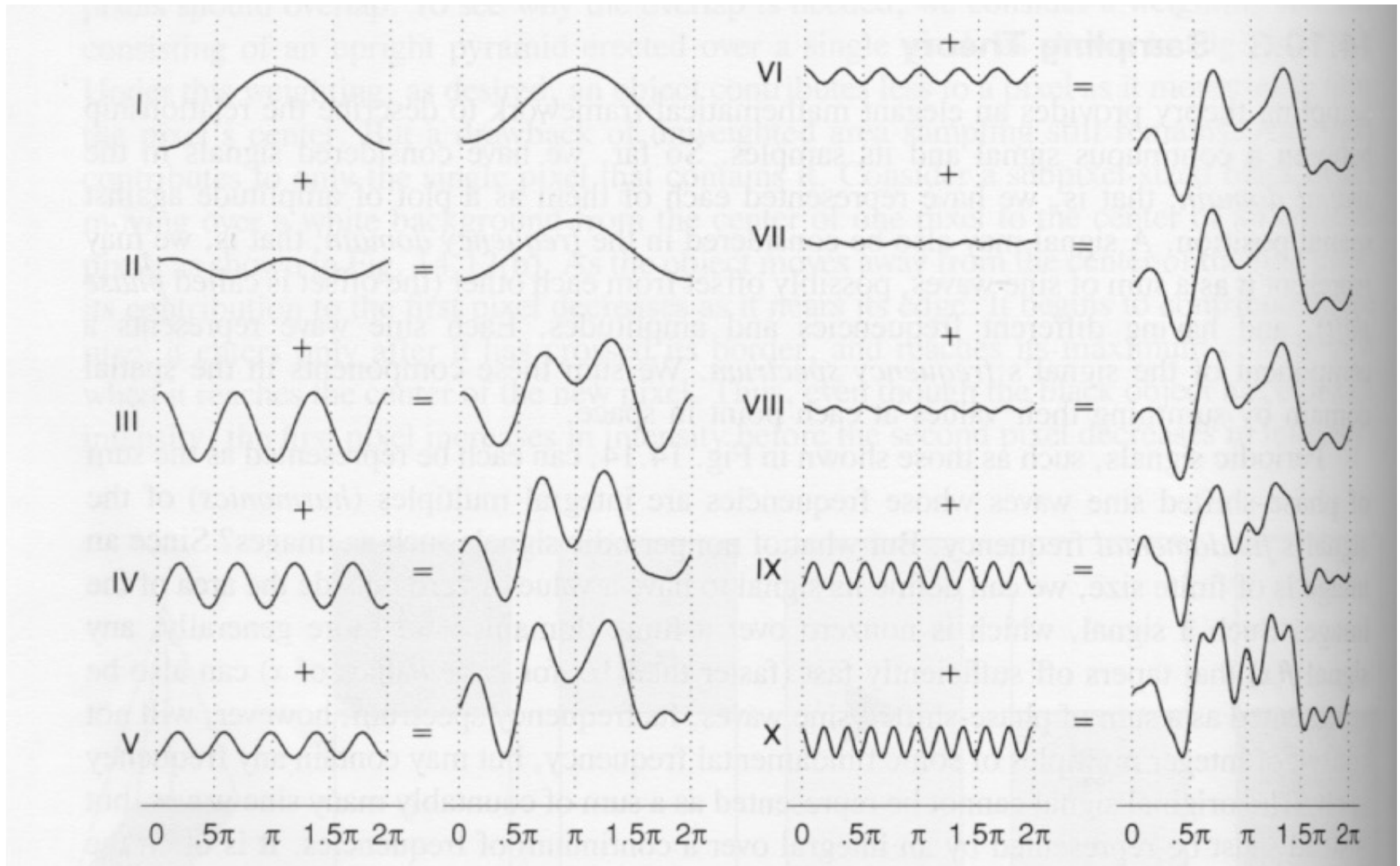
Spatial Domain

- image as spatial signal



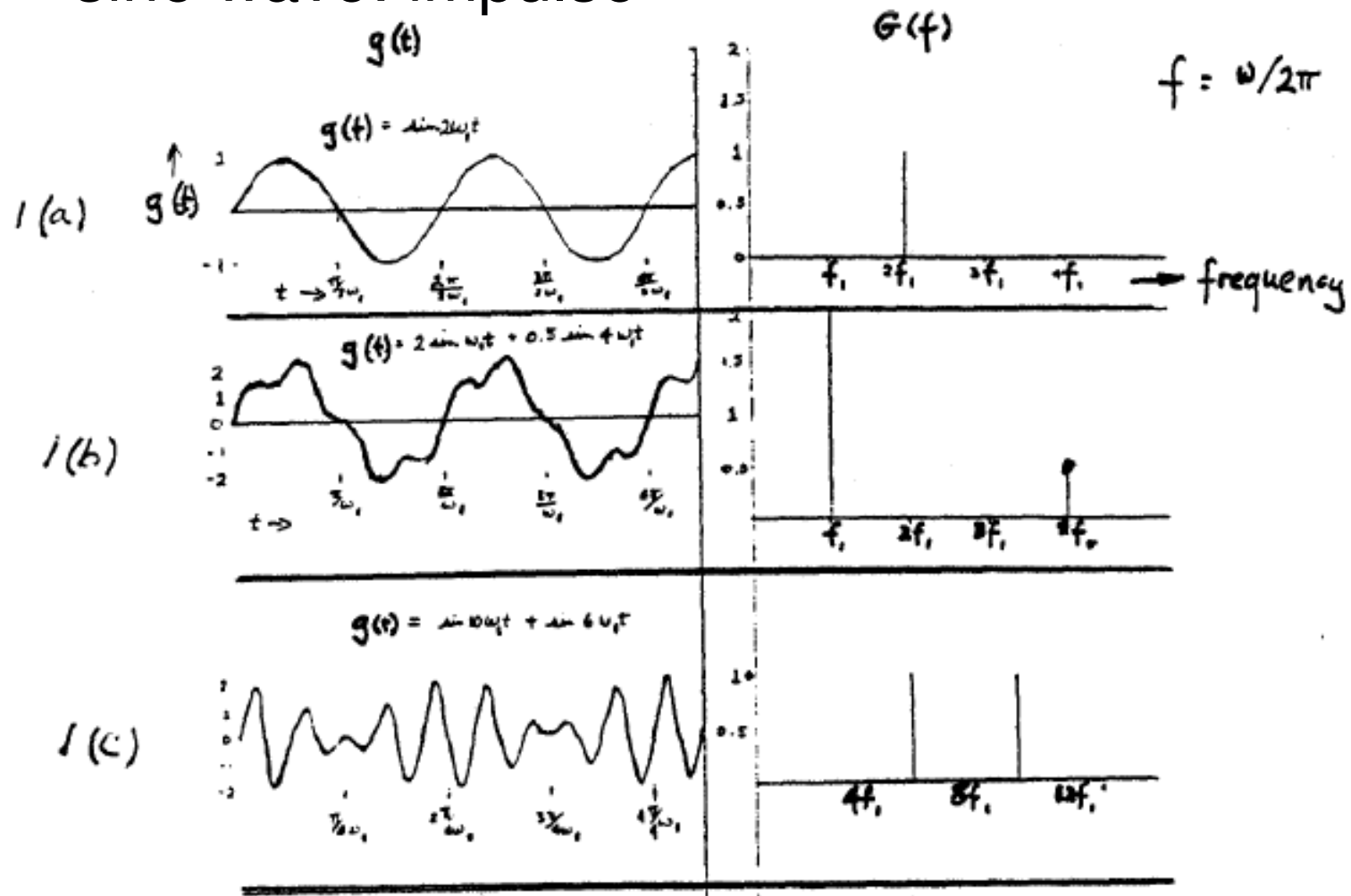
Examples from Foley, van Dam, Feiner, and Hughes

Spatial Domain: Summing Waves



Frequencies: Summing Spikes

- x : wavelength, y : strength
 - sine wave: impulse

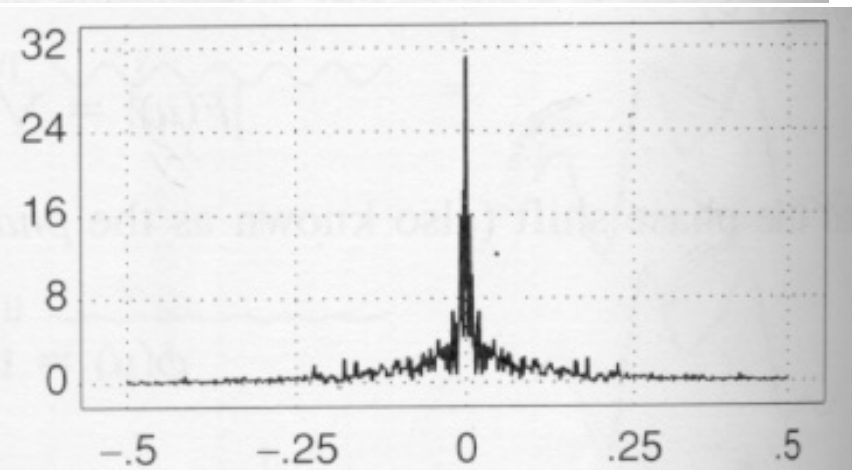
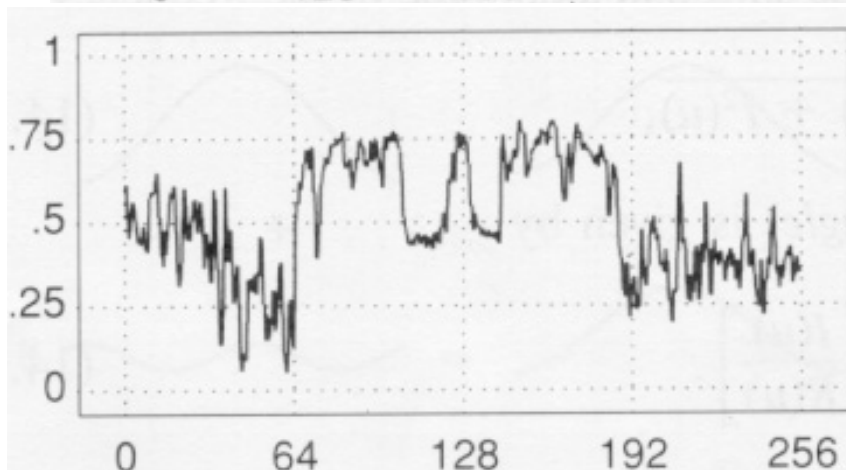
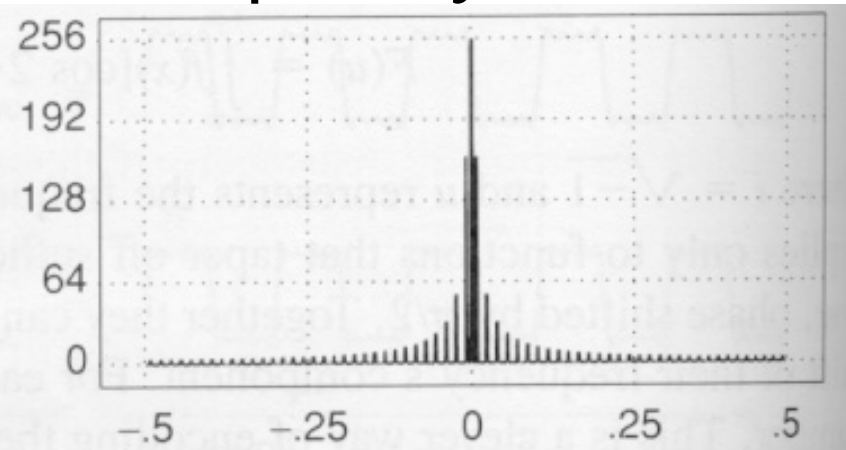
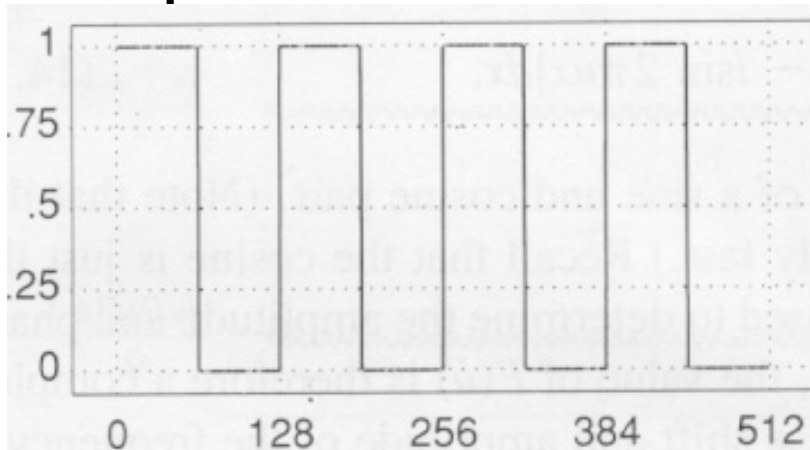


Fourier Transform Examples

- square wave: infinite train of impulses

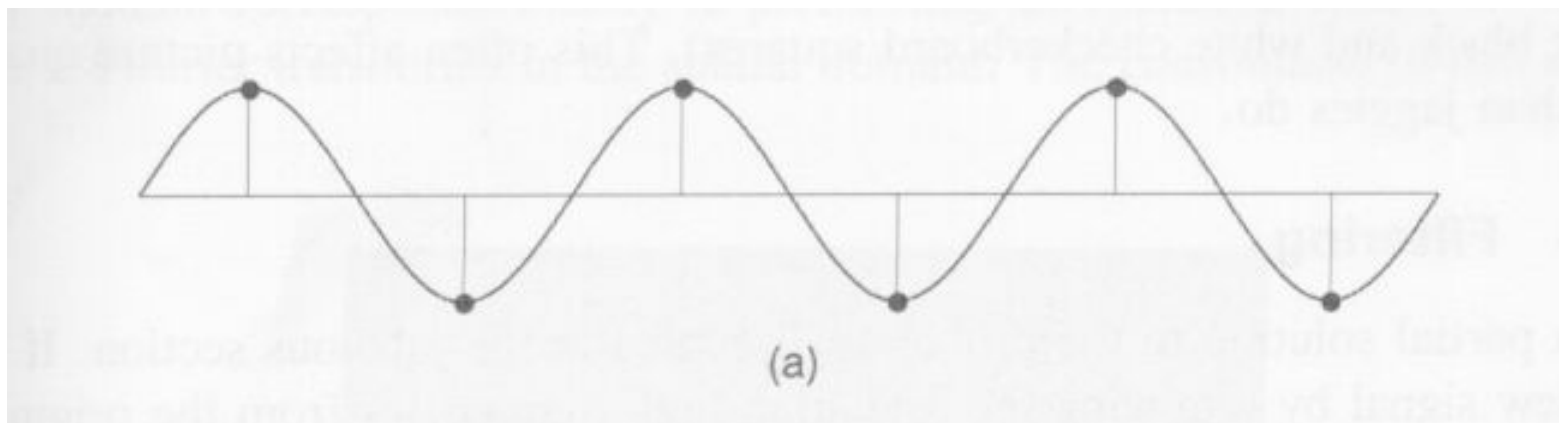
spatial domain

frequency domain



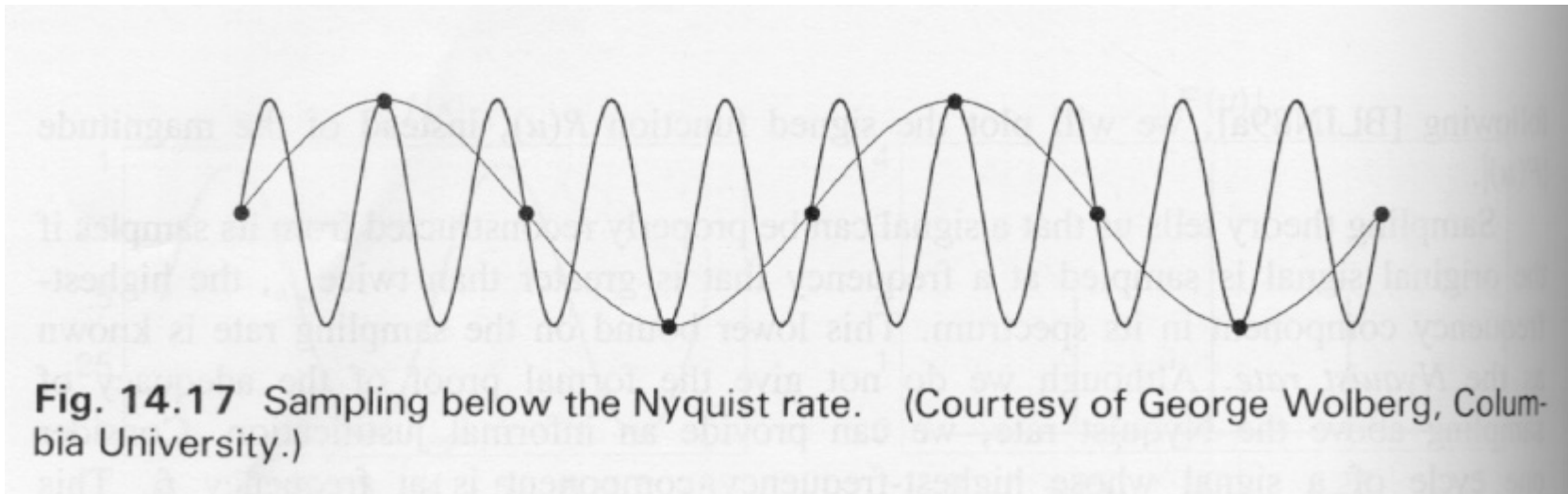
Nyquist Rate

- the lower bound on the sampling rate equals twice the highest frequency component in the image's spectrum
- this lower bound is the Nyquist Rate



Falling Below Nyquist Rate

- when sampling below Nyquist Rate, resulting signal looks like a lower-frequency one
 - this is **aliasing!**





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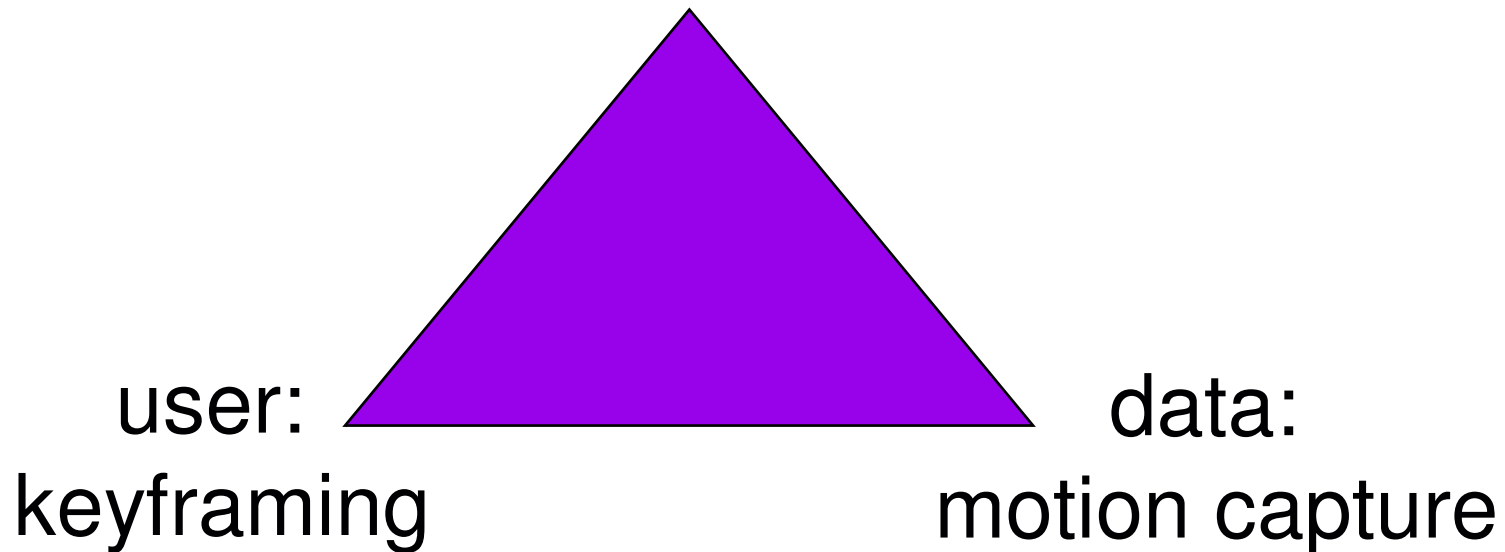
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Animation

Animation

algorithm:

simulating physics, parameterizing models



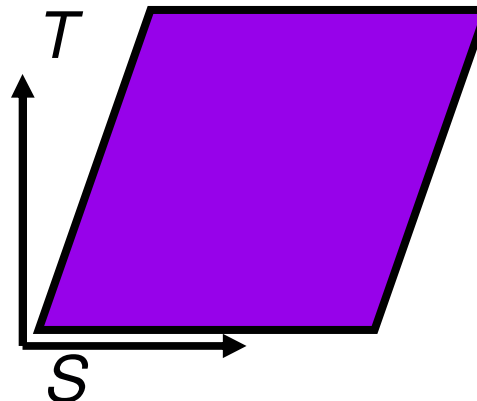
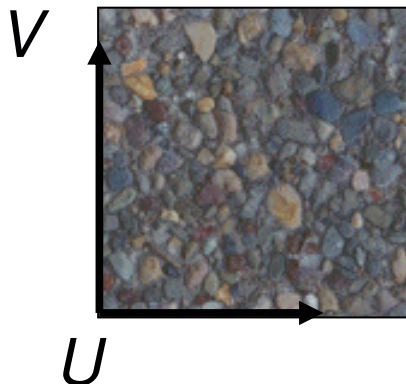


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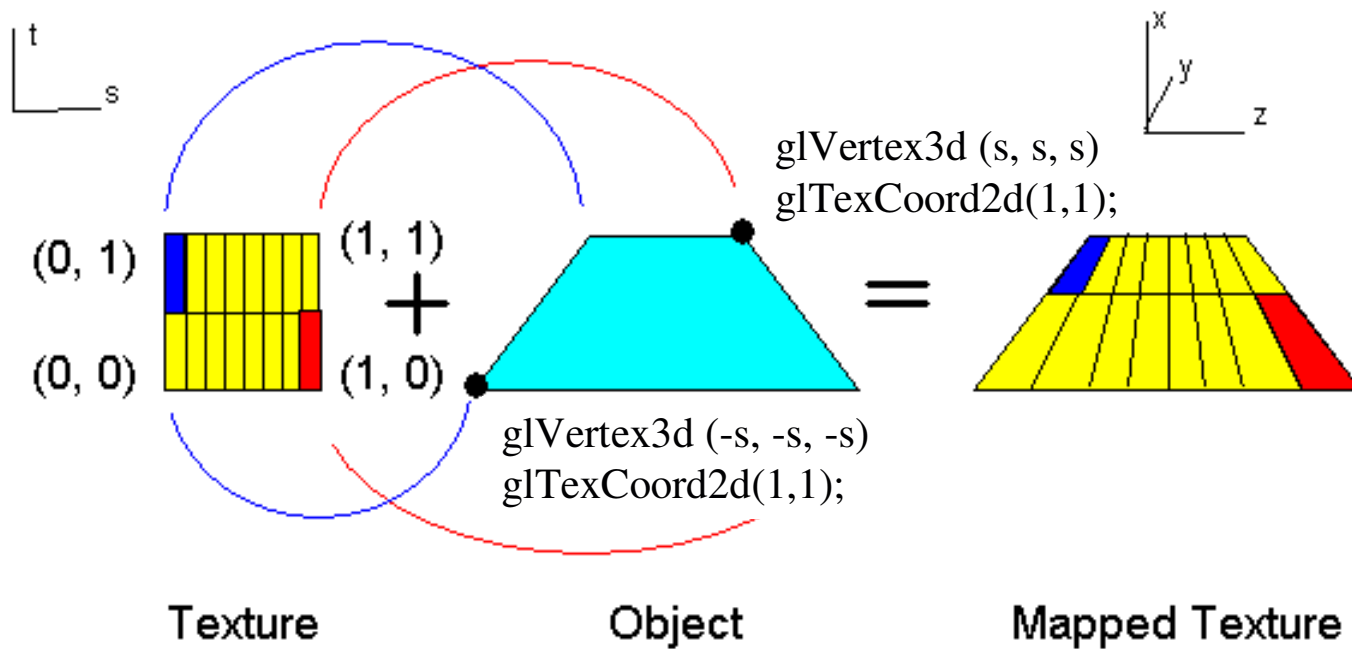
Texture Mapping

Texture Mapping

- texture map is an image, two-dimensional array of color values (texels)
- texels are specified by texture's (u,v) space
- at each screen pixel, texel can be used to substitute a polygon's surface property (color)
- we must map (u,v) space to polygon's (s, t) space

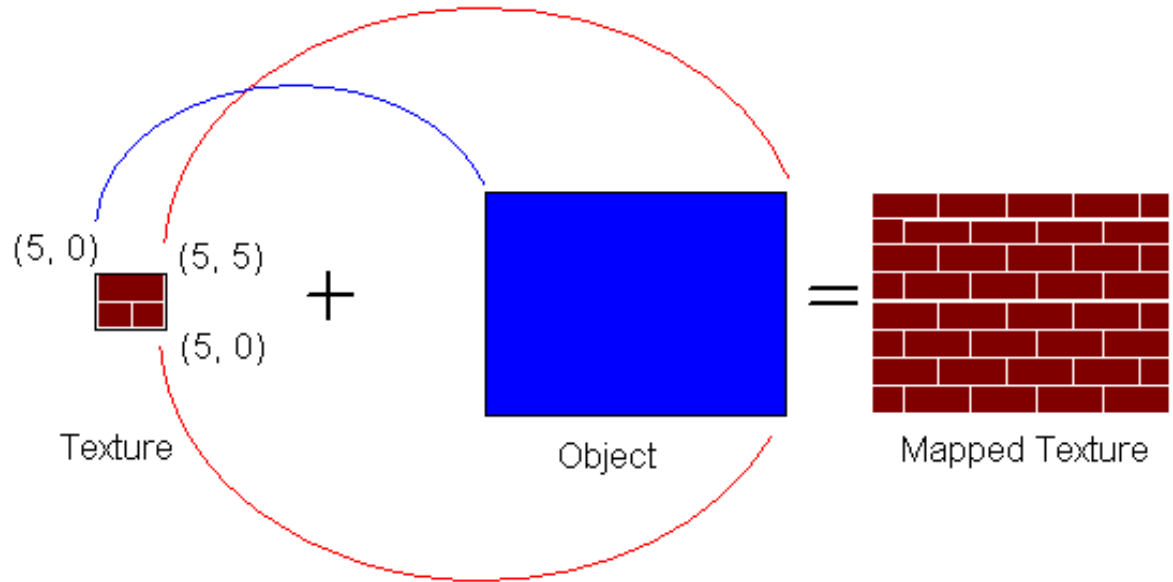


Example Texture Map

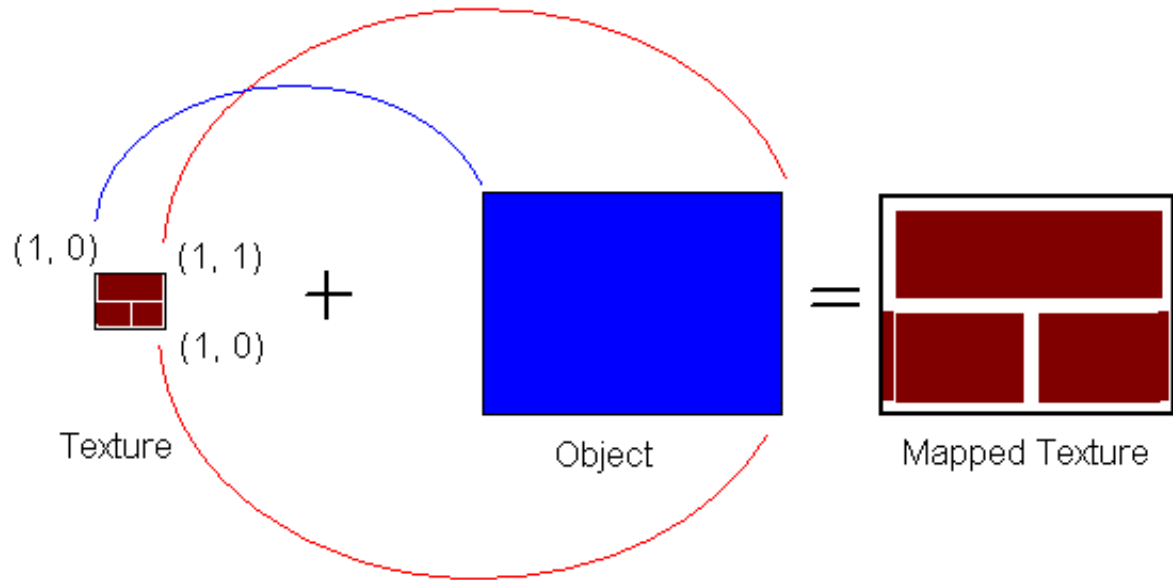


Texture Coordinate Transforms

```
glVertex3d (s, s, s)  
glTexCoord2d(5, 5);
```



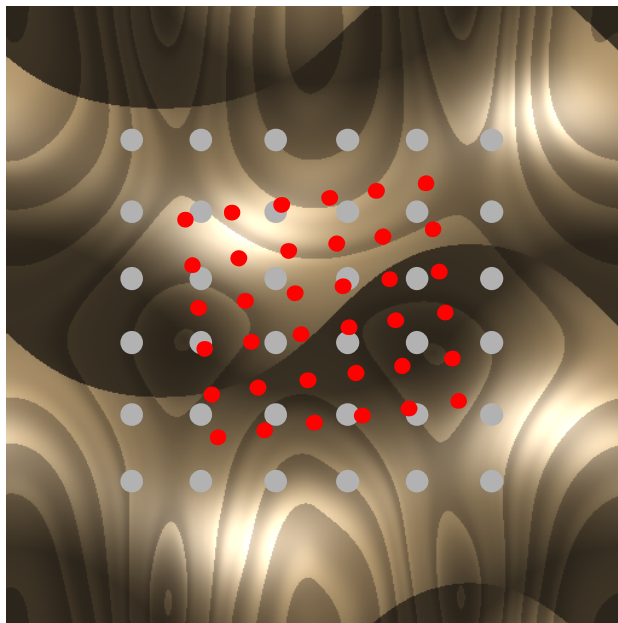
```
glVertex3d (s, s, s)  
glTexCoord2d(1, 1);
```



Texture Mapping and Filtering

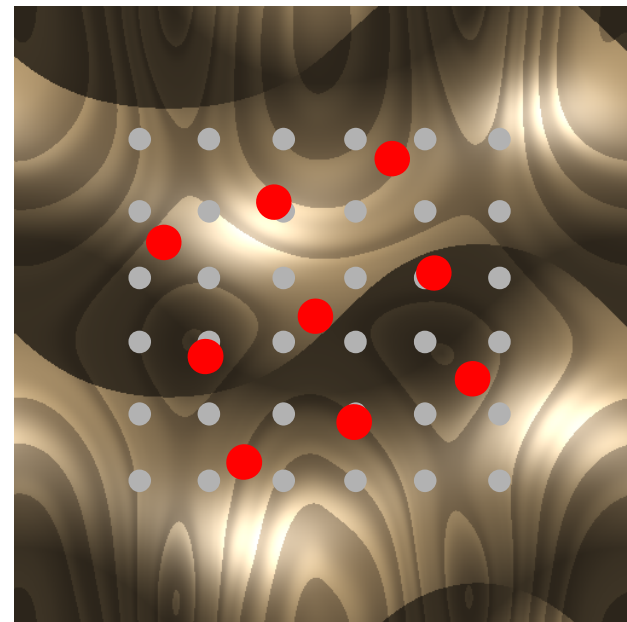
- in practice: 2 cases

texture magnification



interpolation

texture minification



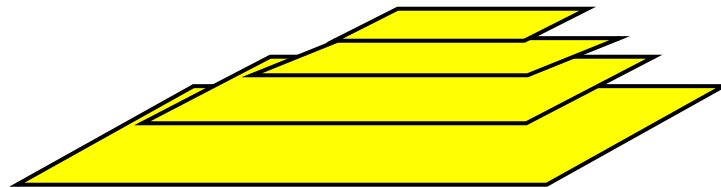
averaging

● Texel

● Pixel

Texture Minification Filters

- solution: precomputation
 - MIP-Mapping (Multum In Parvo)
 - “many things in a small place”
 - store not one texture image, but whole pyramid
 - resolution from level to level varies by factor of two (original resolution ... 1x1)
 - every level is correctly filtered for its resolution





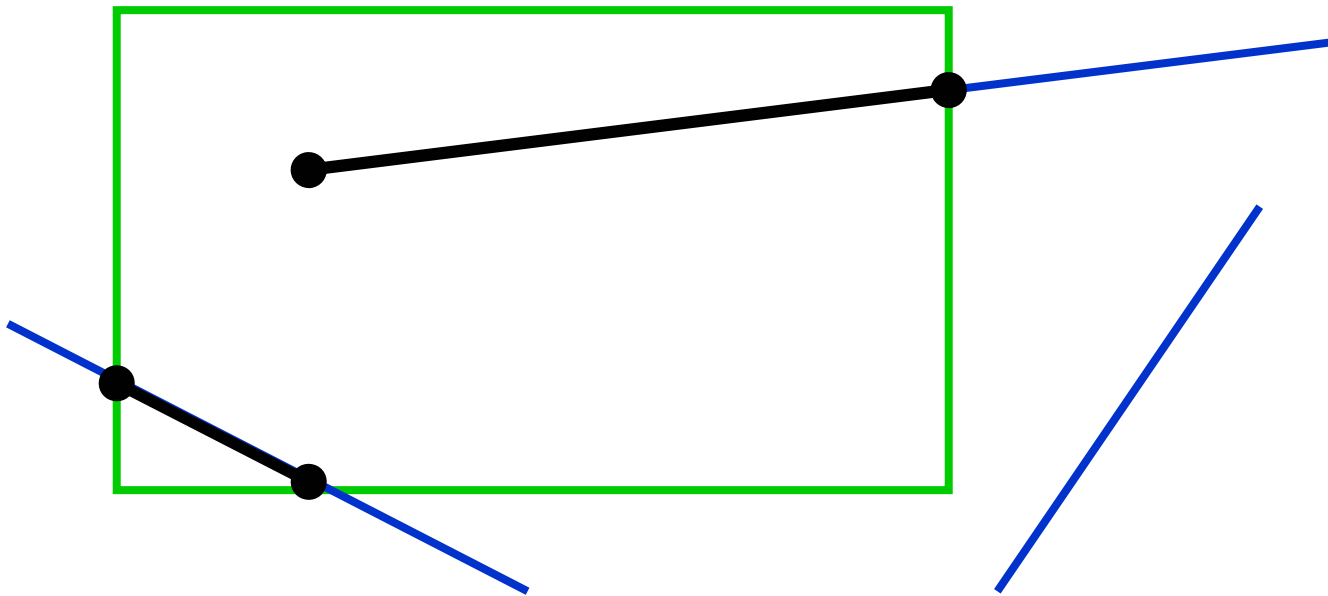
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Clipping

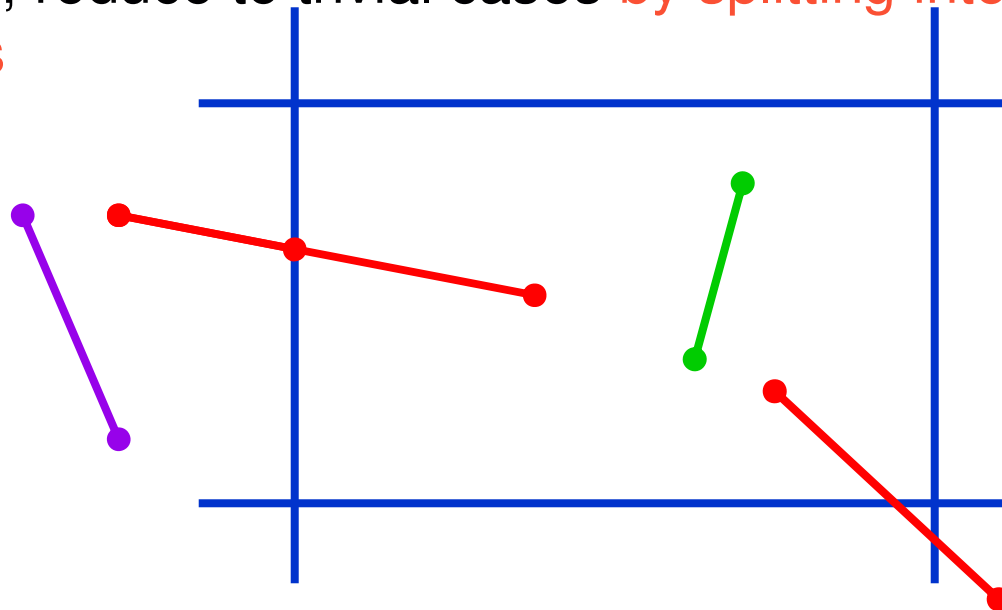
Clipping

- analytically calculating the portions of primitives within the viewport



Clipping Lines To Viewport

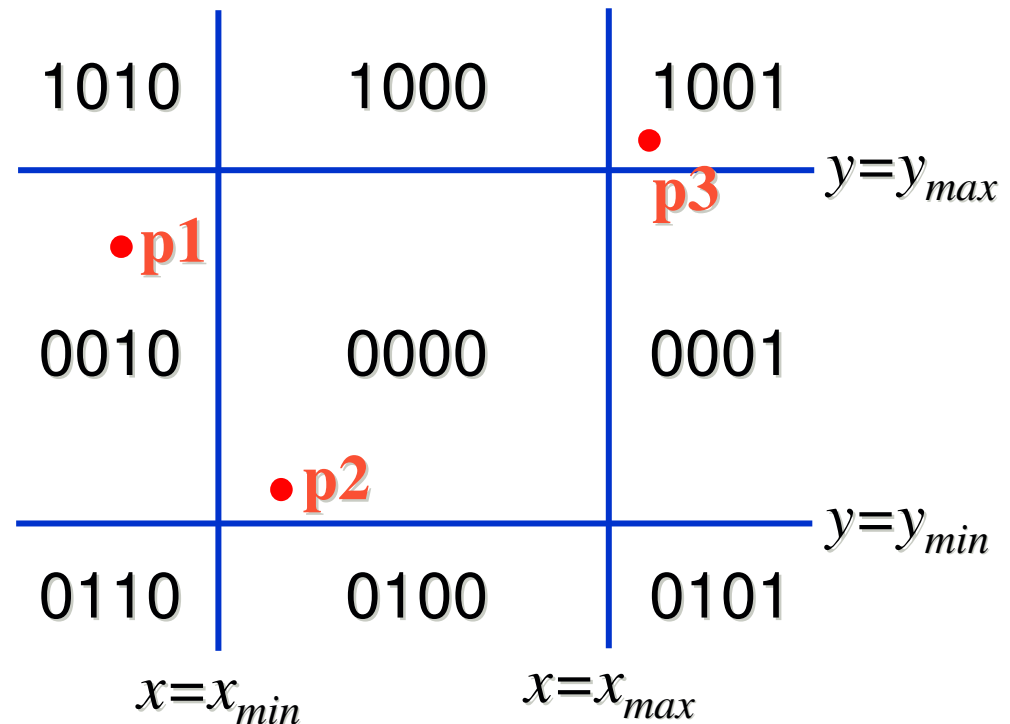
- combining trivial accepts/rejects
 - trivially **accept** lines with both endpoints **inside all edges of the viewport**
 - trivially **reject** lines with both endpoints **outside the same edge of the viewport**
 - otherwise, reduce to trivial cases **by splitting into two segments**



Cohen-Sutherland Line Clipping

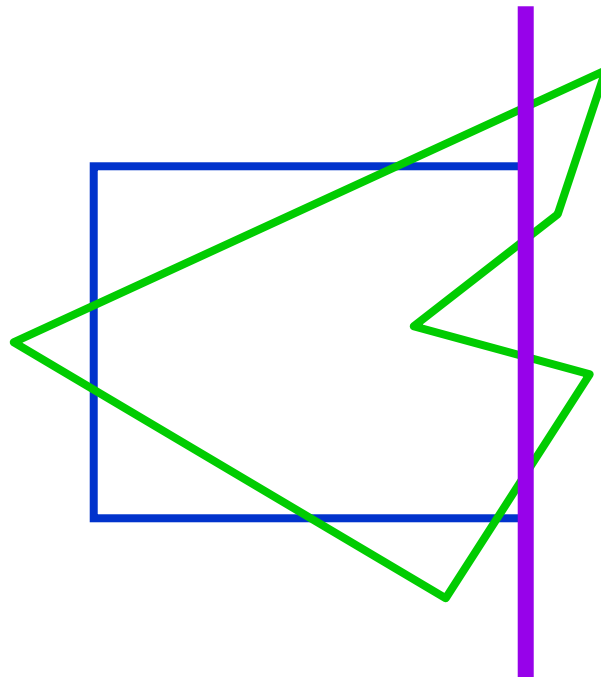
- outcodes
 - 4 flags encoding position of a point relative to top, bottom, left, and right boundary

- $OC(p1)=0010$
- $OC(p2)=0000$
- $OC(p3)=1001$



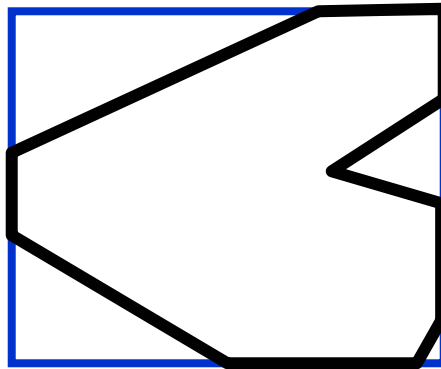
Sutherland-Hodgeman Polygon Clipping

- basic idea:
 - consider each edge of the viewport individually
 - clip the polygon against the edge equation
 - after doing all edges, the polygon is fully clipped



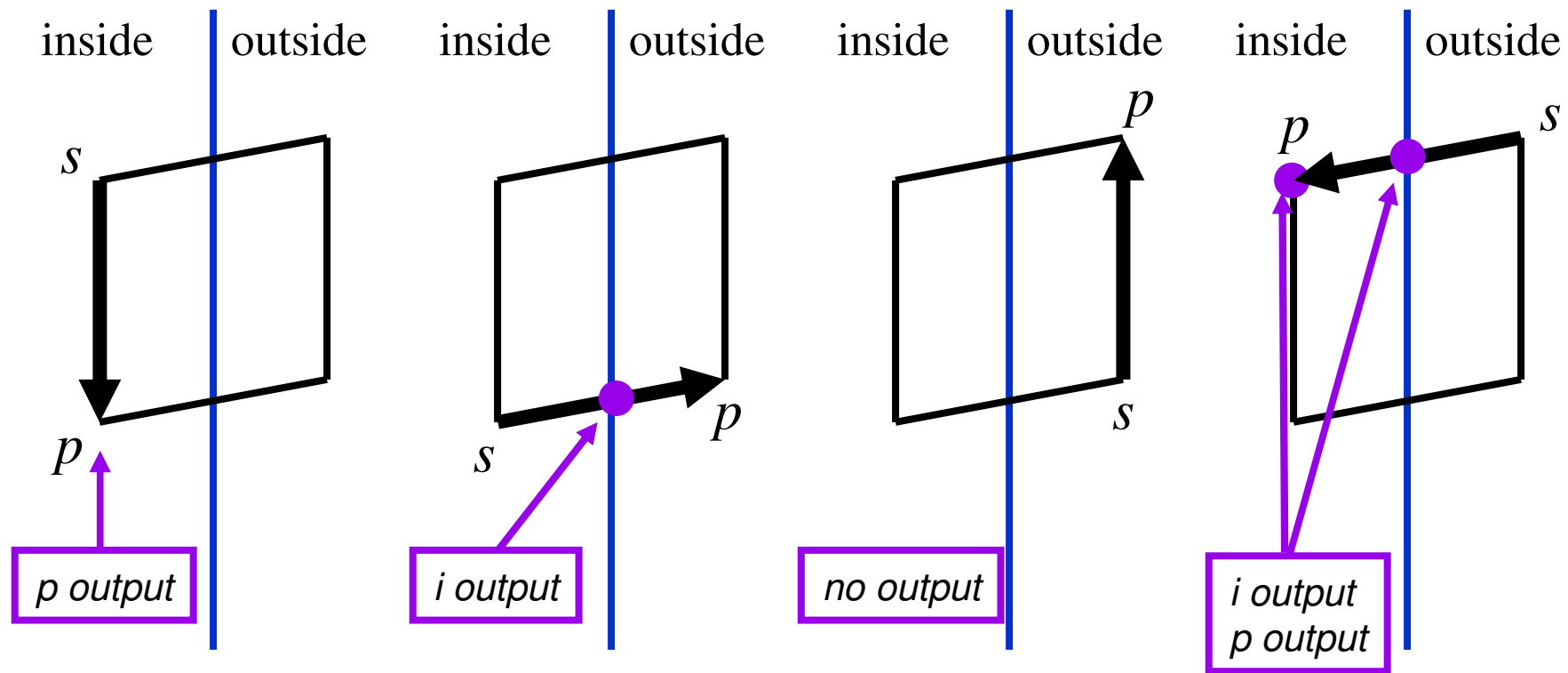
Sutherland-Hodgeman Clipping

- basic idea:
 - consider each edge of the viewport individually
 - clip the polygon against the edge equation
 - after doing all edges, the polygon is fully clipped



Sutherland-Hodgeman Clipping

- edge from s to p takes one of four cases:
(blue line can be a line or a plane)





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Rotation/Quaternions

Rotation Methods

- 3x3 matrices
 - good: simple. bad: drifting, can't interpolate
- Euler angles
 - good: can interpolate, no drift
 - bad: gimbal lock
- axis-angle
 - good: no gimbal lock, can interpolate
 - bad: can't concatenate
- quaternions
 - good: solve all problems. bad: complex

Quaternions

- quaternion is a 4-D unit vector $q = [x \ y \ z \ w]$
 - lies on the unit hypersphere $x^2 + y^2 + z^2 + w^2 = 1$
- for rotation about (unit) axis v by angle θ
 - vector part = $(\sin \theta/2) v = [x \ y \ z]$
 - scalar part = $(\cos \theta/2) = w$
- rotation matrix
$$\begin{bmatrix} 1-2y^2-2z^2 & 2xy+2wz & 2xz-2wy \\ 2xy-2wz & 1-2x^2-2z^2 & 2yz+2wx \\ 2xz+2wy & 2yz-2wx & 1-2x^2-2y^2 \end{bmatrix}$$
- quaternion multiplication $q_1 * q_2 =$
 $[v_1, w_1] * [v_2, w_2] = [(w_1 v_2 + w_2 v_1 + (v_1 \times v_2)), w_1 w_2 - v_1 \cdot v_2]$



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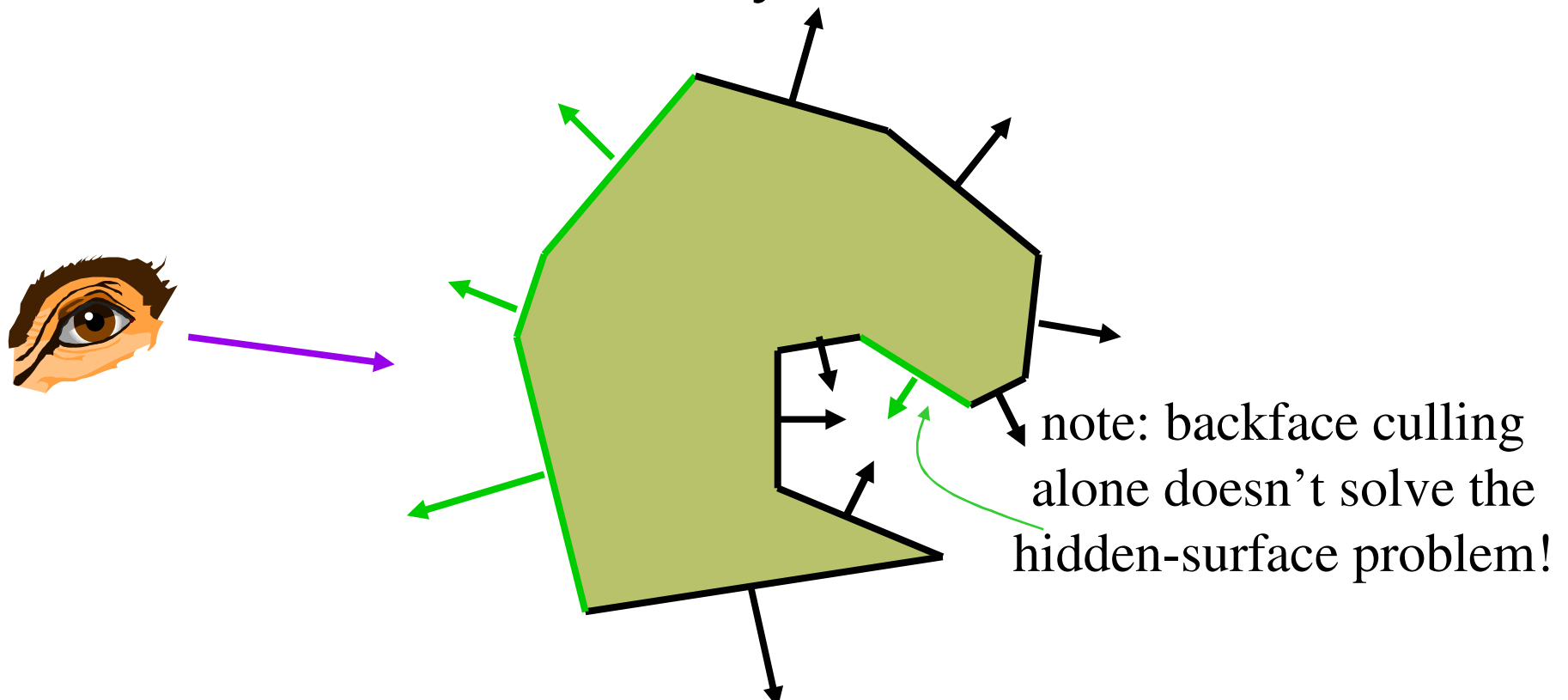
Visibility

Invisible Primitives

- why might a polygon be invisible?
 - polygon outside the *field of view / frustum*
 - clipping
 - polygon is *backfacing*
 - backface culling
 - polygon is *occluded* by object(s) nearer the viewpoint
 - hidden surface removal

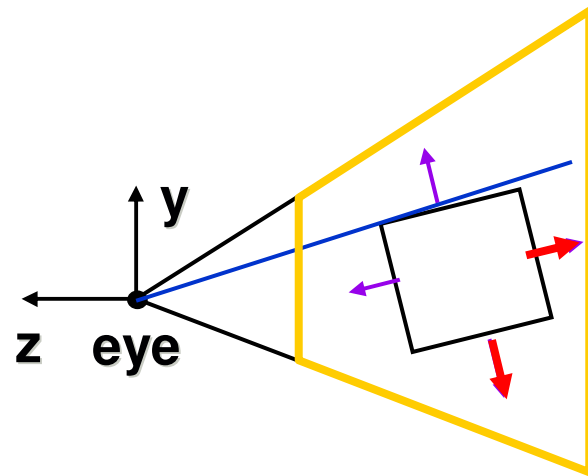
Back-Face Culling

- on the surface of a closed manifold, polygons whose normals point away from the camera are always occluded:



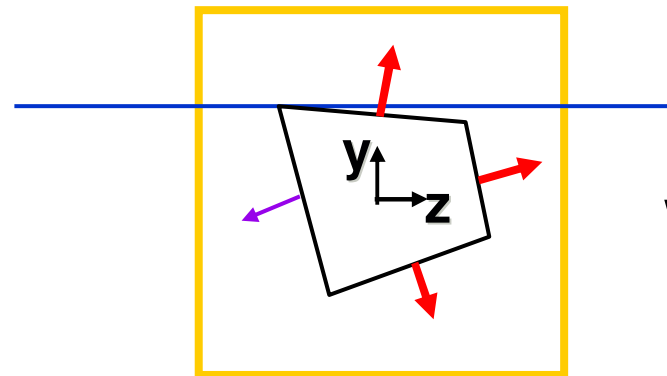
Back-face Culling: NDCS

VCS



NDCS

eye



works to cull if $N_z > 0$

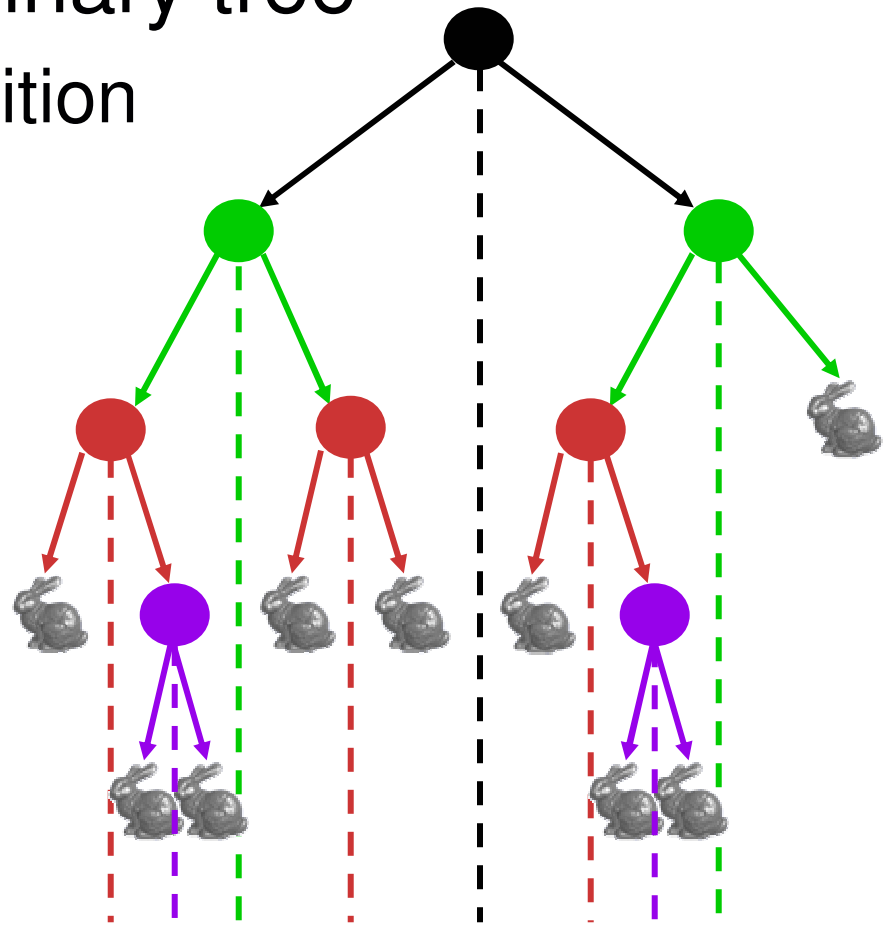
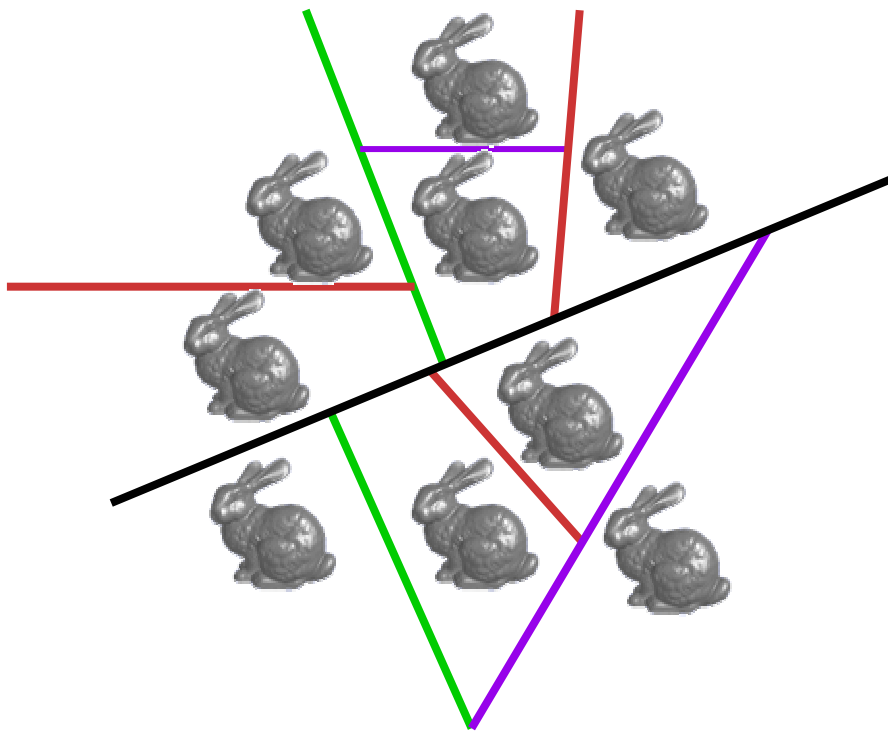
Painter's Algorithm

- draw objects from **back to front**
- problems: no valid visibility order for
 - intersecting polygons
 - cycles of non-intersecting polygons possible



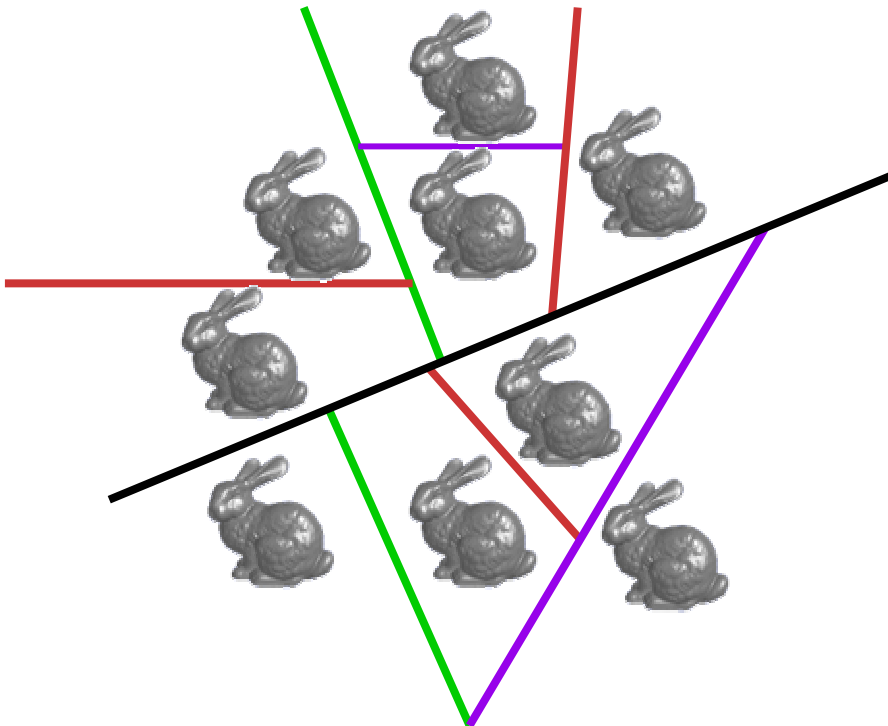
BSP Trees

- preprocess: create binary tree
 - recursive spatial partition

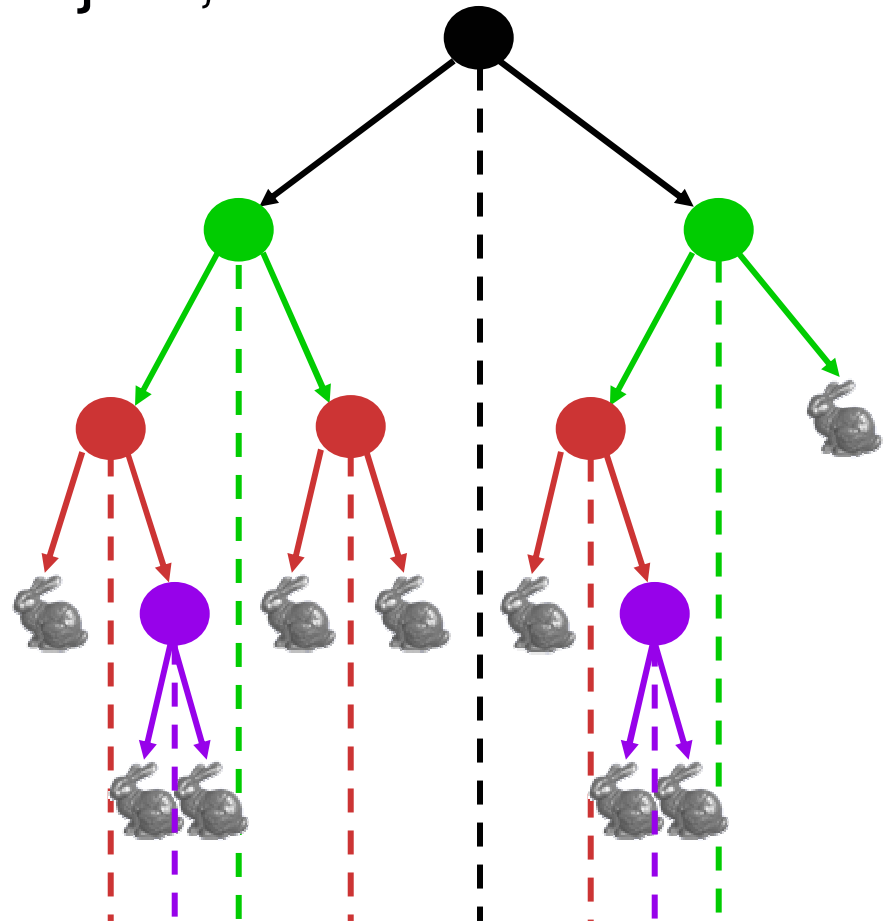


BSP Trees

- runtime: traverse tree
 - check node's plane vs. eyepoint
 - recurse on far, draw object, recurse on near



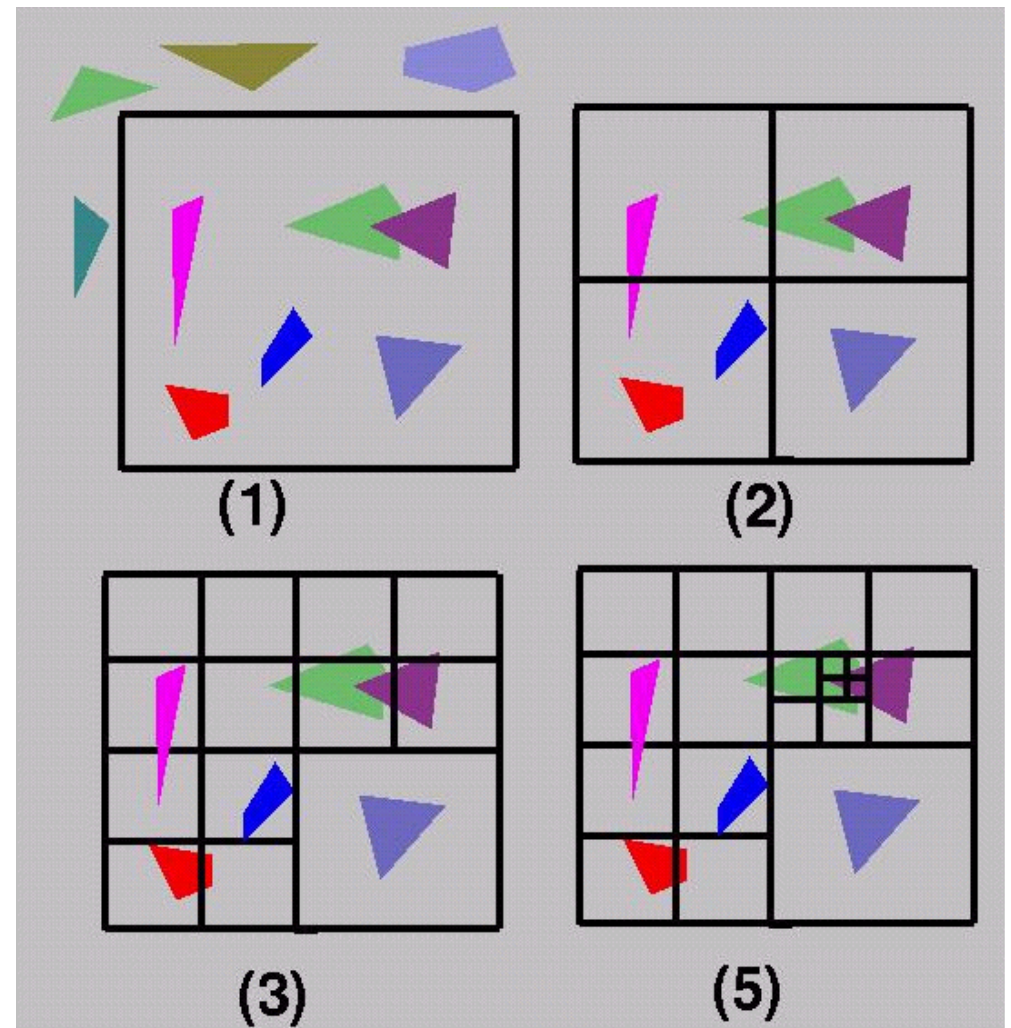
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Warnock's Algorithm

- recursive
 - start at root viewport of entire window
 - clip objects to current viewport
 - trivial if 0 or 1 objects
 - subdivide if more
 - stop if trivial or down to one pixel



The Z-Buffer Algorithm

- augment color framebuffer with **Z-buffer** or **depth buffer** which stores Z value at each pixel
 - at frame beginning, initialize all pixel depths to ∞
 - when rasterizing, interpolate depth (Z) across polygon and store in pixel of Z-buffer
 - suppress writing to a pixel if its Z value is more distant than the Z value already stored there
 - depth-buffer essentially stores $1/z$, rather than z

Hidden Surface Removal

- image-space algorithms
 - Z-buffer, Warnock's
 - perform visibility test for every pixel independently
 - performed late in rendering pipeline, resolution dependent
- object-space algorithms
 - painter's algorithm: depth-sorting, BSP trees
 - determine visibility on a polygon level in camera coordinates
 - early in rendering pipeline (after clipping)
 - resolution independent
 - expensive

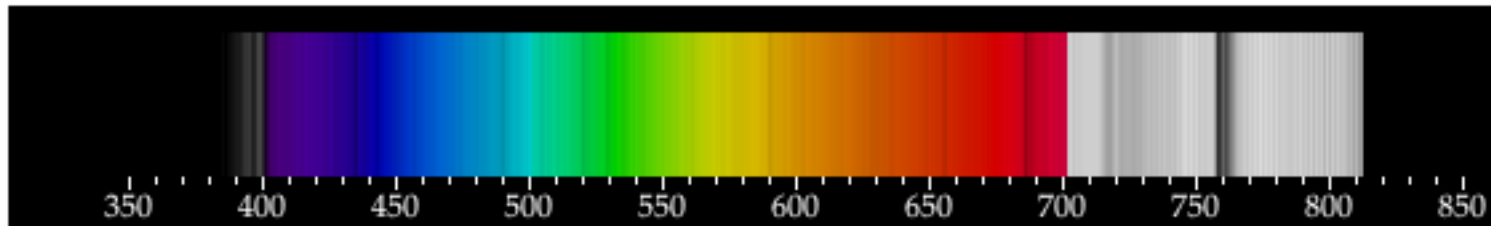


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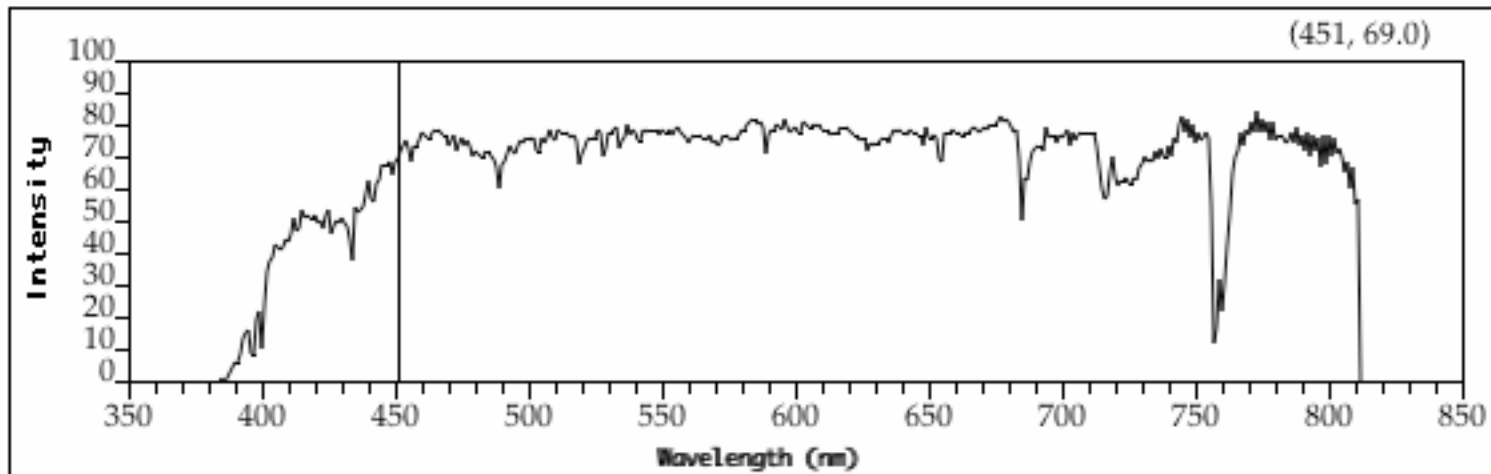
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Color

Sunlight Spectrum



Emission Graph



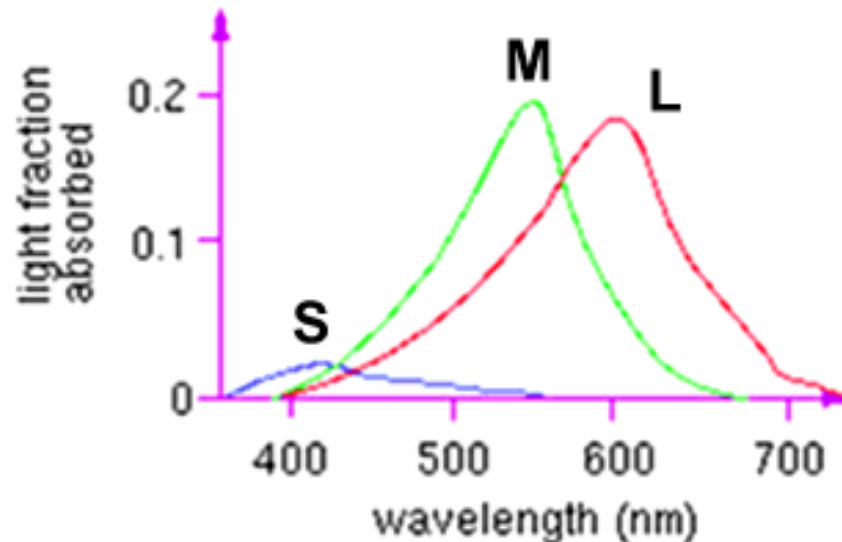
Electromagnetic Spectrum

Humans and Light

- when we view a source of light, our eyes respond to
 - hue: the color we see (red, green, purple)
 - dominant frequency
 - saturation: how far is color from grey
 - how far is the color from gray (pink is less saturated than red, sky blue is less saturated than royal blue)
 - brightness: how bright is the color
 - how bright are the lights illuminating the object?

Trichromacy

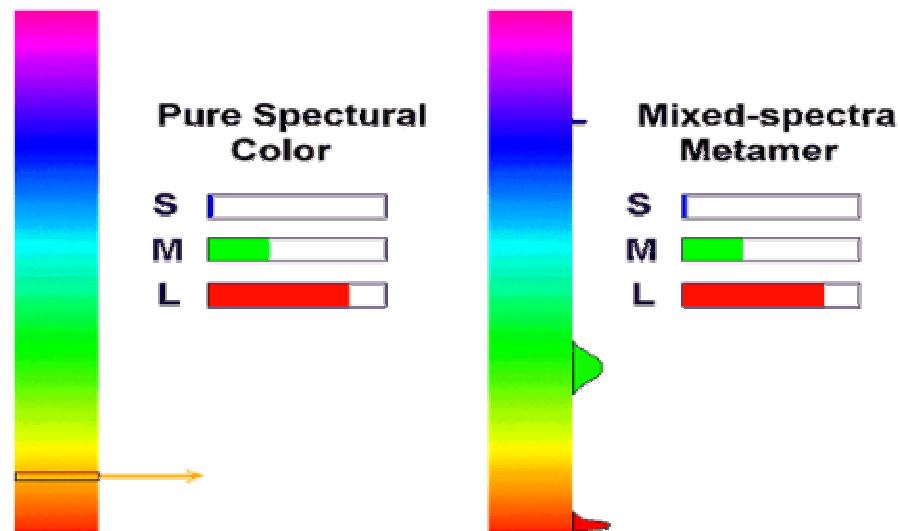
- three types of cones
 - L or R, most sensitive to red light (610 nm)
 - M or G, most sensitive to green light (560 nm)
 - S or B, most sensitive to blue light (430 nm)



– color blindness results from missing cone type(s)

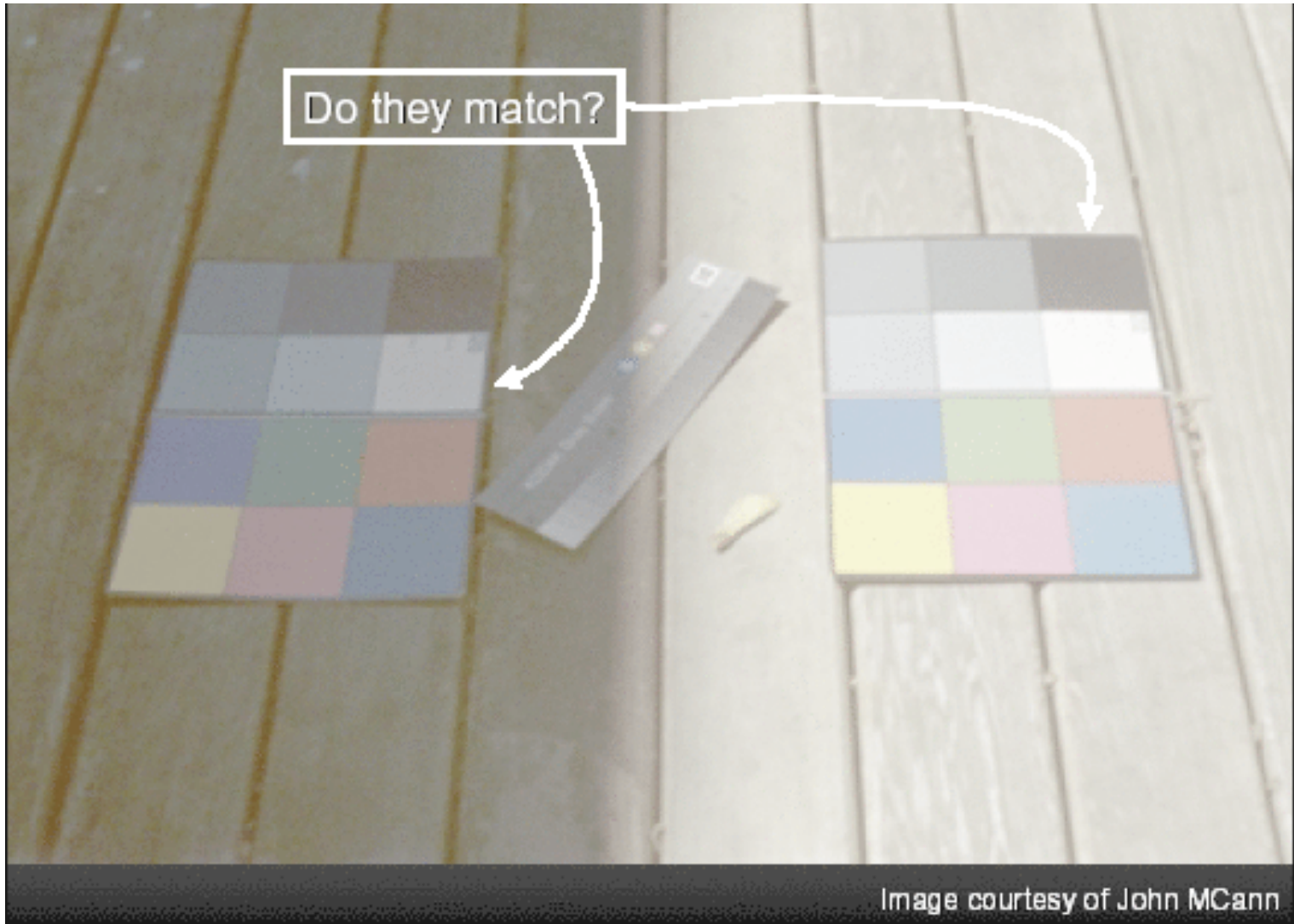
Metamers

a given perceptual sensation of color derives from the stimulus of all three cone types

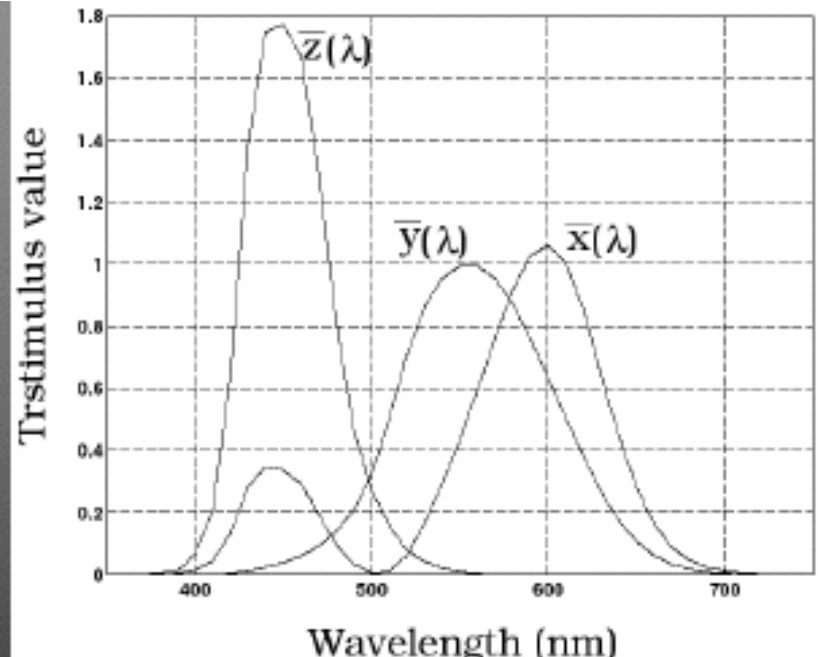
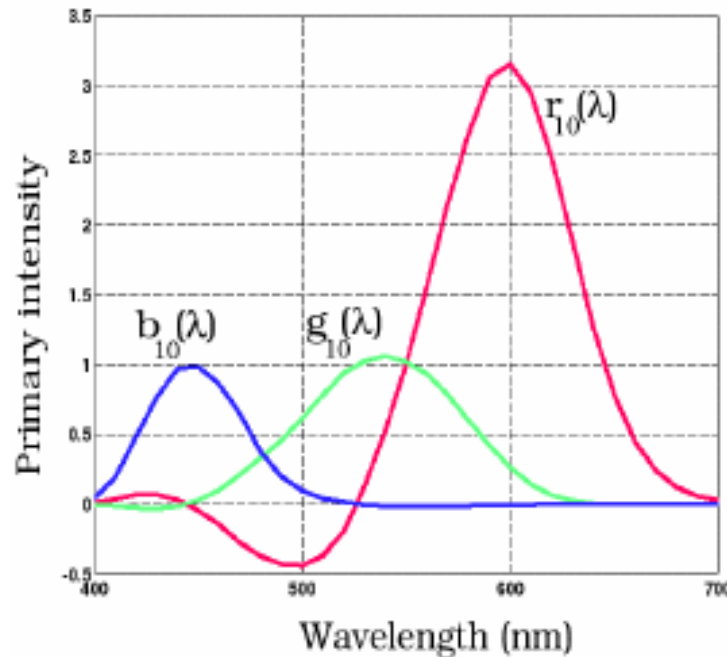


- identical perceptions of color can thus be caused by very different spectra

Color Constancy



Measured vs. CIE Color Spaces

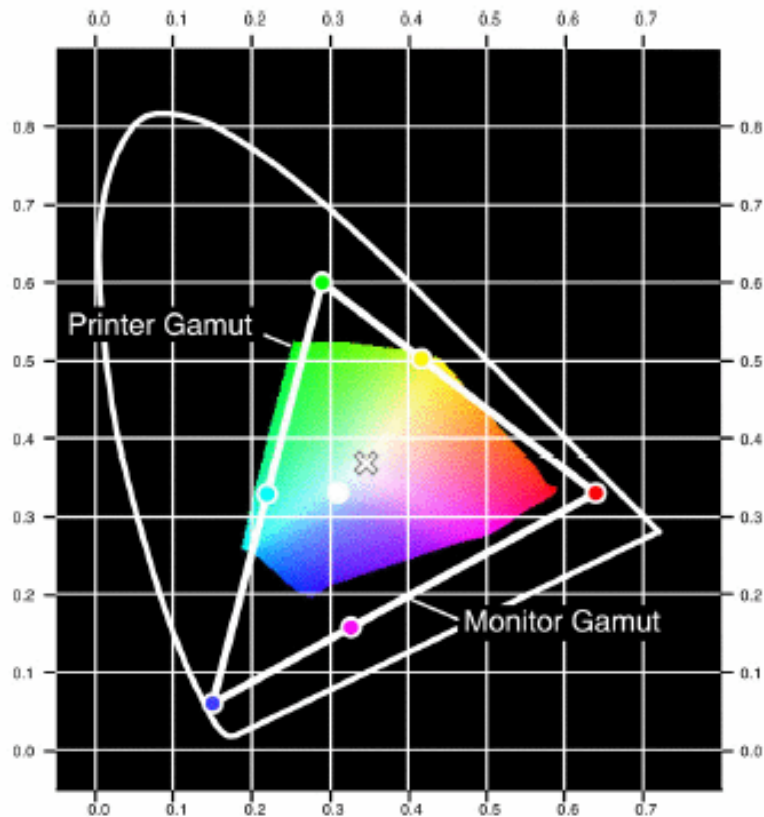


- measured basis
 - monochromatic lights
 - physical observations
 - negative lobes

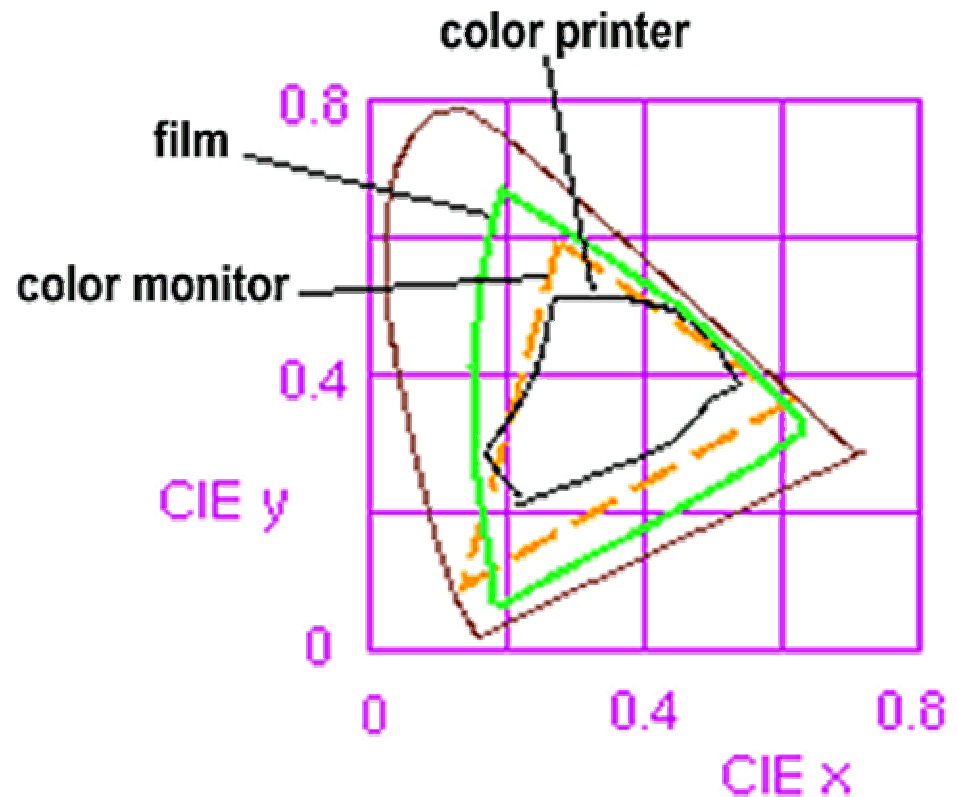
- transformed basis
 - “imaginary” lights
 - all positive, unit area
 - Y is luminance

Device Color Gamuts

- use CIE chromaticity diagram to compare the gamuts of various devices



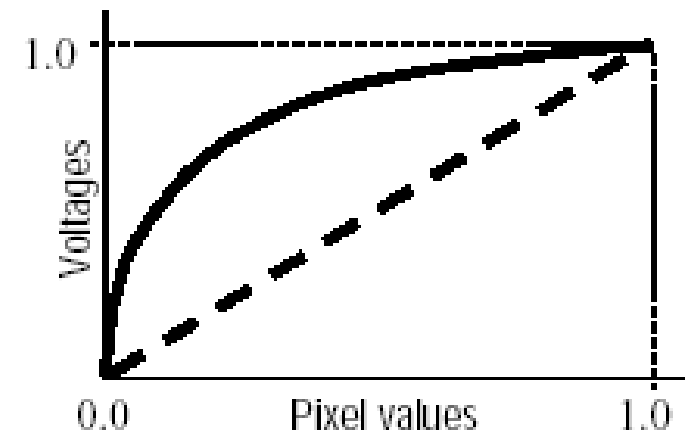
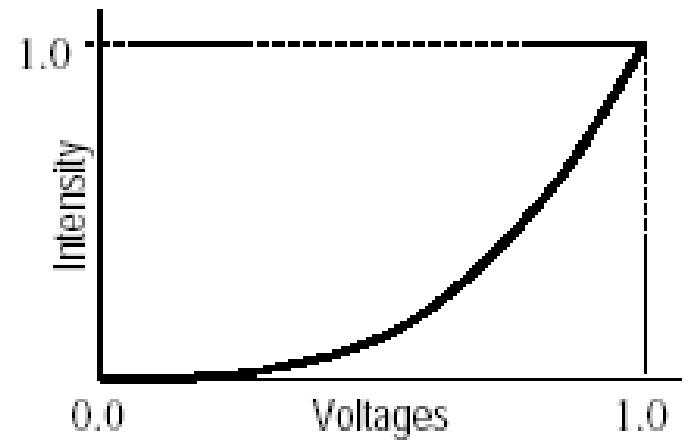
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The Gamma Problem

- device gamma
 - monitor: $\mathbf{I} = A(k_1 D + k_2 V)^\gamma$
 - typical monitor $\gamma = 2.5$
 - LCD: nearly linear
- OS gamma
 - defined by operating system
 - inverse gamma curve $\mathbf{I}^{1/\gamma}$
 - “gamma correction”

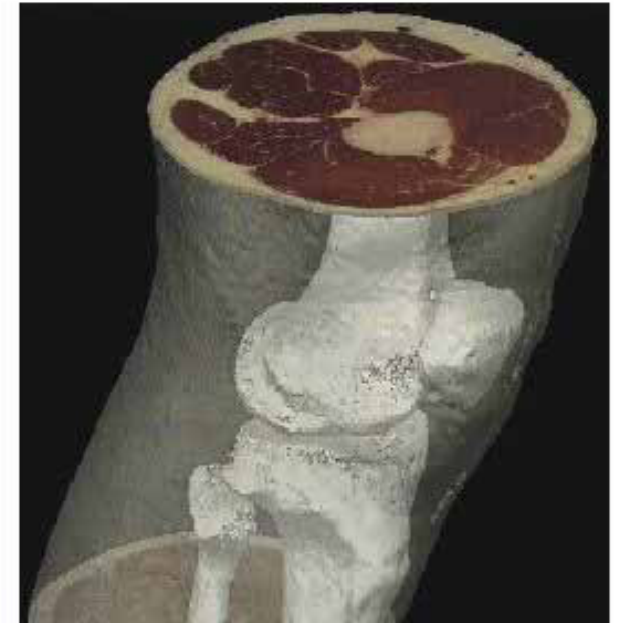
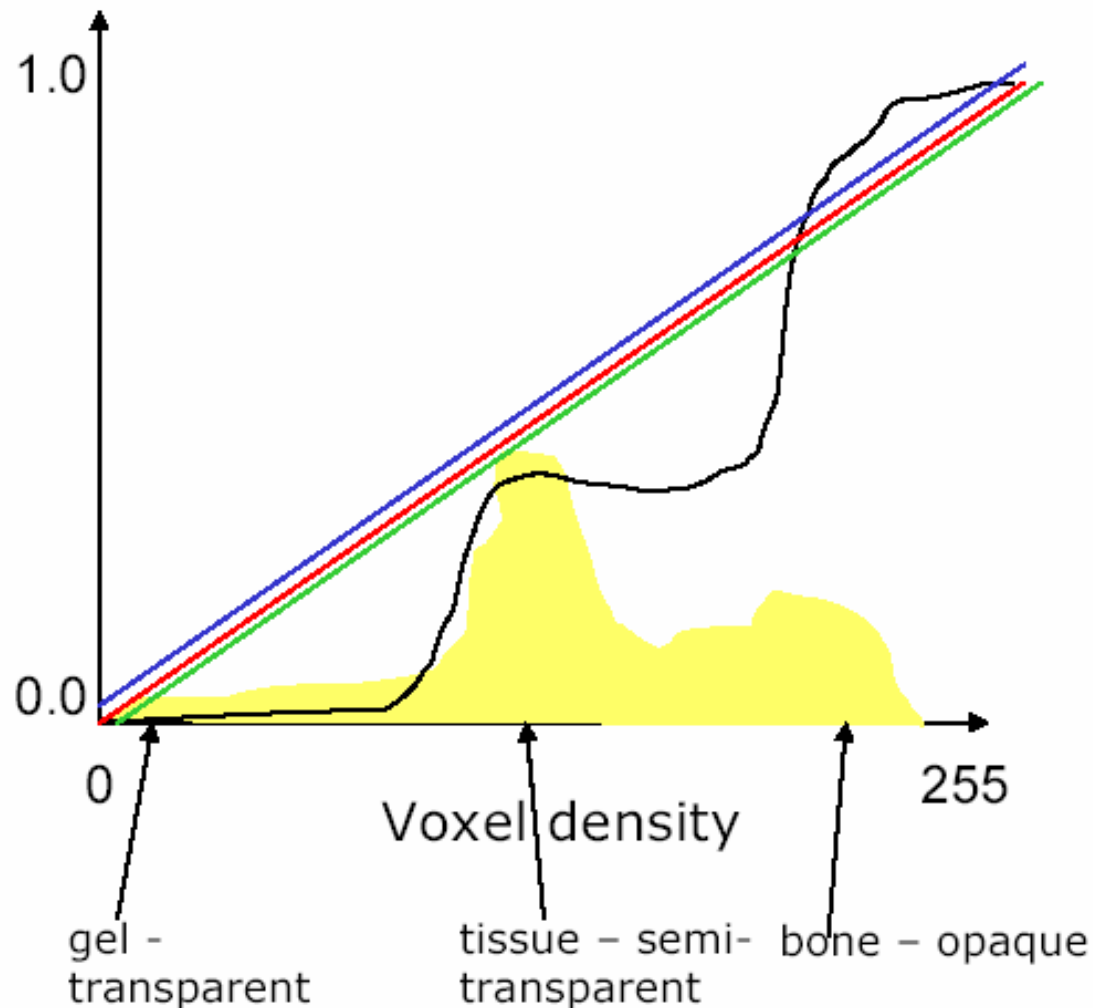




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Scientific Visualization

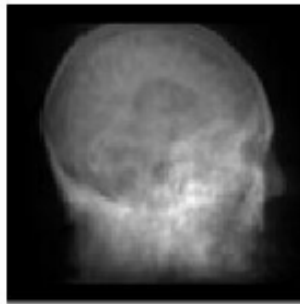
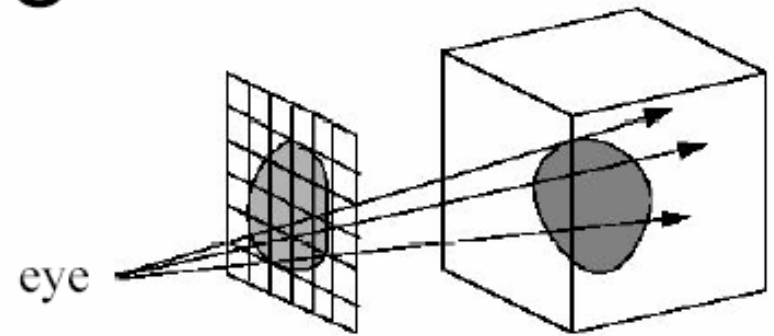
Transfer Functions



- classification of 3D array of voxels

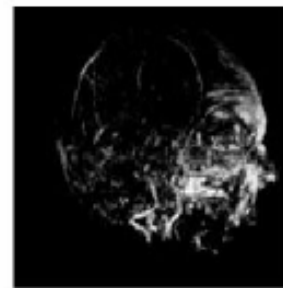
Volume Rendering Modes

- For each pixel in the image, a ray is cast into the volume:
- Four main volume rendering modes exist:



X-Ray:

Rays sum contributions along their path linearly



Maximum Intensity Projection:

A pixel stores the largest intensity values along its ray



Iso-surface:

Rays **composite** contributions only from voxels of a certain intensity defining a surface

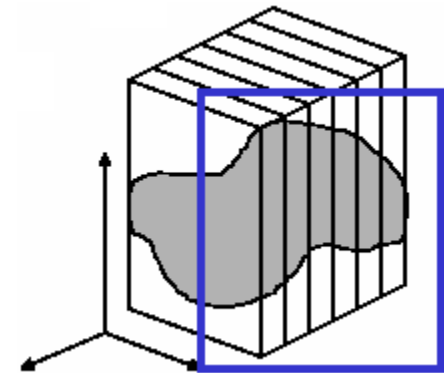
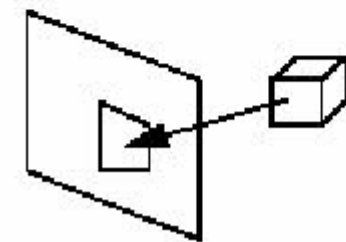
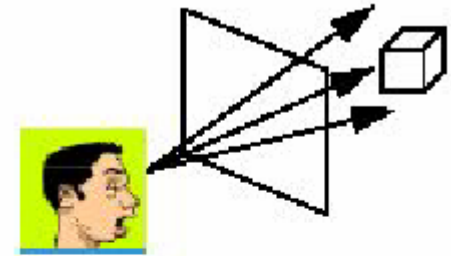


Full-volume:

Rays **composite** contributions along their path linearly

Volume Rendering Algorithms

- ray casting
 - image order, forward viewing
- splatting
 - object order, backward viewing
- texture mapping hardware
 - object order
 - back-to-front compositing





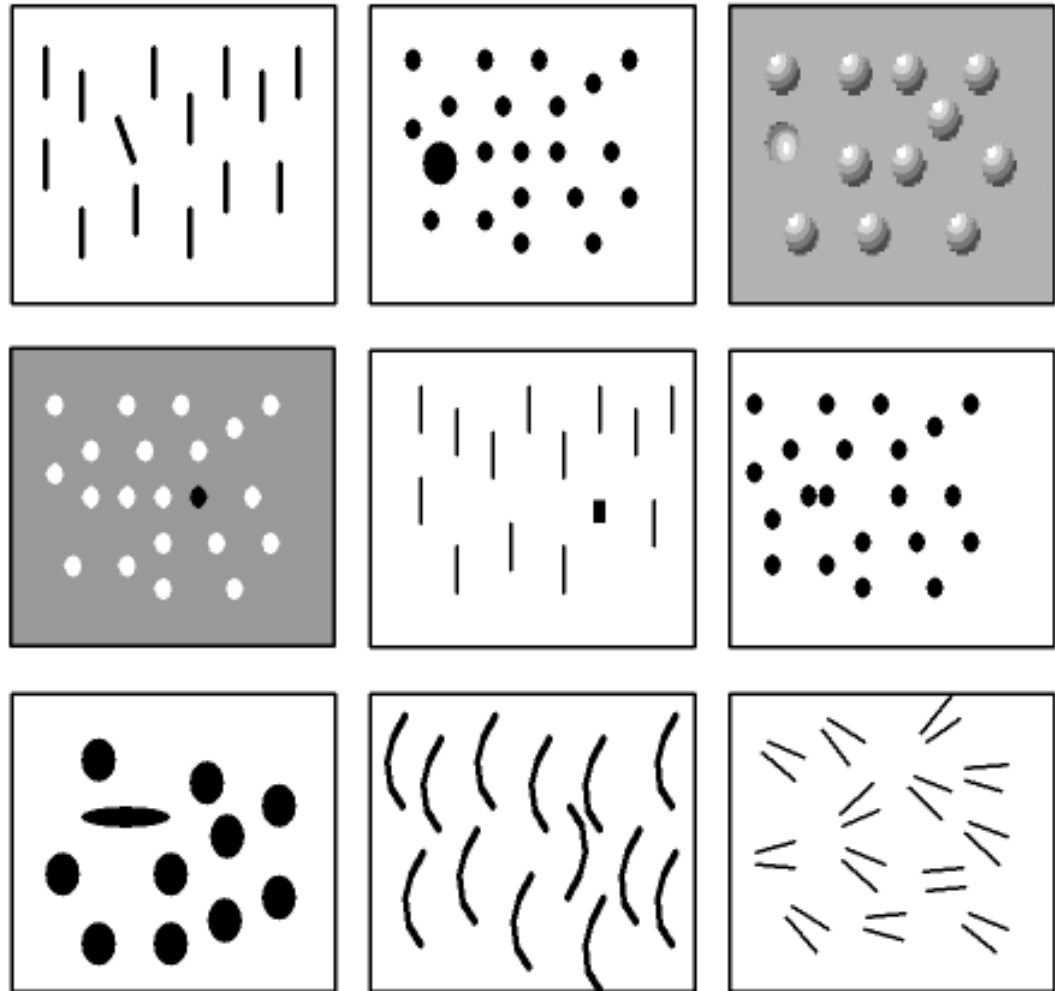
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Information Visualization

Preattentive Visual Dimensions

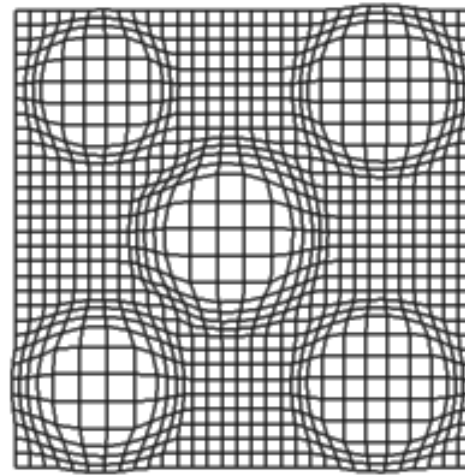
- visual popout independent of distractor count

- hue
- shape
- texture
- length
- width
- size
- orientation
- curvature
- intersection
- intensity
- flicker
- direction of motion
- stereoscopic depth
- lighting direction



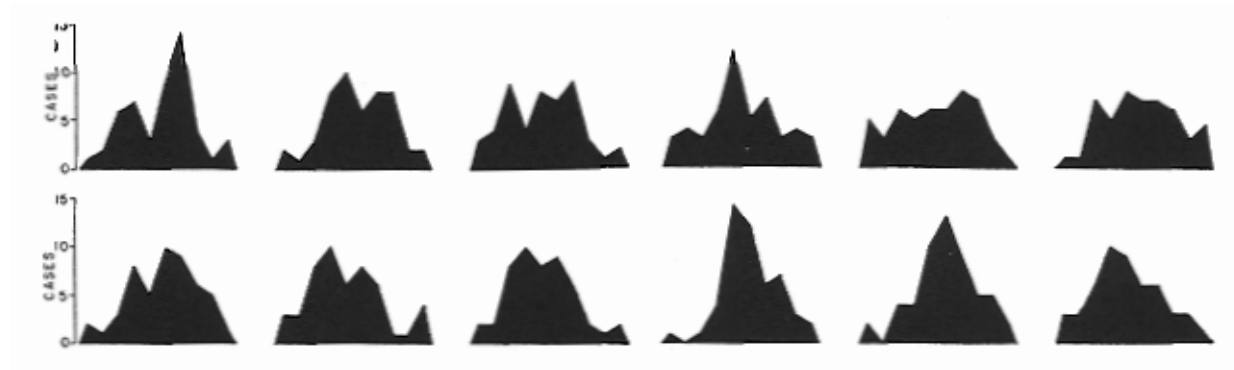
Overview and Detail

- problem: getting lost
 - 1 window: lose track of navigation history
 - 2 windows: see overview and detail both
 - Focus+Context
 - 1 window combines overview and detail
 - carefully chosen distortion



Comparison

- array of small multiples
 - side by side comparison easier than temporal





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Displays and Devices

Display Technologies

- CRT: Cathode Ray Tubes
- LCD: Liquid Crystal Displays
- plasma display panels
- DMD/DLP: micromirror array projectors
- display walls: tiled projector array

Displays and Devices

- mobile display with laser to retina
- stereo glasses/display
- 3D scanners
 - laser stripe + camera
 - laser time-of-flight
 - cameras only, depth from stereo
- Shape Tape
- haptics (Phantom)
- 3D printers

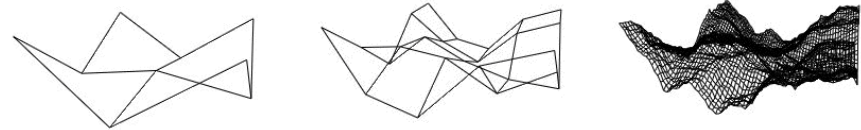


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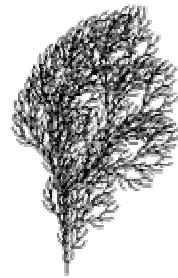
Procedural Approaches

Procedural Approaches

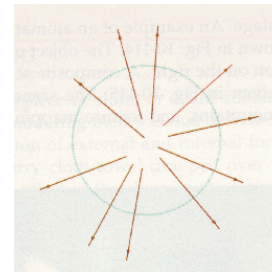
- fractal landscapes



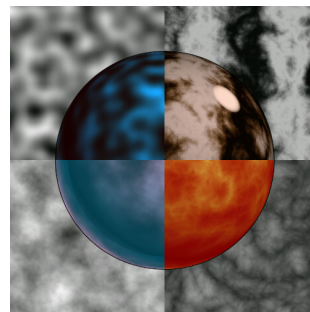
- L-systems



- particle systems



- Perlin noise





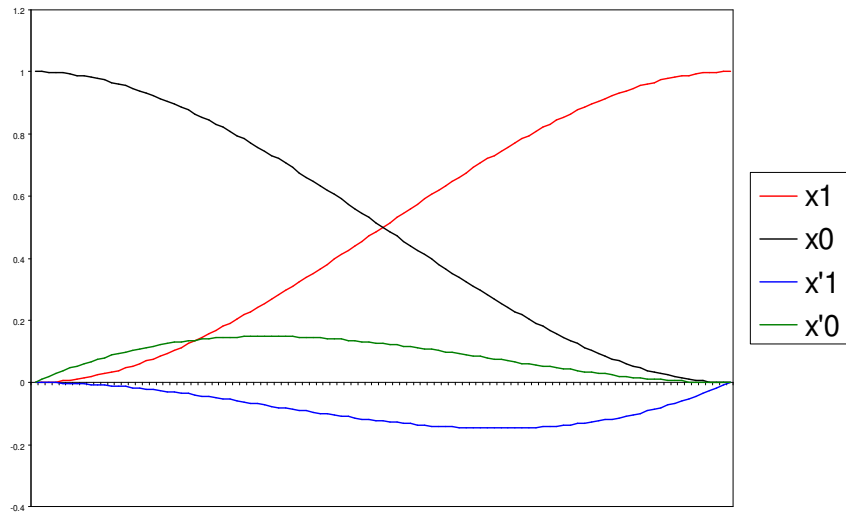
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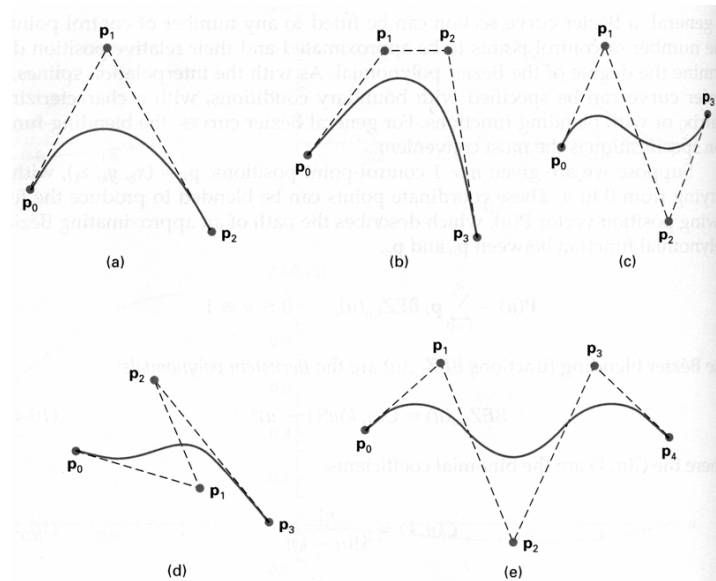
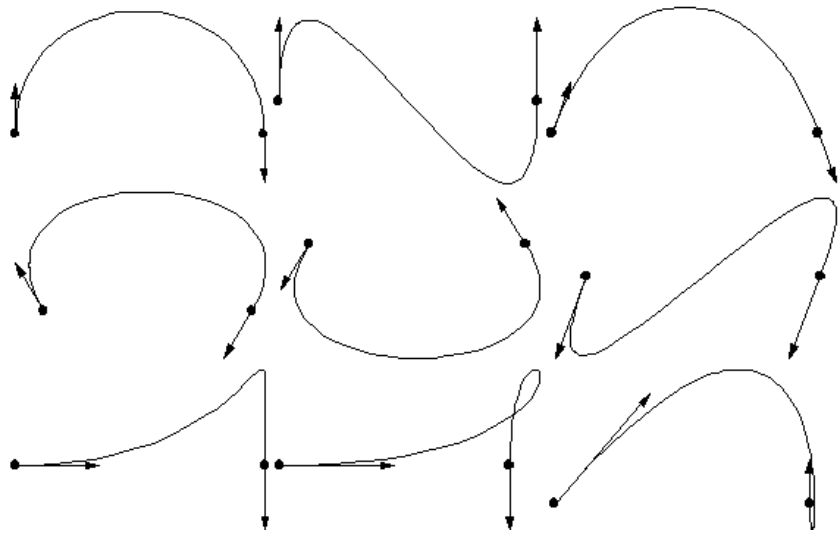
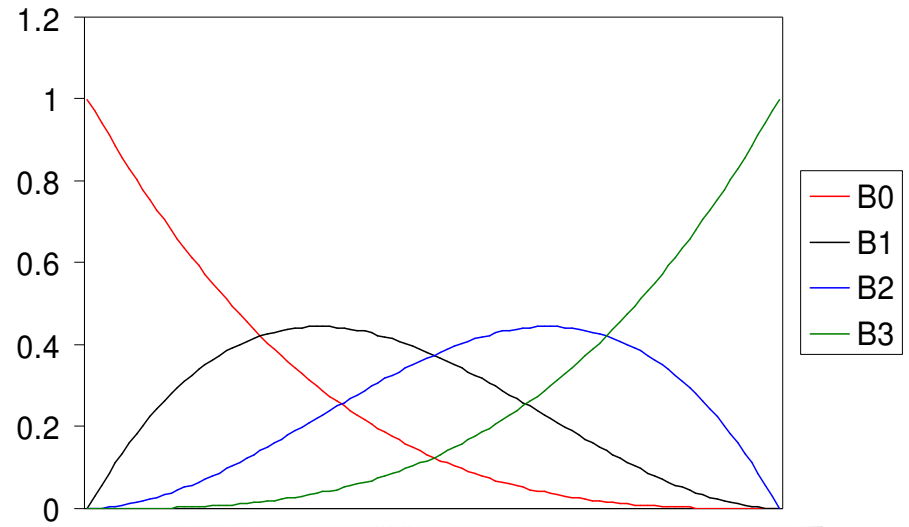
Curves

Comparing Hermite and Bezier

Hermite

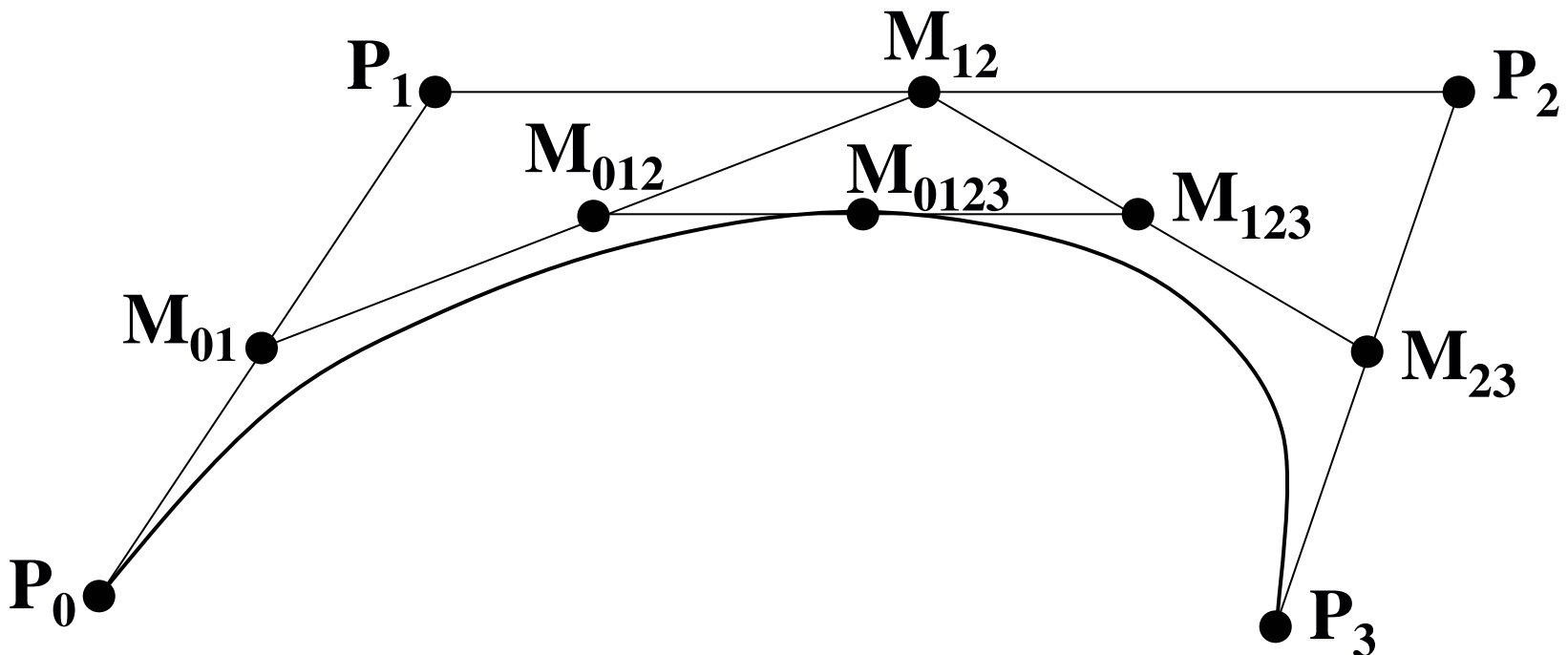


Bezier



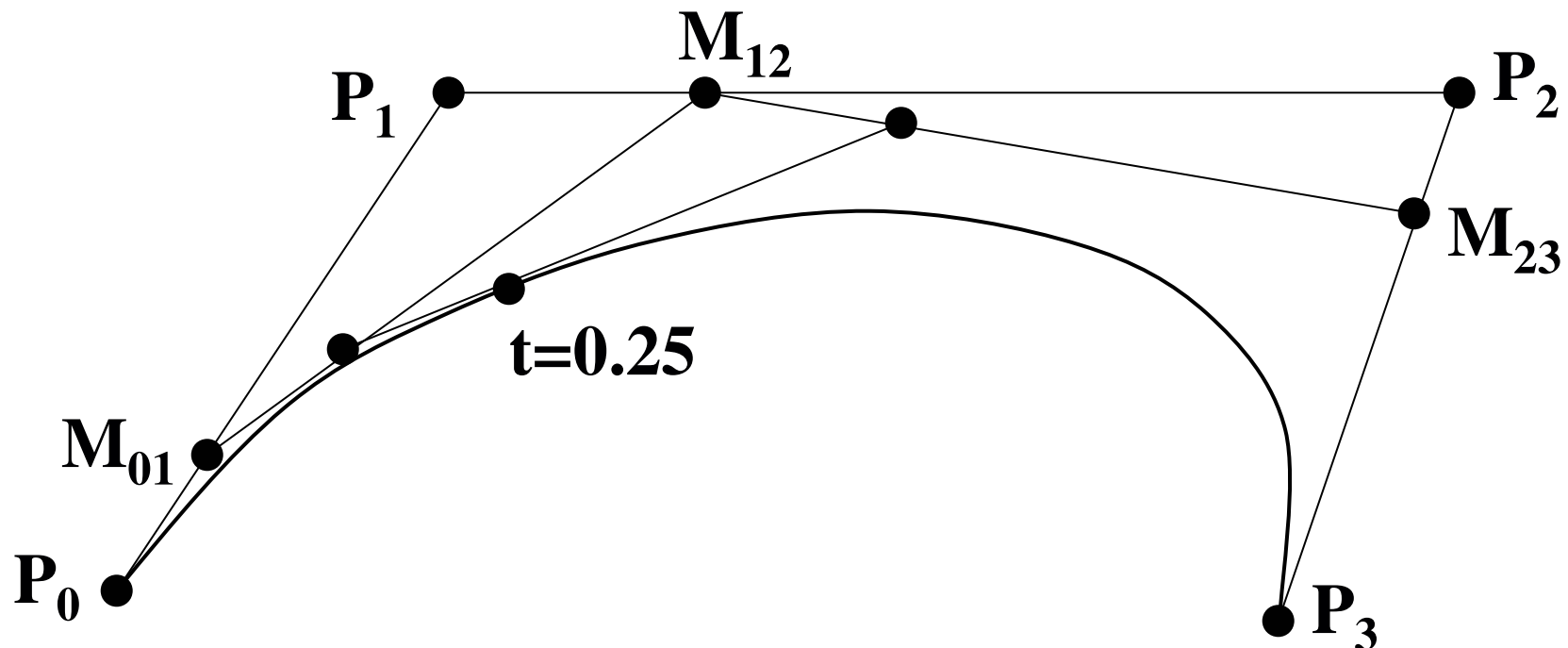
Sub-Dividing Bezier Curves

- step 3: find the midpoint of the line joining M_{012} , M_{123} . call it M_{0123}



de Casteljau's Algorithm

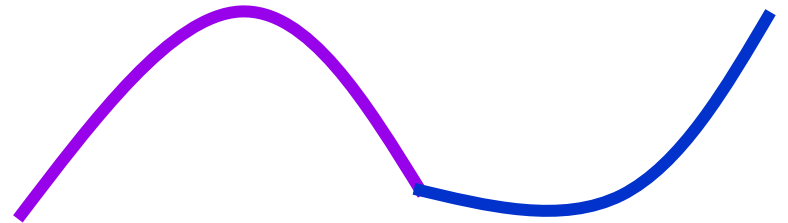
- can find the point on a Bezier curve for any parameter value t with similar algorithm
 - for $t=0.25$, instead of taking midpoints take points 0.25 of the way



demo: www.saltire.com/applets/advanced_geometry/spline/spline.htm

Continuity

- piecewise Bezier: no continuity guarantees



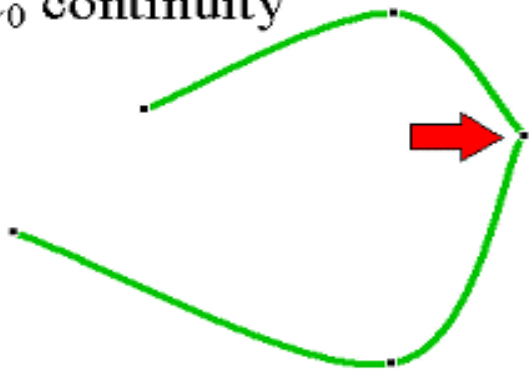
- continuity definitions

- C^0 : share join point

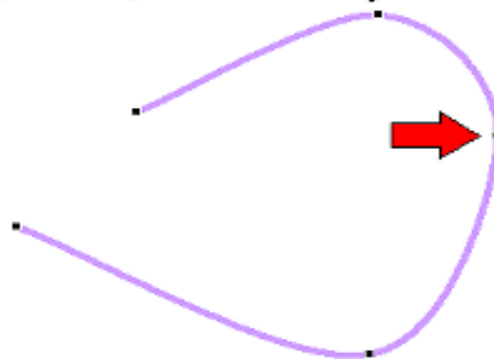
- C^1 : share continuous derivatives

- C^2 : share continuous second derivatives

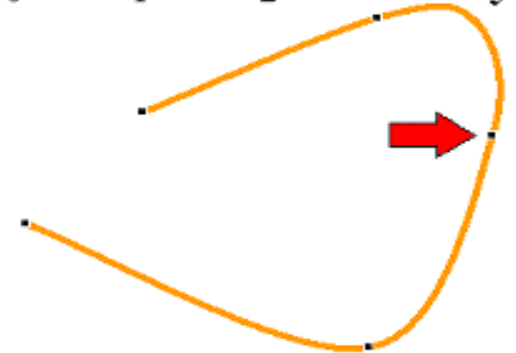
C_0 continuity



C_0 & C_1 continuity



C_0 & C_1 & C_2 continuity



B-Spline

- C_0 , C_1 , and C_2 continuous
- piecewise: locality of control point influence

