



## 2D Arrays, Sorting

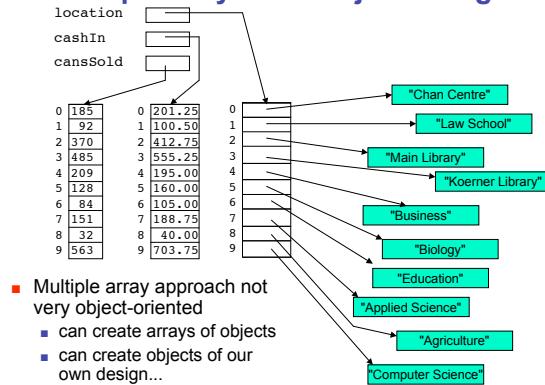
Lecture 16, Tue Mar 7 2006

based on slides by Kurt Eiselt

<http://www.cs.ubc.ca/~tmm/courses/cpsc111-06-spr>

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## Recap: Arrays and Object Design

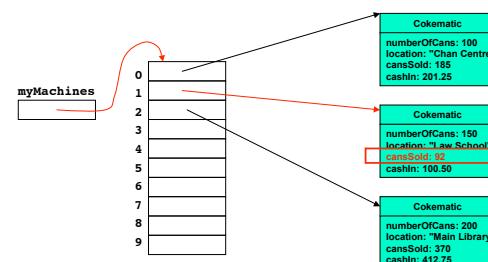


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## Recap: CokeEmpire

- What does this return?

myMachines.getCokematic(1).getcansSold()



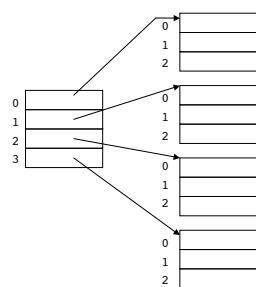
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## Reading

- This week: no new reading

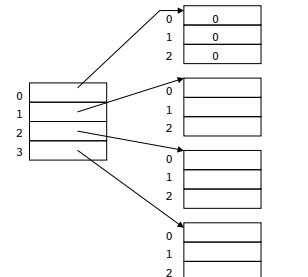
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## Arrays of Arrays



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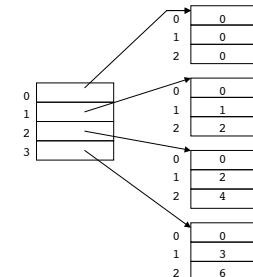
## Arrays of Arrays



- In any given array, all data must be of same type

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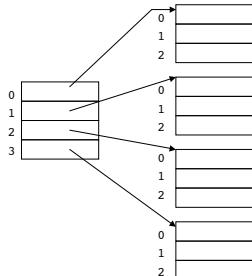
## Arrays of Arrays



- In any given array, all data must be of same type
- All arrays in array of arrays must be of same type

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## Arrays of Arrays



- In any given array, all data must be of same type
- All arrays in array of arrays must be of same type
- So easier to use a two-dimensional array!

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## Two-Dimensional Arrays

columns			
	0	1	2
0	0	0	0
1	0	1	2
2	0	2	4
3	0	3	6

- In Java, 2D array implemented internally as array of arrays
  - but externally syntax of 2D array may seem easier to use

## Two-Dimensional Arrays

columns			
	0	1	2
0	0	0	0
1	0	1	2
2	0	2	4
3	0	3	6

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## Two-Dimensional Arrays

columns			
	0	1	2
0	0	0	0
1	0	1	2
2	0	2	4
3	0	3	6

```
public class ArrayTest5 {
    public static void main(String[] args) {
        int[][] multTable = new int[4][3];
        for (int row = 0; row < multTable.length; row++) {
            for (int col = 0; col < multTable[row].length; col++) {
                multTable[row][col] = row * col;
            }
        }
    }
}
```

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## Two-Dimensional Arrays

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	0	1	2
0	0	0	0
1	0	1	2
2	0	2	4
3	0	3	6

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        int[][] multTable = new int[4][3];
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```

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## Two-Dimensional Arrays

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                multTable[row][col] = row * col;
            }
        }
    }
}
```

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## Two-Dimensional Arrays

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```
public class ArrayTest5 {
    public static void main(String[] args) {
        int[] multTable = new int[4][3];
        for (int row = 0; row < multTable.length; row++) {
            for (int col = 0; col < multTable[row].length; col++) {
                multTable[row][col] = row * col;
            }
        }
        for (int col = 0; col < multTable[row].length; col++) {
            System.out.print(multTable[row][col] + " ");
        }
    }
}
```

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## Two-Dimensional Arrays

columns			
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0	0	0	0
1	0	1	2
2	0	2	4
3	0	3	6

```
public class ArrayTest5 {
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        for (int row = 0; row < multTable.length; row++) {
            for (int col = 0; col < multTable[row].length; col++) {
                multTable[row][col] = row * col;
            }
        }
        for (int row = 0; row < multTable.length; row++) {
            for (int col = 0; col < multTable[row].length; col++) {
                System.out.print(multTable[row][col] + " ");
            }
        }
    }
}
```

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## Two-Dimensional Arrays

columns		0	1	2
rows	0	0	0	0
1	0	1	2	
2	0	2	4	
3	0	3	6	

```
public class ArrayTest5 {
    public static void main(String[] args) {
        int[][] multTable = new int[4][3];

        for (int row = 0; row < multTable.length; row++) {
            for (int col = 0; col < multTable[row].length; col++) {
                multTable[row][col] = row * col;
            }
        }

        for (int row = 0; row < multTable.length; row++) {
            for (int col = 0; col < multTable[row].length; col++) {
                System.out.print(multTable[row][col] + " ");
            }
            System.out.println();
        }
    }
}
```

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## Example: Per-Student Averages

scores				
	0	1	2	3
0	95	82	13	96
1	51	68	63	57
2	73	71	84	78
3	50	50	50	50
4	99	70	32	12

average of row 0 is 71.5  
 average of row 1 is 59.75  
 average of row 2 is 76.5  
 average of row 3 is 50.0  
 average of row 4 is 53.25

### 2D array

- each row is student in course
- values in each row represent student's quiz scores in course

### Print average quiz score for each student

- for each row of scores
  - add up scores
  - divide by number of quizzes in a row
- approach: nested loop

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## Example: Per-Student Averages

```
public class ArrayEx4
{
    public static void main(String[] args)
    {
        double[][] scores = {{95, 82, 13, 96},
                             {51, 68, 63, 57}, {73, 71, 84, 78}, {50, 50, 50, 50},
                             {99, 70, 32, 12}};
        double average;

        // here's where we control looping row by row (student by student)
        for (int row = 0; row < scores.length; row++)
        {
            average = 0;
            // and here's where we control looping through the columns
            // (i.e., quiz scores) within each row
            for (int col = 0; col < scores[row].length; col++)
            {
                average = average + scores[row][col];
            }
            average = average / scores[row].length;
            System.out.println("average of row " + row + " is " + average);
        }
    }
}
```

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## Example: Per-Quiz Averages

scores				
	0	1	2	3
0	95	82	13	96
1	51	68	63	57
2	73	71	84	78
3	50	50	50	50
4	99	70	32	12

average of column 0 is 73.6  
 average of column 1 is 68.2  
 average of column 2 is 48.4  
 average of column 3 is 58.6

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## Example: Per-Quiz Averages

```
public class ArrayEx5
{
    public static void main(String[] args)
    {
        double[][] scores = {{95, 82, 13, 96},
                             {51, 68, 63, 57}, {73, 71, 84, 78}, {50, 50, 50, 50},
                             {99, 70, 32, 12}};
        double average;

        // here's where we control looping column by column (quiz by quiz)
        for (int col = 0; col < scores[0].length; col++)
        {
            average = 0;
            // and here's where we control looping through the rows
            // (i.e., students) within each column
            for (int row = 0; row < scores.length; row++)
            {
                average = average + scores[row][col];
            }
            average = average / scores.length;
            System.out.println("average of column " + col + " is " + average);
        }
    }
}
```

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## Sorting

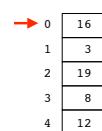
- Computers are essential for keeping track and finding large quantities of data
- Finding data when necessary is much easier when data is sorted in some way
  - computer people think a lot about how to sort things:
    - finding medical records
    - banking information
    - income tax returns
    - driver's license information...
    - even names in a phone book...
- all depend on the information being sorted

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## Selection sort

0	16
1	3
2	19
3	8
4	12

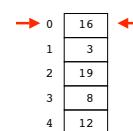
- Let's say want to sort array values in increasing order
  - one way to approach problem is to use algorithm called **selection sort**



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## Selection sort

- Let's say want to sort array values in increasing order
  - one way to approach problem is to use algorithm called **selection sort**
- Start by setting pointer to first element in array
  - this is where smallest value in array will be placed



The smallest value so far is 16  
 Its index is 0

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## Selection sort

- Let's say want to sort array values in increasing order
  - one way to approach problem is to use algorithm called **selection sort**
- Start by setting pointer to first element in array
  - this is where smallest value in array will be placed
- Then look at every value in this unsorted array
  - find minimum value

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## Selection sort

→ 0	16
1	3
2	19
3	8
4	12

The smallest value so far is 3

Its index is 1

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## Selection sort

→ 0	16
1	3
2	19
3	8
4	12

The smallest value so far is 3

Its index is 1

29

## Selection sort

→ 0	16
1	3
2	19
3	8
4	12

The smallest value so far is 3

Its index is 1

30

## Selection sort

→ 0	16
1	3
2	19
3	8
4	12

The smallest value so far is 3

Its index is 1

31

## Selection sort

→ 0	16
1	3
2	19
3	8
4	12

The smallest value so far is 3

Its index is 1

32

## Selection sort

→ 0	3
1	16
2	19
3	8
4	12

The smallest value so far is 3

Its index is 1

33

## Selection sort

0	3
1	16
2	19
3	8
4	12

- At this point we know
  - smallest number in array is in first element (index 0)
  - first element is sorted
  - rest of array remains unsorted
- Now select second element of array to be location which will hold next smallest value

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→ 0	3
1	16
2	19
3	8
4	12

The smallest value so far is 16

Its index is 1

35

## Selection sort

- At this point we know
  - smallest number in array is in first element (index 0)
  - first element is sorted
  - rest of array remains unsorted
- Now select second element of array to be location which will hold next smallest value
- In other words, do everything again to unsorted part of array
  - in this case, all but first element

0	3
1	16
2	19
3	8
4	12

The smallest value so far is 16

Its index is 1

36

## Selection sort

- At this point we know
  - smallest number in array is in first element (index 0)
  - first element is sorted
  - rest of array remains unsorted
- Now select second element of array to be location which will hold next smallest value
- In other words, do everything again to unsorted part of array
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  - first element is sorted
  - rest of array remains unsorted
- Now select second element of array to be location which will hold next smallest value
  - In other words, do everything again to unsorted part of array
    - in this case, all but first element

0	3
1	16
2	19
3	8
4	12

The smallest value so far is 8

Its index is 3

37

## Selection sort

- At this point we know
  - smallest number in array is in first element (index 0)
  - first element is sorted
  - rest of array remains unsorted
- Now select second element of array to be location which will hold next smallest value
  - In other words, do everything again to unsorted part of array
    - in this case, all but first element

0	3
1	16
2	19
3	8
4	12

The smallest value so far is 8

Its index is 3

38

## Selection sort

- At this point we know
  - smallest number in array is in first element (index 0)
  - first element is sorted
  - rest of array remains unsorted
- Now select second element of array to be location which will hold next smallest value
  - In other words, do everything again to unsorted part of array
    - in this case, all but first element
- Now swap minimum value with selected array value
  - in this case, second element

0	3
1	16
2	19
3	8
4	12

The smallest value so far is 8

Its index is 3

39

## Selection sort

- At this point we know
  - smallest number in array is in first element (index 0)
  - first element is sorted
  - rest of array remains unsorted
- Now select second element of array to be location which will hold next smallest value
  - In other words, do everything again to unsorted part of array
    - in this case, all but first element
- Now swap minimum value with selected array value
  - in this case, second element

0	3
1	8
2	19
3	16
4	12

The smallest value so far is 8

Its index is 3

40

## Selection sort

- Now first two elements of array are sorted
- Select third element of array to be location of next smallest value
  - Search unsorted portion of array for that value, just like before

0	3
1	8
2	19
3	16
4	12

The smallest value so far is 19

Its index is 2

41

## Selection sort

- Now first two elements of array are sorted
- Select third element of array to be location of next smallest value
  - Search unsorted portion of array for that value, just like before

0	3
1	8
2	19
3	16
4	12

The smallest value so far is 16

Its index is 3

42

## Selection sort

- Now first two elements of array are sorted
- Select third element of array to be location of next smallest value
  - Search unsorted portion of array for that value, just like before

0	3
1	8
2	19
3	16
4	12

The smallest value so far is 12

Its index is 4

43

## Selection sort

- Now first two elements of array are sorted
- Select third element of array to be location of next smallest value
  - Search unsorted portion of array for that value, just like before
- Again, swap values

0	3
1	8
2	19
3	16
4	12

The smallest value so far is 12

Its index is 4

44

45

## Selection sort

- Now first two elements of array are sorted
- Select third element of array to be location of next smallest value
  - Search unsorted portion of array for that value, just like before
- Again, swap values

0	3
1	8
2	12
3	16
4	19

0	3
1	8
2	12
3	16
4	19

## Selection sort

- Now first two elements of array are sorted
- Select third element of array to be location of next smallest value
  - Search unsorted portion of array for that value, just like before
- Again, swap values
  - then do whole thing again

The smallest value so far is 16

Its index is 3

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0	3
1	8
2	12
3	16
4	19

The smallest value so far is 16

Its index is 3

47

## Selection sort

- Now first two elements of array are sorted
- Select third element of array to be location of next smallest value
  - Search unsorted portion of array for that value, just like before
- Again, swap values
  - then do whole thing again

The smallest value so far is 16

Its index is 3

48

## Selection sort

- Now first two elements of array are sorted
- Select third element of array to be location of next smallest value
  - Search unsorted portion of array for that value, just like before
- Again, swap values
  - then do whole thing again
- Swap again
  - not actually necessary in this case
  - but we follow algorithm

0	3
1	8
2	12
3	16
4	19

The smallest value so far is 16

Its index is 3

49

0	3
1	8
2	12
3	16
4	19

## Selection sort

- Are we done?
  - could select last element of array
    - (index 4)
  - but all of array except for last element is already sorted
  - so last element is largest value in array
    - and that's the right place
- Yes, array is sorted, and we're done
  - no need to select last element

0	16
1	3
2	19
3	8
4	12

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## Selection sort

- Showed arrows moving down array
  - red arrow on left represents one array index variable
  - yellow arrow on right represents different one
- Consider variables being controlled by loop
  - red arrow shows outer loop
  - yellow arrow shows inner loop inside outer loop
- Nested loop structure again

## Selection sort

```
// selection sort
public class SortTest1
{
    public static void main(String[] args)
    {
        int[] numbers = {16,3,19,8,12};
        int min, temp;
        //select location of next sorted value
        for (int i = 0; i < numbers.length-1; i++)
        {
            min = i;
            //find the smallest value in the remainder of
            //the array to be sorted
            for (int j = i+1; j < numbers.length; j++)
            {
                if (numbers[j] < numbers[min])
                {
                    min = j;
                }
            }
            //swap two values in the array
            temp = numbers[i];
            numbers[i] = numbers[min];
            numbers[min] = temp;
        }

        System.out.println("Printing sorted result");
        for (int i = 0; i < numbers.length; i++)
        {
            System.out.println(numbers[i]);
        }
    }
}
```

i	0	16	j
1	3		
2	19		
3	8		
4	12		

## Selection sort

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i	0	16	j
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3	8		
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## Selection sort

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        int[] numbers = {16,3,19,8,12};
        int min, temp;
        //select location of next sorted value
        for [int i = 0] i < numbers.length-1; i++
        {
            min = i;
            //find the smallest value in the remainder of
            //the array to be sorted
            for (int j = i+1; j < numbers.length; j++)
            {
                if (numbers[j] < numbers[min])
                {
                    min = j;
                }
            }
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```

i	0	16	j
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2	19		
3	8		
4	12		

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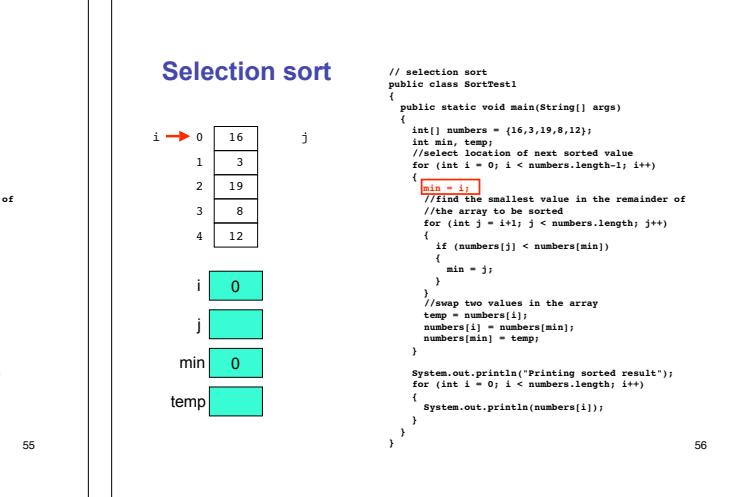
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## Selection sort

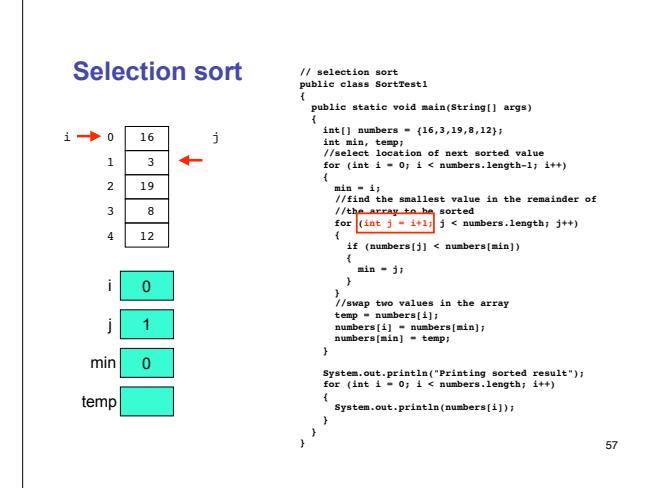
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        for (int i = 0; i < numbers.length; i++)
        {
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        }
    }
}
```



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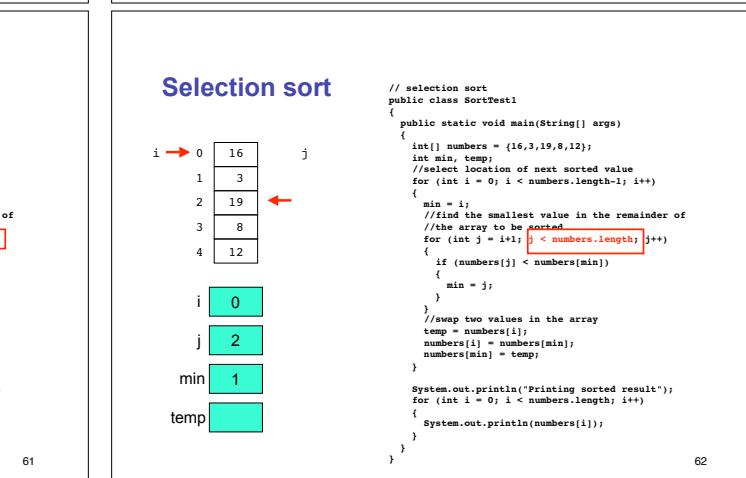
## Selection sort

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                if (numbers[j] < numbers[min])
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                    min = j;
                }
            }
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    }
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```

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## Selection sort

```
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            //find the smallest value in the remainder of
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            for (int j = i+1; j < numbers.length; j++)
            {
                if (numbers[j] < numbers[min])
                {
                    min = j;
                }
            }
            //swap two values in the array
            temp = numbers[i];
            numbers[i] = numbers[min];
            numbers[min] = temp;
        }
        System.out.println("Printing sorted result");
        for (int i = 0; i < numbers.length; i++)
        {
            System.out.println(numbers[i]);
        }
    }
}
```



61

## Selection sort

```
// selection sort
public class SortTest1
{
    public static void main(String[] args)
    {
        int[] numbers = {16,3,19,8,12};
        int min, temp;
        //select location of next sorted value
        for (int i = 0; i < numbers.length-1; i++)
        {
            min = i;
            //find the smallest value in the remainder of
            //the array to be sorted
            for (int j = i+1; j < numbers.length; j++)
            {
                if (numbers[j] < numbers[min])
                {
                    min = j;
                }
            }
            //swap two values in the array
            temp = numbers[i];
            numbers[i] = numbers[min];
            numbers[min] = temp;
        }
        System.out.println("Printing sorted result");
        for (int i = 0; i < numbers.length; i++)
        {
            System.out.println(numbers[i]);
        }
    }
}
```

63

## Selection sort

```

int[] numbers = {16,3,19,8,12};
int min, temp;
//select location of next sorted value
for (int i = 0; i < numbers.length-1; i++)
{
    min = i;
    //find the smallest value in the remainder of the array
    //the array to be sorted
    for (int j = i+1; j < numbers.length; j++)
    {
        if (numbers[j] < numbers[min])
        {
            min = j;
        }
    }
    //swap two values in the array
    temp = numbers[i];
    numbers[i] = numbers[min];
    numbers[min] = temp;
}
System.out.println("Printing sorted result");
for (int i = 0; i < numbers.length; i++)
{
    System.out.println(numbers[i]);
}

```

6

## Selection sort

i → 0    16    j

1    3

2    19

3    8

4    12 ←

i    0

j    4

min    1

temp

```

int[] numbers = {16,3,19,8,12};
int min, temp;
//select location of next sorted value
for (int i = 0; i < numbers.length-1; i++)
{
    min = i;
    //find the smallest value in the remainder of the array
    //the array to be sorted
    for (int j = i+1; j < numbers.length; j++)
    {
        if (numbers[j] < numbers[min])
        {
            min = j;
        }
    }
    //swap two values in the array
    temp = numbers[i];
    numbers[i] = numbers[min];
    numbers[min] = temp;
}
System.out.println("Printing sorted result");
for (int i = 0; i < numbers.length; i++)
{
    System.out.println(numbers[i]);
}

```

6

## Selection sort

```

i -> 0   [ 16 ]   j
      |       |
      1       3
      |       |
      2       19
      |       |
      3       8
      |       |
      4       12

i [ 0 ]   ←
j [ 5 ]
min [ 1 ]
temp [ ]   ←

int[] numbers = {16, 3, 19, 8, 2, 1};
//selected location of next sorted value
for (int i = 0; i < numbers.length-1; i++)
{
    min = i;
    //find the smallest value in the remainder of the array to be sorted
    for (int j = i+1; j < numbers.length; j++)
    {
        if (numbers[j] < numbers[min])
        {
            min = j;
        }
    }
    //swap two values in the array
    temp = numbers[i];
    numbers[i] = numbers[min];
    numbers[min] = temp;
}

System.out.println("Printing sorted result");
for (int i = 0; i < numbers.length; i++)
{
    System.out.println(numbers[i]);
}

```

7

## Selection sort

```

int[] numbers = {16, 3, 19, 8, 12};
int min, temp;
//select location of next sorted value
for (int i = 0; i < numbers.length-1; i++)
{
    min = i;
    //find the smallest value in the remainder
    //the array to be sorted
    for (int j = i+1; j < numbers.length; j++)
    {
        if (numbers[j] < numbers[min])
        {
            min = j;
        }
    }
    //swap two values in the array
    temp = numbers[i];
    numbers[i] = numbers[min];
    numbers[min] = temp;
}
System.out.println("Printing sorted result");
for (int i = 0; i < numbers.length; i++)
{
    System.out.println(numbers[i]);
}

```

i → 0      j  
 1      3  
 2      19  
 3      8 ←  
 4      12

i      0  
 j      3  
 min      1  
 temp

6

## Selection sort

```

i → 0      16    j
          3
          19
          8
          12

i   0
j   4
min 1
temp

int[] numbers = {16,3,19,8,12};
int min, temp;
//select location of next sorted value
for (int i = 0; i < numbers.length-1; i++)
{
    min = i;
    //find the smallest value in the remainder
    //the array to be sorted
    for (int j = i+1; j < numbers.length; j++)
    {
        if (numbers[j] < numbers[min])
        {
            min = j;
        }
    }
    //swap two values in the array
    temp = numbers[i];
    numbers[i] = numbers[min];
    numbers[min] = temp;
}
System.out.println("Printing sorted result");
for (int i = 0; i < numbers.length; i++)
{
    System.out.println(numbers[i]);
}

```

6

## Selection sort

```

int[] numbers = {16, 3, 19, 8, 12};
int min, temp;
//select element of next sorted value
for (int i = 0; i < numbers.length - 1; i++)
{
    min = i;
    //find the smallest value in the remainder
    //of the array to be sorted
    for (int j = i + 1; j < numbers.length; j++)
    {
        if (numbers[j] < numbers[min])
        {
            min = j;
        }
    }
    //swap two values in the array
    temp = numbers[i];
    numbers[i] = numbers[min];
    numbers[min] = temp;
}
System.out.println("Printing sorted result");
for (int i = 0; i < numbers.length; i++)
{
    System.out.println(numbers[i]);
}

```

7

## Selection sort

i → 0    16  
1    3  
2    19  
3    8 ←  
4    12

i    0

j    3

min    1

temp    12

```

int[] numbers = {16, 3, 19, 8, 12};
int min, temp;
//select location of next sorted value
for (int i = 0; i < numbers.length-1; i++)
{
    min = i;
    //find the smallest value in the remainder of
    //the array to be sorted
    for (int j = i+1; j < numbers.length; j++)
    {
        if (numbers[j] < numbers[min])
        {
            min = j;
        }
    }
    //swap two values in the array
    temp = numbers[i];
    numbers[i] = numbers[min];
    numbers[min] = temp;
}

System.out.println("Printing sorted result");
for (int i = 0; i < numbers.length; i++)
{
    System.out.print(numbers[i]);
}
}

```

}

## Selection sort

i → 0    16  
1    3  
2    19  
3    8  
4    12 ←

i    0  
j    4  
min    1  
temp

```

int[] numbers = {16, 3, 19, 8, 12};
int min, temp;
//select location of next sorted value
for (int i = 0; i < numbers.length-1; i++)
{
    min = i;
    //find the smallest value in the remainder of
    //the array to be sorted
    for (int j = i+1; j < numbers.length; j++)
    {
        if (numbers[j] < numbers[min])
        {
            min = j;
        }
    }
    //swap two values in the array
    temp = numbers[i];
    numbers[i] = numbers[min];
    numbers[min] = temp;
}
System.out.println("Printing sorted result");
for (int i = 0; i < numbers.length; i++)
{
    System.out.println(numbers[i]);
}
}

```

## Selection sort

```

i → 0 [16] j
  3
  19
  8
  12

i [0]
j [5]
min [1]
temp [16]

int[] numbers = {16,3,19,12,8};
int min, temp;
//selected location of next sorted value
for (int i = 0; i < numbers.length-1; i++)
{
    min = i;
    //find the smallest value in the remainder of
    //the array to be sorted
    for (int j = i+1; j < numbers.length; j++)
    {
        if (numbers[j] < numbers[min])
        {
            min = j;
        }
    }
    //swap two values in the array
    temp = numbers[i];
    numbers[i] = numbers[min];
    numbers[min] = temp;
}

System.out.println("Printing sorted result");
for (int i = 0; i < numbers.length; i++)
{
    System.out.println(numbers[i]);
}
}

```

## Selection sort

```

int[] numbers = {16, 3, 19, 8, 12};
int min, temp;
//selected location of next sorted value
for (int i = 0; i < numbers.length-1; i++)
{
    min = i;
    //find the smallest value in the remainder of
    //the array to be sorted
    for (int j = i+1; j < numbers.length; j++)
    {
        if (numbers[j] < numbers[min])
        {
            min = j;
        }
    }
    //swap two values in the array
    temp = numbers[i];
    numbers[i] = numbers[min];
    numbers[min] = temp;
}

System.out.println("Printing sorted result");
for (int i = 0; i < numbers.length; i++)
{
    System.out.println(numbers[i]);
}

```

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## Selection sort

The diagram illustrates the state of variables and the array during the execution of a selection sort algorithm. The array `numbers` is represented as a stack of cards with values: 16, 3, 19, 8, 12. Variable `i` is highlighted in green and points to index 1. Variable `j` is also highlighted in green and points to index 1. Variable `min` is highlighted in green and points to index 1. Variable `temp` is highlighted in green and points to index 1.

```

    int[] numbers = {16,3,19,8,12};
    int min, temp;
    //selected location of next sorted value
    for (int i = 0; i < numbers.length-1; i++)
    {
        min = i;
        //find the smallest value in the remainder of
        //the array to be sorted
        for (int j = i+1; j < numbers.length; j++)
        {
            if (numbers[j] < numbers[min])
            {
                min = j;
            }
        }
        //swap two values in the array
        temp = numbers[i];
        numbers[i] = numbers[min];
        numbers[min] = temp;
    }
    System.out.println("Printing sorted result");
    for (int i = 0; i < numbers.length; i++)
    {
        System.out.println(numbers[i]);
    }
}
  
```

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## Selection sort

```

    int[] numbers = {16, 3, 19, 8, 12};
    int min, temp;
    //select location of next sorted value
    for (int i = 0; i < numbers.length-1; i++)
    {
        min = i;
        //find the smallest value in the remainder
        //of the array to be sorted
        for (int j = i+1; j < numbers.length; j++)
        {
            if (numbers[j] < numbers[min])
            {
                min = j;
            }
        }
        //swap two values in the array
        temp = numbers[i];
        numbers[i] = numbers[min];
        numbers[min] = temp;
    }
    System.out.println("Printing sorted result");
    for (int i = 0; i < numbers.length; i++)
    {
        System.out.print(numbers[i]);
    }
}

```

7

## Selection sort

The diagram illustrates the state of variables during the execution of a Java program. The left side shows the current values of variables:

- i**: 0 (highlighted in red)
- j**: 16
- 2**: 19
- 3**: 8
- 4**: 12
- i**: 1 (highlighted in red)
- j**: 5 (highlighted in green)
- min**: 1 (highlighted in green)
- temp**: 16 (highlighted in green)

An arrow points from the value 16 in the **j** row to the **numbers[1]** line in the code. Another arrow points from the value 5 in the **j** row to the **numbers[min]** line in the code.

```

    {
        int[] numbers = {16,3,19,8,12};
        int min, temp;
        //select location of next sorted value
        for (int i = 0; i < numbers.length-1; i++) {
            min = i;
            //find the smallest value in the remainder of
            //the array to be sorted
            for (int j = i+1; j < numbers.length; j++) {
                if (numbers[j] < numbers[min])
                    min = j;
            }
            //swap two values in the array
            temp = numbers[i];
            numbers[i] = numbers[min];
            numbers[min] = temp;
        }
        System.out.println("Printing sorted result");
        for (int i = 0; i < numbers.length; i++)
        {
            System.out.println(numbers[i]);
        }
    }
}
  
```

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## Selection sort

The diagram illustrates the execution state of a Java program for the selection sort algorithm. The stack trace shows the current method call:

```
public static void main(String[] args)
```

The local variables are:

i	0	3	j
	1	16	
	2	19	←
	3	8	
	4	12	

The array numbers is shown as:

1
2
min
temp

The current line of code being executed is:

```
for (int j = i+1; j < numbers.length; j++)
```

A red box highlights this line of code.

79

## Selection sort

public static void main(String[] args){  
 {  
 int[] numbers = {16,3,19,8,12};  
 int min, temp;  
 //select location of next sorted value  
 for (int i = 0; i < numbers.length-1; i++)  
 {  
 min = i;  
 //find the smallest value in the remainder  
 //the array to be sorted  
 for (int j = i+1; j < numbers.length; j++)  
 {  
 if (numbers[j] < numbers[min])  
 {  
 min = j;  
 }  
 }  
 //swap two values in the array  
 temp = numbers[i];  
 numbers[i] = numbers[min];  
 numbers[min] = temp;  
 }  
 System.out.println("Printing sorted result");  
 for (int i = 0; i < numbers.length; i++)  
 {  
 System.out.print(numbers[i]);  
 }  
 }  
}

8

## Selection sort

```

public static void main(String[] args)
{
    int[] numbers = {16,3,19,8,12};
    int min, temp;
    //select location of next sorted value
    for (int i = 0; i < numbers.length-1; i++)
    {
        min = i;
        //find the smallest value in the remainder of
        //the array to be sorted
        for (int j = i+1; j < numbers.length; j++)
        {
            if (numbers[j] < numbers[min])
            {
                min = j;
            }
        }
        //swap two values in the array
        temp = numbers[i];
        numbers[i] = numbers[min];
        numbers[min] = temp;
    }

    System.out.println("Printing sorted result");
    for (int i = 0; i < numbers.length; i++)
    {
        System.out.println(numbers[i]);
    }
}

```

81





## Selection sort

	0	3
	1	8
→	2	19
	3	16
	4	12

i	2
j	4
min	3
temp	16

```
// selection sort
public class SortTest1
{
    public static void main(String[] args)
    {
        int[] numbers = {16,3,19,8,12};
        int min, temp;
        //select location of next sorted value
        for (int i = 0; i < numbers.length-1; i++)
        {
            min = i;
            //find the smallest value in the remainder of
            //the array to be sorted
            for (int j = i+1; j < numbers.length; j++)
            {
                if (numbers[j] < numbers[min])
                    min = j;
            }
        }
        //swap two values in the array
        temp = numbers[i];
        numbers[i] = numbers[min];
        numbers[min] = temp;
    }

    System.out.println("Printing sorted result");
    for (int i = 0; i < numbers.length; i++)
    {
        System.out.println(numbers[i]);
    }
}
```

}

## Selection sort

```

    numbers = [16,3,19,8,12];
    min, temp;
    select location of next sorted value
    (int i = 0; i < numbers.length-1; i++)
    {
        i++;
        find the smallest value in the remainder
        the array to be sorted
        (int j = i+1; j < numbers.length; j++)
        {
            if (numbers[j] < numbers[min])
            {
                min = j;
            }
        }
        swap two values in the array
        temp = numbers[i];
        numbers[i] = numbers[min];
        numbers[min] = temp;
    }

    System.out.println("Printing sorted result");
    for (int i = 0; i < numbers.length; i++)
    {
        System.out.println(numbers[i]);
    }
}

```

10

## Selection sort

```

i   0 [3]   j
    1 [8]
    2 [19] →
    3 [16]
    4 [12] ←

i [2]
j [4]

min [3]
temp [16]

int[] numbers = {16,3,19,8,12};
int min, temp;
//select location of next sorted value
for (int i = 0; i < numbers.length-1; i++)
{
    min = i;
    //find the smallest value in the remainder of
    //the array to be sorted
    for (int j = i+1; j < numbers.length; j++)
    {
        if (numbers[j] < numbers[min])
        {
            min = j;
        }
    }
    //swap two values in the array
    temp = numbers[i];
    numbers[i] = numbers[min];
    numbers[min] = temp;
}

System.out.println("Printing sorted result");
for (int i = 0; i < numbers.length; i++)
{
    System.out.println(numbers[i]);
}
}

```

## Selection sort

	0	3
	1	8
→	2	19
	3	16
	4	12

i	2
j	4
min	4
temp	16

```

// selection sort
public class SortTest1
{
    public static void main(String[] args)
    {
        int[] numbers = {16,3,19,8,12};
        int min, temp;
        //select location of next sorted value
        for (int i = 0; i < numbers.length-1; i++)
        {
            min = i;
            //find the smallest value in the remainder
            //the array to be sorted
            for (int j = i+1; j < numbers.length; j++)
            {
                if (numbers[j] < numbers[min])
                {
                    min = j;
                }
            }
            //swap two values in the array
            temp = numbers[i];
            numbers[i] = numbers[min];
            numbers[min] = temp;
        }

        System.out.println("Printing sorted result");
        for (int i = 0; i < numbers.length; i++)
        {
            System.out.print(numbers[i]);
        }
    }
}

```

}

## Selection sort

i	0	3	j
	1	8	int
→	2	19	int
	3	16	//se
	4	12	for
			{
			//
			//
			fo
			{
i		2	}
j		5	//
min		4	te
temp		16	n
			n
			)
			Syst
			for
			{
			Sv

```
// selection sort
public class SortTest1
{
    public static void main(String[] args)
    {
        int[] numbers = {16,3,19,8,12};
        int min, temp;
        //select location of next sorted value
        for (int i = 0; i < numbers.length-1; i++)
        {
            min = i;
            //find the smallest value in the remainder
            //of the array to be sorted
            for (int j = i+1; j < numbers.length; j++)
            {
                if (numbers[j] < numbers[min])
                {
                    min = j;
                }
            }
            //swap two values in the array
            temp = numbers[i];
            numbers[i] = numbers[min];
            numbers[min] = temp;
        }

        System.out.println("Printing sorted result");
        for (int i = 0; i < numbers.length; i++)
        {
            System.out.println(numbers[i]);
        }
    }
}
```

## Selection sort

```

i   0   3   j
      1   8
      2   19
      3   16
      4   12

int[] numbers = {16,3,19,8,12};
int min, temp;
//select element of next sorted value
for (int i = 0; i < numbers.length-1; i++)
{
    min = i;
    //find the smallest value in the remainder of
    //the array to be sorted
    for (int j = i+1; j < numbers.length; j++)
    {
        if (numbers[j] < numbers[min])
        {
            min = j;
        }
    }
    //swap two values in the array
    temp = numbers[i];
    numbers[i] = numbers[min];
    numbers[min] = temp;
}
System.out.println("Printing sorted result");
for (int i = 0; i < numbers.length; i++)
{
    System.out.println(numbers[i]);
}

```

## Selection sort

0	3
1	8
2	19
3	16
4	12

i	2
j	5
min	4
temp	19

```
// selection sort
public class SortTest {
    public static void main(String[] args)
    {
        int[] numbers = {16,3,19,8,12};
        int min, temp;
        //select location of next sorted value
        for (int i = 0; i < numbers.length-1; i++)
        {
            min = i;
            //find the smallest value in the remainder
            //of the array to be sorted
            for (int j = i+1; j < numbers.length; j++)
            {
                if (numbers[j] < numbers[min])
                {
                    min = j;
                }
            }
            //swap two values in the array
            temp = numbers[i];
            numbers[i] = numbers[min];
            numbers[min] = temp;
        }

        System.out.println("Printing sorted result");
        for (int i = 0; i < numbers.length; i++)
        {
            System.out.println(numbers[i]);
        }
    }
}
```

## Selection sort

i    0    3    j  
   1    8  
   2    12  
   3    16  
   4    12

min    4  
       19

temp    2  
       5

```
int i;
int j;
//se
for {
    mi
    //
    //
    fo
    {
        }
        // te
        // su
    }
}
Syst
for
{
    Sy
```

```

// selection sort
public class SortTest1
{
    public static void main(String[] args)
    {
        int[] numbers = {16,3,19,8,12};
        int min, temp;
        //select location of next sorted value
        for (int i = 0; i < numbers.length-1; i++)
        {
            min = i;
            //find the smallest value in the remainder
            //of the array to be sorted
            for (int j = i+1; j < numbers.length; j++)
            {
                if (numbers[j] < numbers[min])
                {
                    min = j;
                }
            }
            //swap two values in the array
            temp = numbers[i];
            numbers[i] = numbers[min];
            numbers[min] = temp;
        }

        System.out.println("Printing sorted result");
        for (int i = 0; i < numbers.length; i++)
        {
            System.out.println(numbers[i]);
        }
    }
}

```

## Selection sort

```

i   0   3   j
      8
1   12
3   16
4   19

    → 2   ←

i   2
j   5
min 4
temp 19

int[] numbers = {16,3,19,8,12};
int min = temp;
//select location of next sorted value
for (int i = 0; i < numbers.length-1; i++)
{
    min = i;
    //find the smallest value in the remainder of
    //the array to be sorted
    for (int j = i+1; j < numbers.length; j++)
    {
        if (numbers[j] < numbers[min])
        {
            min = j;
        }
    }
    //swap two values in the array
    temp = numbers[i];
    numbers[i] = numbers[min];
    numbers[min] = temp;
}
System.out.println("Printing sorted result");
for (int i = 0; i < numbers.length; i++)
{
    System.out.println(numbers[i]);
}
}

```



## Selection sort

```
// selection sort
public class SortTest1
{
    public static void main(String[] args)
    {
        int[] numbers = {16,3,19,8,12};
        int min, temp;
        //select location of next sorted value
        for (int i = 0; i < numbers.length-1; i++)
        {
            min = i;
            //find the smallest value in the remainder of
            //the array to be sorted
            for (int j = i+1; j < numbers.length; j++)
            {
                if (numbers[j] < numbers[min])
                {
                    min = j;
                }
            }
            //swap two values in the array
            temp = numbers[i];
            numbers[i] = numbers[min];
            numbers[min] = temp;
        }
        System.out.println("Printing sorted result");
        for (int i = 0; i < numbers.length; i++)
        {
            System.out.println(numbers[i]);
        }
    }
}
```

i 0 3 j  
1 8  
2 12  
3 16  
4 19  
  
i 3  
j 5  
min 3  
temp 16

118

## Selection sort

```
// selection sort
public class SortTest1
{
    public static void main(String[] args)
    {
        int[] numbers = {16,3,19,8,12};
        int min, temp;
        //select location of next sorted value
        for (int i = 0; i < numbers.length-1; i++)
        {
            min = i;
            //find the smallest value in the remainder of
            //the array to be sorted
            for (int j = i+1; j < numbers.length; j++)
            {
                if (numbers[j] < numbers[min])
                {
                    min = j;
                }
            }
            //swap two values in the array
            temp = numbers[i];
            numbers[i] = numbers[min];
            numbers[min] = temp;
        }
        System.out.println("Printing sorted result");
        for (int i = 0; i < numbers.length; i++)
        {
            System.out.println(numbers[i]);
        }
    }
}
```

i 0 3 j  
1 8  
2 12  
3 16  
4 19  
  
i 3  
j 5  
min 3  
temp 16

119

## Selection sort

```
// selection sort
public class SortTest1
{
    public static void main(String[] args)
    {
        int[] numbers = {16,3,19,8,12};
        int min, temp;
        //select location of next sorted value
        for (int i = 0; i < numbers.length-1; i++)
        {
            min = i;
            //find the smallest value in the remainder of
            //the array to be sorted
            for (int j = i+1; j < numbers.length; j++)
            {
                if (numbers[j] < numbers[min])
                {
                    min = j;
                }
            }
            //swap two values in the array
            temp = numbers[i];
            numbers[i] = numbers[min];
            numbers[min] = temp;
        }
        System.out.println("Printing sorted result");
        for (int i = 0; i < numbers.length; i++)
        {
            System.out.println(numbers[i]);
        }
    }
}
```

i 0 3 j  
1 8  
2 12  
3 16  
4 19  
  
i 4  
j 5  
min 3  
temp 16

120

## Selection sort

```
// selection sort
public class SortTest1
{
    public static void main(String[] args)
    {
        int[] numbers = {16,3,19,8,12};
        int min, temp;
        //select location of next sorted value
        for (int i = 0; i < numbers.length-1; i++)
        {
            min = i;
            //find the smallest value in the remainder of
            //the array to be sorted
            for (int j = i+1; j < numbers.length; j++)
            {
                if (numbers[j] < numbers[min])
                {
                    min = j;
                }
            }
            //swap two values in the array
            temp = numbers[i];
            numbers[i] = numbers[min];
            numbers[min] = temp;
        }
        System.out.println("Printing sorted result");
        for (int i = 0; i < numbers.length; i++)
        {
            System.out.println(numbers[i]);
        }
    }
}
```

i 0 3 j  
1 8  
2 12  
3 16  
4 19  
  
i 4  
j 5  
min 3  
temp 16

121

## Selection sort

```
// selection sort
public class SortTest1
{
    public static void main(String[] args)
    {
        int[] numbers = {16,3,19,8,12};
        int min, temp;
        //select location of next sorted value
        for (int i = 0; i < numbers.length-1; i++)
        {
            min = i;
            //find the smallest value in the remainder of
            //the array to be sorted
            for (int j = i+1; j < numbers.length; j++)
            {
                if (numbers[j] < numbers[min])
                {
                    min = j;
                }
            }
            //swap two values in the array
            temp = numbers[i];
            numbers[i] = numbers[min];
            numbers[min] = temp;
        }
        System.out.println("Printing sorted result");
        for (int i = 0; i < numbers.length; i++)
        {
            System.out.println(numbers[i]);
        }
    }
}
```

i 0 3 j  
1 8  
2 12  
3 16  
4 19  
  
i 4  
j 5  
min 3  
temp 16

122

## Tracing with the Debugger

123