# BMatrix_Explainer 

by Matias I. Bofarull Oddo
Department of Computer Science
The University of British Columbia

Fortran


## Paradigm

| Designed by | John Backus |
| :---: | :---: |
| Developer | John Backus and IBM |
| First appeared | 1957; 65 years ago |
| Stable release | Fortran 2018 (ISO/IEC 1539-1:2018) / <br> 28 November 2018; 3 years ago |
| Typing discipline | strong, static, manifest |
| Filename extensions | .f, .for, .f90 |
| Website | fortran-lang.org $C^{\text {S }}$ |
| Majo | implementations |

Absoft, Cray, GFortran, G95, IBM XL Fortran Intel, Hitachi, Lahey/Fujitsu, Numerical Algorithms Group, Open Watcom, PathScale, PGI, Silverfrost, Oracle Solaris Studio, others

Influenced by
Speedcoding
Influenced
ALGOL 58, BASIC, C, Chapel, ${ }^{[1]}$ CMS-2, DOPE, Fortress, PLII, PACT I, MUMPS, IDL, Ratfor

C++
Logo endorsed by the C++ standards
committee

MATLAB (programming language)

| Paradigm | multi-paradigm: functional, imperative, procedural, object-oriented, array |
| :---: | :---: |
| Designed by | Cleve Moler |
| Developer | MathWorks |
| First appeared | late 1970s |
| Stable release | R2022b ${ }^{[1]} /$ / September 15, 2022; 4 days ago |
| Typing discipline | dynamic, weak |
| Filename extensions |  |
| Website | mathworks.come |
| Influenced by |  |
| APL•EISPACK - LINPACK • PLIO Speakeasy ${ }^{[11]}$ |  |
| Influenced |  |
| Julia ${ }^{[12]} \cdot$ Octave ${ }^{[13]} \cdot$ Scilab ${ }^{[14]}$. INTLAB ${ }^{[15\| \| 16\| \| 177][18]}$ |  |

1). MATLAB Programming at Wikibooks

| MATLAB (software) |
| :--- | :--- |


|  |
| :--- | :--- |


|  |  |
| :---: | :---: |
| Paradigm | Multi-paradigm: multiple dispatch (primary paradigm), procedural, functional, meta, multistaged ${ }^{[1]}$ |
| Designed by | Jeff Bezanson, Alan Edelman, Stefan Karpinskj, Viral B. Shah |
| Developer | Jeff Bezanson, Stefan Karpinski, Viral B. Shah, and other contributors ${ }^{[2] \mid 3]}$ |
| First appeared | 2012; 10 years ago ${ }^{[4]}$ |
| Stable release | 1.8.1 $1^{[5]} / 16$ September 2022; 13 days ago and 1.6.7 LTS ${ }^{[8\|9\| 9]}$ / 19 July 2022; 2 months ago |
| Preview release | Being worked on: 1.8. $2^{[6]}$ and $1.9 .0-\mathrm{DEV}$ with dally updates ${ }^{[7]}$ |
| Typing discipline | Dynamic, ${ }^{[10]}$ strong. ${ }^{[10]}$ nominative, parametric, optional |
| Implementation language | Julia, C, C++, Scheme, uvm ${ }^{[11]}$ |
| Plattorm | Tier 1: x86-64, \|A-32, CUDA $10.1+{ }^{[12]}$ Nvidia GPUs flor Linux and Windows) Tier 2: 64-bit Arm (e.g. Apple M1 Macs, while they also have tier 1 support using Rosetta ${ }^{(13)}$, 32-bit Windows (64-bd is ter 1) Tier 3: 32-bit Arm, PowerPC, AMD ( ROCm ) GPUs. Also supports oneAP/Intel's GPUs and Google's TPUs, ${ }^{[14]}$ and has web browser support flor JavaScript and WebAssembly) ${ }^{[15]}$ and can work in Android. For more details see "supported platorms" E. $^{\text {. }}$ |
| os | Linux, macOS, Windows and FreeBSD |
| License | MIT (core), ${ }^{[2]}$ GPL $22_{1}^{116 / 117]}$ a makefile option omits GPL libraries ${ }^{[19]}$ |
| Filename extensions | .j |
| Website | Julialang.orge |
| Influenced by |  |
| $\mathrm{C}^{[4] \cdot} \cdot$ Dylan $^{[19]} \cdot \mathrm{Lisp}^{[4]} \cdot$ Lua $^{[20]}$. Mathematica ${ }^{4 \text { 4/ }}$ (strictly its Wotram Languaga ${ }^{[21](22)} \cdot$ MATLAB ${ }^{(4]} \cdot \operatorname{Per} \boldsymbol{r}^{(20]}$. Python ${ }^{[20]} \cdot \mathrm{R}^{[4]} \cdot$ Rubyy ${ }^{(20)} \cdot$ Scheme ${ }^{[23]}$ |  |




D


Long-story short, I made a Depth-First Search recursive scraper for Wikimedia API to extract knowledge networks hidden in semantically rich infobox fields.

My goal was to interlink these networks to fill information gaps, and then create a human-in-the-loop vis tool for Wikipedia editors.

As you can guess, it didn't go as planned . . .


Influenced by


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## Fortran

From Wikipedia，the free encyclopedia
Fortran（／fortræn／；formerly FORTRAN）is a general－purpose，compiled imperative programming language that is especially suited to numeric computation and scientific computing．
Fortran was originally developed by IBM ${ }^{[2]}$ in the 1950 s for scientific and engineering applications，and subsequently came to dominate scientific computing．It has been in use for over six decades in computationally intensive areas such as numerical weather prediction，finite element analysis，computational fluid dynamics，geophysics，computational physics，crystallography and computational chemistry．It is a popular language for high－performance computing ${ }^{[3]}$ and is used for programs that benchmark and rank the world＇s fastest supercomputers．${ }^{[4][5]}$

Fortran has had numerous versions，each of which has added extensions while largely retaining compatibility with preceding versions．Successive versions have added support for structured programming and processing of character－based data（FORTRAN 77），array programming，modular programming and generic programming（Fortran 90），High Performance Fortran（Fortran 95），object－oriented programming（Fortran 2003），concurrent programming（Fortran 2008），and native parallel computing capabilities（Coarray Fortran 2008／2018）．

Fortran＇s design was the basis for many other programming languages．Among the better－known is BASIC，which is based on FORTRAN II with a number of syntax cleanups，notably better logical structures，${ }^{[6]}$ and other changes to work more easily in an interactive environment．${ }^{[7]}$

Since August 2021 Fortran has ranked among the top 15 languages in the TIOBE index，a measure of the popularity of programming languages．${ }^{[8]}$

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3．1．1 Simple FORTRAN II program
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## LESSON Software that gap－fills Wikipedia is NOT an InfoVis project

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6 Science and engineering
7 Portability
8 Obsolete variants
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| Fortran |  |
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| Designed by | John Backus |
| Developer | John Backus and IBM |
| First appeared 1957； 65 years ago |  |
| Stable release | Fortran 2018 （ISO／EC 1539－ 1：2018）／ 28 November 2018； 4 years ago |
| Typing discipline | strong，static，manifest |
| Filename extensions | ．f，．for，．f90 |
| Website | fortran－lang．org |
| Major implementations |  |

Absoft，Cray，GFortran，G95，IBM XL Fortran， Intel，Hitachi，Lahey／Fujitsu，Numerical Algorithms Group，Open Watcom，PathScale， PGI，Silverfrost，Oracle Solaris Studio，others

## Influenced by

## Speedcoding，Modula－2

 InfluencedALGOL 58，BASIC，C，Chapel，${ }^{[1]}$ CMS－2， DOPE，Fortress，PLI，PACT I，MUMPS，IDL， Ratfor，Coral，Dartmouth BASIC，SISAL，S，

F_Sharp_(programming_language) orth_(programing_language) orth_(programming_language) orth_(programming_language) $\begin{gathered}\text { RPL_(programning_language) } \\ \text { Factor_(orogramminglanguas }\end{gathered}$ language) Joy_(programming_language) orth_(programming_language)
ortran 1DL_(p)
ortran PL/I
ortan MMMPS
ortran MUMPS
fortran Fortres
ortran
fortran PACTESS_(programming_language)
ortran Chapel_(programming_language)
Fortran C_(programing_language
ortran CMS-2
fortran DOPE
fortran DoPE_(Dartmouth_oversimplified_Programming_Experiment)
ortran BASIC
SW-bASIC QBasi
GW-BASIC QuickBASIC
GW-BASIC MSX_BASIC
Go_(programming_language) Crystal_(programming_language
Go_(programing_language) Zig_(programming_language) Haskell Mercury_(programining_language)
Haskell amega
Haskell Isabelle_(proof_assistant)
Haskell Language_Integrated_Query
Haskell LiveScript_(programming_language)
askell PureScript
askell visual_Basic_ NET
Haskell Raku_(programming_language
Haskell Rust_(programming__anguage
Haskell Scala_(programming_language)
Haskell Swift_(programming_language)
Haskell wikipedia:Citation_needed
Haskell Idris_(programming_language)
Haskell Python (programning language)
Haskell Hack_(programming_language)
aaskell Java_(programming_language)
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Haskell Generics_in_Java
Haskell Agda_(programinine_language)
Haskell Bluespec
Haskell C Sharp
Haskell Cayenne_(programming_ language
Haskell Clean_(programming_language)
Haskell C+11
askell Coffeescript
askell Concepts_(C++)
Haskell Curry_(programining_language)
Haskell Epigram_(programing_language)
Haskell Escher_(programming_language)
taskell clojure
ypertalk Sensetalk
yyperTalk AppleScript
HyperTalk ECMASCript
HyperTalk JavaScript
yperTalk Lingo_(programining_language)
HyperTalk LiveCode
Supertal
Iswim gu-zasic
(orogramming language)

Firrected_outgoing_Car_Jung.tsy

Carvin_Frieerveld James_k._A._Smith
Carl_Gustav_Hempel Jaegwon_Kim
Carl_Gustav_Hempel John_Earman
$\begin{array}{ll}\text { Carl_Gustav_Hempel } & \text { Lawrence_sklar } \\ \text { Carl_Gustav_Hempel } & \text { Nelson_Goodman }\end{array}$
Carl_Gustav_Hempel Peter_Achinstein
Carl_Gustav_Hempel Philip_Kitcher
Carl_Gustav_Hempel Richard_Jeffrey
Carl_Gustav_Hempel Robert_Nozick
Carl_Gustav_Hempel Wesley_C._Salmon
$\begin{array}{ll}\text { Carl_Jung } & \text { Robert_Anton_Wil_ } \\ \text { Carl_Jung } & \text { Ross_Nichols }\end{array}$
$\begin{array}{lll}\text { Carl_Jung } & \text { Ross_Nichots } \\ \text { Carl_Jung } & \text { Sigmund_Freud }\end{array}$
Carl_Jung Philip_K._Dick
Carl_Jung Terence_McKenna
Carl_Jung Wolfgang_Pauli

| Carl_Jung | $\begin{array}{l}\text { Sonu_Shamdasani } \\ \text { Carl_Jung } \\ \text { Joseph_Campbell }\end{array}$ |
| :--- | :--- |

$\begin{array}{ll}\text { carl_Jung } & \text { Joseph_Camp } \\ \text { Carl_Jung } \\ \text { Jean_Piaget }\end{array}$
Carl_Jung Jordan_Peters
Carl_Jung James_Hillman
Carl_Jung Hermann_Hesse
Carl_Jung Gaston_Bachelard
arl_Jung Erich_Neumann_(psychologist)
$\begin{array}{lll}\text { Carl_Jung } & \text { Carl_Rogers } \\ \text { Car__Jung } & \text { Arnold_l_ }\end{array}$
Carl_Jung Alan_watts
Carl_schmitt Alan_Jacob_Taubes
Carl_Schmitt Jacques_Derrida
Carl_schmitt Jaime_Guzmán
$\begin{array}{ll}\text { Carl_Schmitt } & \text { Jiang_Shigong } \\ \text { Carl_Schmitt } & \text { Jürgen_Habermas }\end{array}$
$\begin{array}{ll}\text { Carl_Schmitt } & \text { Jurgen_Habermas } \\ \text { Ciu_Xiaofeng_(academic) }\end{array}$
Carl_Schmitt Mario_Tronti
Carl_Schmitt Slavoj_zizizek
Carl_Schmitt $\begin{aligned} & \text { Paul_Gottfried } \\ & \text { Carl_Schitt }\end{aligned}$
Carl_Schmitt Reinhart_Koselleck
$\begin{array}{cc}\text { Carl_Schmitt } & \begin{array}{c}\text { Herfried_Münkler } \\ \text { Carl_Schmitt }\end{array} \\ \text { Susan_Buck-Morss }\end{array}$
Carl_Schmitt
Carl_Schmitt $\begin{aligned} & \text { Susan_Buck-Mors } \\ & \text { Waldemar_Gurian }\end{aligned}$
Carl_Schmitt walter_Benjamin
Carl_Schmitt Wang_Shaoguang
Carl_Schmitt Mark_Lilla
Carl_Schmitt Hans_Morgenthal
Carl_Schmitt Leo_Straus
Carl_schmitt Adam_Wielomski
Carl_Schmitt Adrian_vermeule
Carl_Schmitt Alain_de_Benoist
Carl_Schmitt Aleksandr_Dugin
carl_Schmitt
Andrew_Arato
arloshmitt
Carl_Schmitt Carlo_Galli_(political_scientist)
Carl_Schmitt Chantal_Mouffe
Carl_Schmitt Carlo_Lottieri
Carl_Schmitt Copenhagen_School_(international_relations)
Carl_schmitt Curtis_Yarvir
$\begin{array}{ll}\text { Carl_Schmitt } & \text { Ernst_Jünger } \\ \text { Carl_Schmitt } & \text { Francis_Parker_Yockey }\end{array}$
Carl_schmitt $\begin{aligned} & \text { Friedrich_Hayek }\end{aligned}$
Carl_Schmitt Gianfranco_Miglio
Carl_schmitt Christopher_Ferrara
Carl_Schmitt Hannah_Arendt
arl_stumpf Max_Scheler
Carl_Stumpf Wolfgang_Köhl
Carl_Stumpf Kurt_Koffka
\# by Matias I. Bofarull Oddo - 2022.10.30
import re
import requests
from urllib. parse Beautifulsoup
rest_API = "https://en.wikipedia.org/api/rest_v1/page/html/
param_API $=$ "?redirect=truesstash=false

def scrape_programming_languages(root_href):

```
dict_wikigraph \(=\{ \}\)
def wikiscrape_infobox(page_href):
```

try:
page_href not in dict_wikigraph
dict_wikigraph[page_href] $=$
page = sesh.get (
rest_API + quote_plus(page_href) + param_API,
timeout $=100$,
url_match $=$ url_regex.search(page.url)
true_href = unquote_plus(url_match.group(1))
soup $=$ Beautifulsoup(page.content, "html.parser")
infobox_rows = = [row.prettify() for row in infobox_HTML.find_all

row_index $=0$
data_strings
data_strings $=$ incoming":
-outgoing": ".
for row in infobox_rows:
influenced_by_regex.search(row) or "Influences" in row: data_strings["incoming"] += infobox_rows[row_index]
data_strings["incoming"] $+=$ infobox_rows[row_index +1 1]
if "Influenced" in row:
data_strings["outgoing"]]
data_strings $[$ "outgoing"]
infobox_rows $[$ row_index] data_strings["outgoing"] row_index $+=$
ta_incoming $=$ B
incoming $=$ Beautifulsoup
ata_strings["incoming"],
list_incoming $=[$
str(a["href"])[2:]
for a in data_incoming.find_all
\{"rel": True\},
,
data_outgoing = Beautifulsoup ata_strings ["outgoing"], "html. parser"
list_outgoing $=[$
for a in data_outgoing.find_alle
\{"rel": True\},
fage_href in dict_wikigraph:

## What are other ways to understand

 and better work with information



Fig. 1 Example networks and their portraits. The random network is an Erdős-Rényi graph while the real network is the NCAA Division-I football network (Park and Newman 2005). Colors denote the entries of the portrait matrix $B$ (Eq. (2); white indicates $B_{\ell, k}=0$ )


## Random network




Regular network




Fig. 1 Example networks and their portraits. The random network is an Erdős-Rényi graph while the real network is the NCAA Division-I football network (Park and Newman 2005). Colors denote the entries of the portrait matrix $B$ (Eq. (2); white indicates $B_{\ell, k}=0$ )





Fig. 1 Example networks and their portraits. The random network is an Erdős-Rényi graph while the real network is the NCAA Division-I football network (Park and Newman 2005). Colors denote the entries of the portrait matrix $B$ (Eq. (2); white indicates $B_{\ell, k}=0$ )


Nodes in $l$-shell


FIG. 12. (Color online) Evolution of a $B$ matrix portrait when using the order-parameter performance measure with $\hat{\sigma}=0.6$. Initial topology was a periodic ring lattice with nearest and next-nearest-neighbor coupling. $B$ matrices were taken at iterations (a) 1 , (b) 4000 , (c) 8000 , (d) 14000 , (e) 20000 , and (f) 180000 . Colors represent the number of nodes at a given index within the $B$ matrix and are plotted on a $\log$ scale $\left[\log \left(b_{l k}\right)\right]$.


(a)

FUN FACT
This is the first published network portrait.

(b)

Fig. 2: (Color online) (a) A $B$-Matrix with a logarithmic color scale (the white background indicates zero elements of $B$ ). The degree distribution is slightly visible in the first row. The "turning point" about row 4 represents finite-size effects. Shown is the network of the $10 \%$ most connected actors on IMDB [2]. (b) The same matrix with a logarithmic horizontal axis. The degree distribution is now clearly visible.

How exactly do we get a graph's B-Matrix? How do we interpret a network portrait? That's exactly what BMatrix_Explainer is all about.
github.com/dirediredock/BMatrix_Explainer



To get started with BMatrix_Explainer, consider this small graph as an explainer example:

- It has 7 nodes and 14 edges
- Edgelist:

$$
\begin{aligned}
& 1-2 \\
& 1-3 \\
& 2-4 \\
& 2-5 \\
& 2-6 \\
& 2-3 \\
& 3-4 \\
& 3-5 \\
& 3-6 \\
& 4-5 \\
& 4-6 \\
& 5-7 \\
& 5-6 \\
& 6-7
\end{aligned}
$$



We start by picking a node, and initialize an empty matrix.

| 0 | 0 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 |



Rows are for number of hops away from this starting node, and columns are for node counts.

| 0 | 0 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 |



We only have one node at hand (no hops yet), so we flip the bit at zeroth row and first column.

| 0 | $\mathbf{1}$ | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 |



Then at first hop, there are two nodes - so we flip the bit at the first row and second column.

| 0 | 1 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 1 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 |



At second hop there are three nodes, so we flip the bit at the second row and third column.

| 0 | $\mathbf{1}$ | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | $\mathbf{1}$ | 0 | 0 | 0 |
| 0 | 0 | 0 | $\mathbf{1}$ | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 |



At third hop there is one node (last one), so we flip the bit at the third row and first column.

| 0 | $\mathbf{1}$ | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | $\mathbf{1}$ | 0 | 0 | 0 |
| 0 | 0 | 0 | $\mathbf{1}$ | 0 | 0 |
| 0 | $\mathbf{1}$ | 0 | 0 | 0 | 0 |



This completes the bit matrix of node 1 (of 7 ).

| 0 | 1 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 1 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 0 | 0 |
| 0 | $\mathbf{1}$ | 0 | 0 | 0 | 0 |



We repeat and get a bit matrix for node 2 (of 7), and we store the already completed matrix.

| 0 | $\mathbf{1}$ | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 0 | 0 | 0 | $\mathbf{1}$ |
| 0 | $\mathbf{1}$ | 0 | 0 | 0 | 0 |
| $\mathbf{1}$ | 0 | 0 | 0 | 0 | 0 |



This is the bit matrix of node 3 (of 7), and we save the two already completed matrices.

| 0 | 1 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 0 | 0 | 0 | 1 |
| 0 | 1 | 0 | 0 | 0 | 0 |
| 1 | 0 | 0 | 0 | 0 | 0 |



The bit matrix of node 4 (of 7), and we save the three already completed matrices.

| 0 | 1 | 0 | 0 | 0 | 0 |
| :---: | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 1 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 0 | 0 |
| 0 | 1 | 0 | 0 | 0 | 0 |



The bit matrix of node 5 (of 7), and we save the four already completed matrices.

| 0 | 1 | 0 | 0 | 0 | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 | 0 | 1 |
| 0 | $\mathbf{1}$ | 0 | 0 | 0 | 0 |
| 1 | 0 | 0 | 0 | 0 | 0 |



The bit matrix of node 6 (of 7), and we save the five already completed matrices.



Finally, the bit matrix of node 7 (of 7), and we save the six already completed matrices.



We add these seven bit matrices element-wise into a single matrix. This ends the algorithm.

| 0 | $\mathbf{7}$ | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | $\mathbf{2}$ | 0 | $\mathbf{1}$ | $\mathbf{4}$ |
| 0 | $\mathbf{4}$ | $\mathbf{1}$ | $\mathbf{2}$ | 0 | 0 |
| $\mathbf{5}$ | $\mathbf{2}$ | 0 | 0 | 0 | 0 |

We're done!
The B-Matrix of the graph.

And it has a bunch of properties.

| 0 | $\mathbf{7}$ | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | $\mathbf{2}$ | 0 | $\mathbf{1}$ | $\mathbf{4}$ |
| 0 | $\mathbf{4}$ | $\mathbf{1}$ | $\mathbf{2}$ | 0 | 0 |
| $\mathbf{5}$ | $\mathbf{2}$ | 0 | 0 | 0 | 0 |

Also each row adds up to the total number of nodes.


The first row marks the number of times different node counts happened at exactly one hop away from the starting node.

The node degree is how many edges a node has, so this row is effectively a record of frequency of node degrees.


We can visualize the distribution of node degrees with a bar chart of counts (histogram).



Frequency of node degrees

[Row 1, Column 2] Two nodes of degree 2

| 0 | $\mathbf{7}$ | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | $\mathbf{2}$ | 0 | $\mathbf{1}$ | $\mathbf{4}$ |
| 0 | $\mathbf{4}$ | $\mathbf{1}$ | $\mathbf{2}$ | 0 | 0 |
| $\mathbf{5}$ | $\mathbf{2}$ | 0 | 0 | 0 | 0 |


[Row 1, Column 4] One node of degree 4

| 0 | $\mathbf{7}$ | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | $\mathbf{2}$ | 0 | $\mathbf{1}$ | $\mathbf{4}$ |
| 0 | $\mathbf{4}$ | $\mathbf{1}$ | $\mathbf{2}$ | 0 | 0 |
| $\mathbf{5}$ | $\mathbf{2}$ | 0 | 0 | 0 | 0 |


[Row 1, Column 5] Four nodes of degree 5

| 0 | $\mathbf{7}$ | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | $\mathbf{2}$ | 0 | $\mathbf{1}$ | $\mathbf{4}$ |
| 0 | $\mathbf{4}$ | $\mathbf{1}$ | $\mathbf{2}$ | 0 | 0 |
| $\mathbf{5}$ | $\mathbf{2}$ | 0 | 0 | 0 | 0 |

Finally, the last row is the maximum number of hops the algorithm got through before running out of nodes.

In other words, the final hop number is equivalent to the diameter of the graph, $L$-shell of 3 in this case.


| 0 | $\mathbf{7}$ | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | $\mathbf{2}$ | 0 | $\mathbf{1}$ | $\mathbf{4}$ |
| 0 | $\mathbf{4}$ | $\mathbf{1}$ | $\mathbf{2}$ | 0 | 0 |
| $\mathbf{5}$ | $\mathbf{2}$ | 0 | 0 | 0 | 0 |

Frequency of node 3-shell degrees


The graph diameter is the length of the shortest path between the two most distanced nodes.

| 0 | $\mathbf{7}$ | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | $\mathbf{2}$ | 0 | $\mathbf{1}$ | $\mathbf{4}$ |
| 0 | $\mathbf{4}$ | $\mathbf{1}$ | $\mathbf{2}$ | 0 | 0 |
| $\mathbf{5}$ | $\mathbf{2}$ | 0 | 0 | 0 | 0 |

Frequency of node 3-shell degrees

In contrast to this explainer example, the B-Matrix of a real-world graph can be very large.

It is not practical to show this data abstraction directly with numbers, we need a visual encoding.

| 0 | $\mathbf{7}$ | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | $\mathbf{2}$ | 0 | $\mathbf{1}$ | $\mathbf{4}$ |
| 0 | $\mathbf{4}$ | $\mathbf{1}$ | $\mathbf{2}$ | 0 | 0 |
| $\mathbf{5}$ | $\mathbf{2}$ | 0 | 0 | 0 | 0 |

In literature this is solved by mapping the B-Matrix node count to a colormap range.


| 0 | $\mathbf{7}$ | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | $\mathbf{2}$ | 0 | $\mathbf{1}$ | $\mathbf{4}$ |
| 0 | $\mathbf{4}$ | $\mathbf{1}$ | $\mathbf{2}$ | 0 | 0 |
| $\mathbf{5}$ | $\mathbf{2}$ | 0 | 0 | 0 | 0 |



However, we can do one more edit to increase information resolution in this heatmap idiom.

Notice that the zeroth row always has the highest value (which sets the colormap extreme).

In large networks this value can be
 so high that the colormap must be log-transformed.

## We can safely

 remove the zeroth row.This is fine because this row only contains redundant data (total node count).


Then we can get higher fidelity by rescaling the colormap.

| $\mathbf{5}$ | 0 | 0 | $\mathbf{2}$ | 0 | $\mathbf{1}$ | 4 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{4}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{4}$ | $\mathbf{1}$ | $\mathbf{2}$ |
| $\mathbf{3}$ | 0 | 0 |  |  |  |  |
| $\mathbf{2}$ |  | $\mathbf{2}$ | 0 | 0 | 0 | 0 |
| $\mathbf{1}$ |  |  |  |  |  |  |

That's it!
This figure is the network portrait of the graph.


Now let's explore real-world networks with

## BMatrix_Explainer

a Python-based B-Matrix visualization GitHub repo.


| Graph | networkx.graph_atlas(1115) |
| :--- | :--- | :--- |
| Nodes | 7 |
| Edges | 14 |

Recall that each row of the B-Matrix can be visually encoded as stacked bars for count data.


BMatrix_Explainer fully features this visualization
with bars encoding node counts, or histograms.


And that is not all! To further support interpretation tasks, in BMatrix_Explainer both color and bar encondings can have per-row normalization to enhance information discovery within hop level.



A small "small-world" network.



Knowledge network from Fortran infobox.




Knowledge network from Carl Jung infobox.



For future work, I would like to build a B-Matrix reverse-highlight visualization system.
This can help network exploration tasks such as understanding nodes with special properties, where these located, and in relation to what global network features.


## Thank You!

To check out code, data, and more figures
https://github.com/dirediredock/BMatrix_Explainer https://github.com/dirediredock/infobox_īnterlinker

