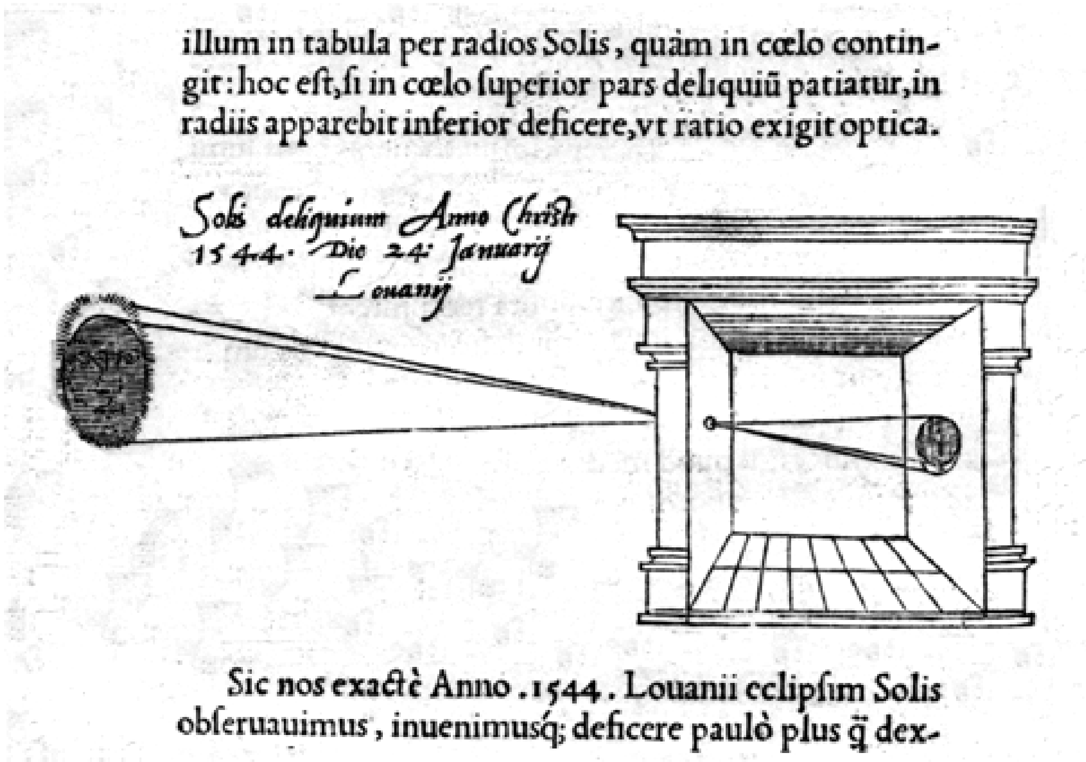
Cameras

(Reading: Chapter 1)

- **Goal:** understand how images are formed
- Camera obscura dates from 15th century
- Basic abstraction is the pinhole camera
- Perspective projection is a simple mathematical operation that discards one dimension
- The human eye functions very much like a camera

Camera Obscura


illum in tabula per radios Solis, quàm in cœlo contin-
git: hoc eſt, ſi in cœlo ſuperior pars deliquiũ patiatur, in
radiis apparebit inferior deficere, vt ratio exigit optica.

Sic nos exactè Anno .1544. Louanii eclipſim Solis
obſeruauimus, inuenimusq; deficere paulò plus q̃ dex-

"When images of illuminated objects ... penetrate through a small hole into a very dark room ... you will see [on the opposite wall] these objects in their proper form and color, reduced in size ... in a reversed position, owing to the intersection of the rays". *Da Vinci*

http://www.acmi.net.au/AIC/CAMERA_OBSCURA.html (Russell Naughton)

Slide credit: David Jacobs

Jetty at Margate England, 1898.

http://brightbytes.com/cosite/collection2.html (Jack and Beverly Wilgus)

Slide credit: David Jacobs

First known photograph

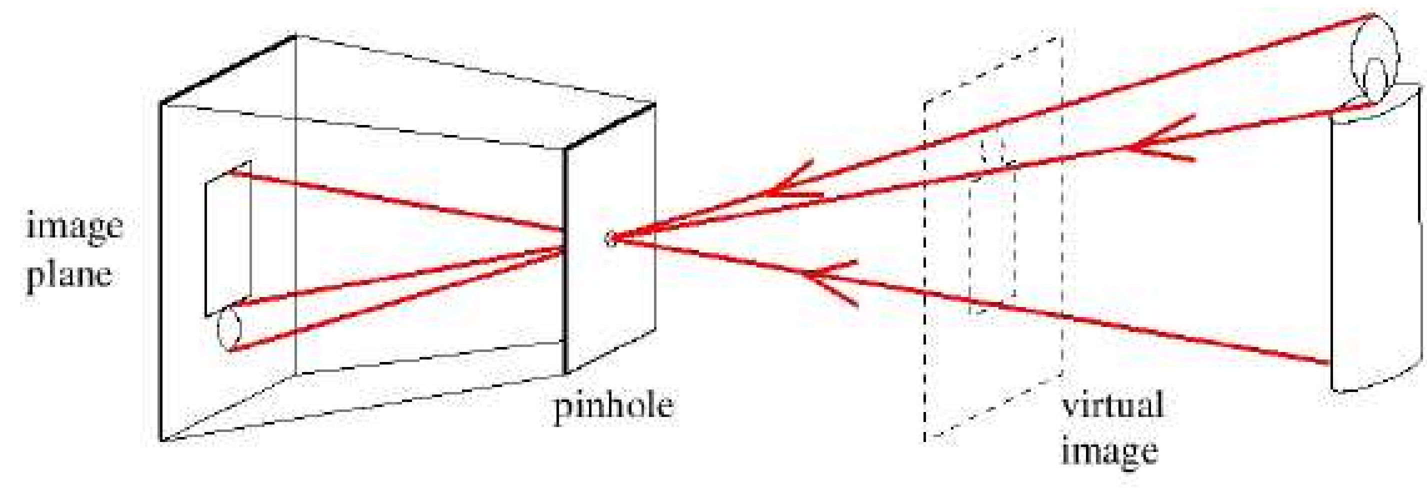
La table servie

Forsyth & Ponce Figure 1.16

Credit: Nicéphore Niepce, 1822

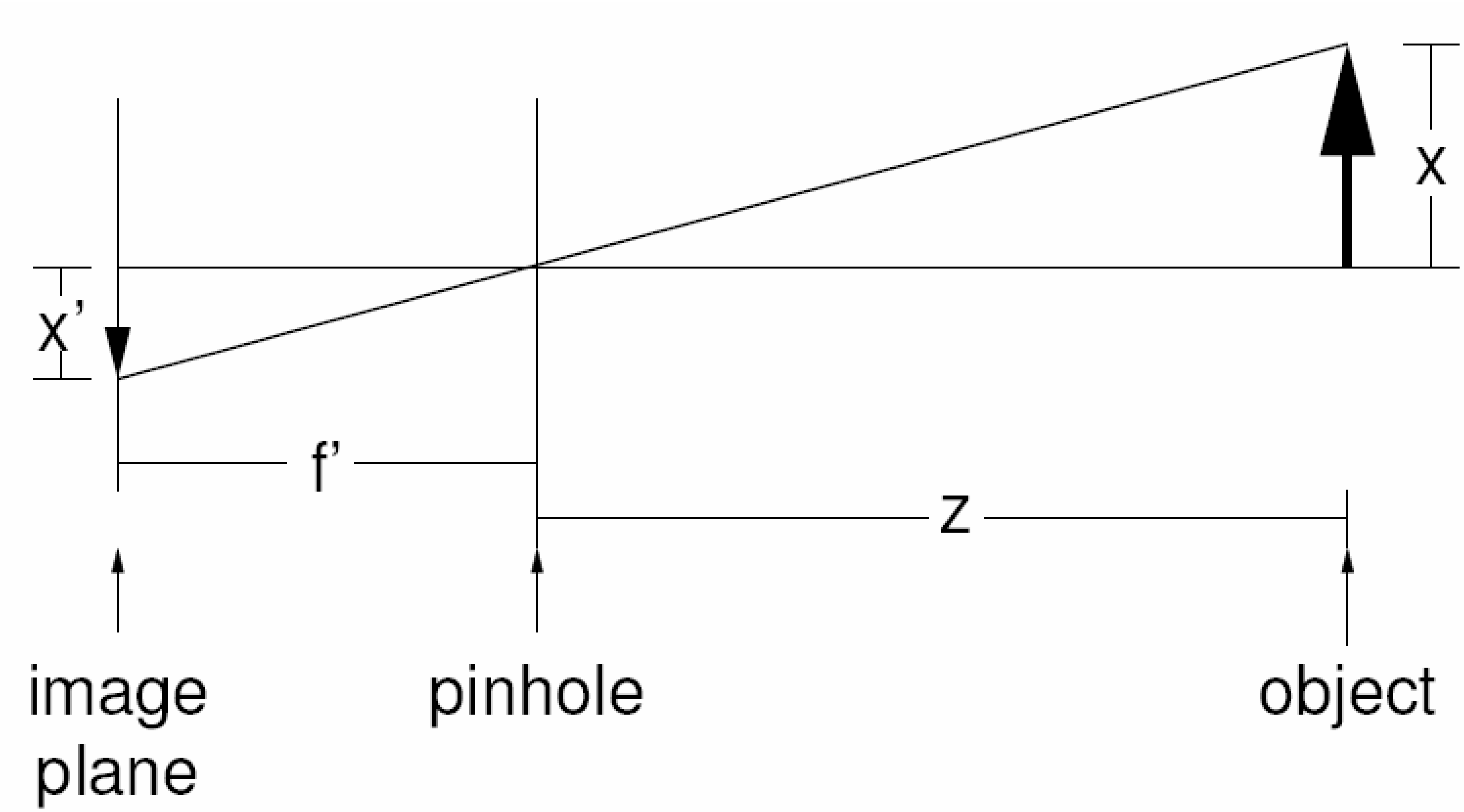
Pinhole cameras

- Pinhole camera - box with a small hole in it
- Image is upside down, but not mirrored left-to-right
- **Question:** Why does a mirror reverse left-to-right but not top-to-bottom?



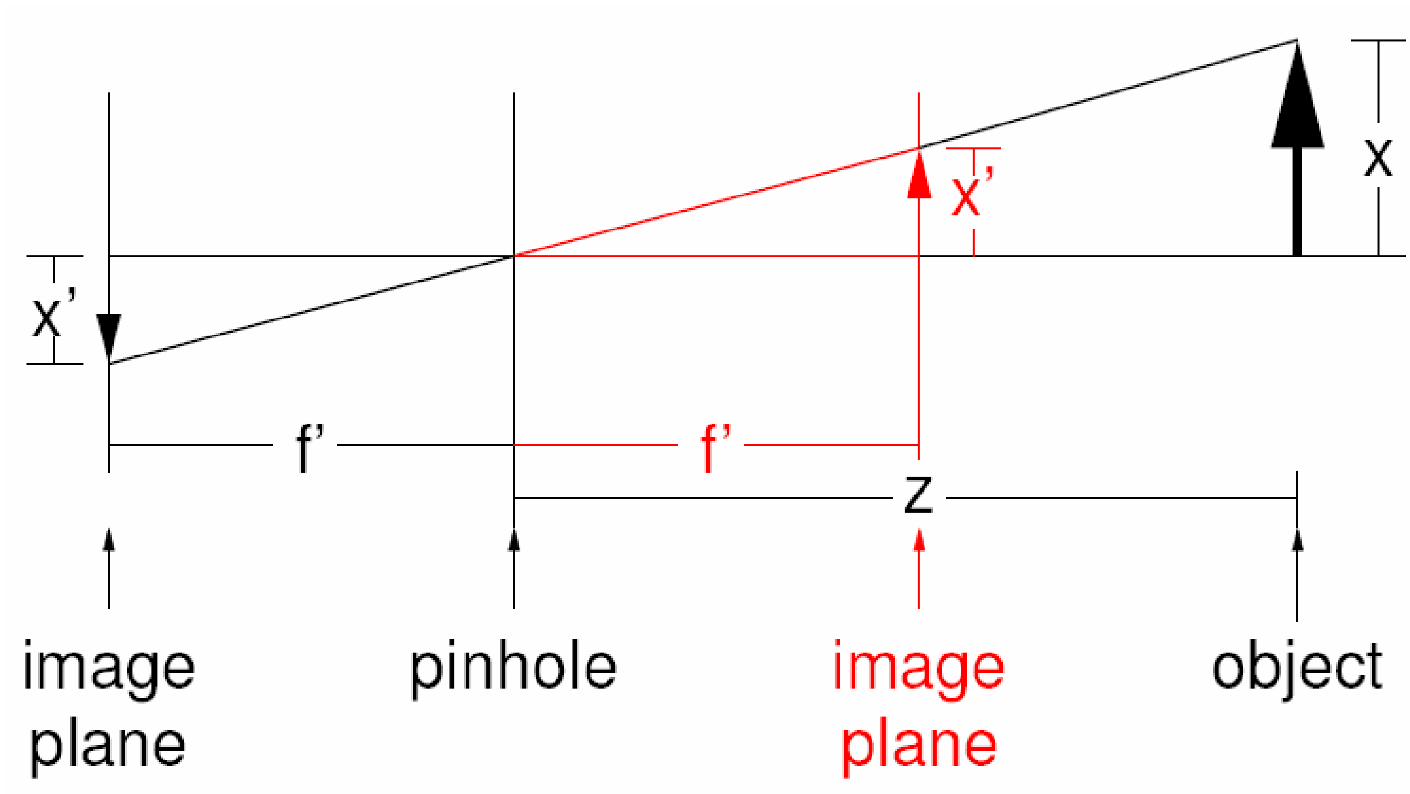
Forsyth & Ponce Figure 1.2

Pinhole camera in 2D



$$X' = (f' / Z)\ X$$

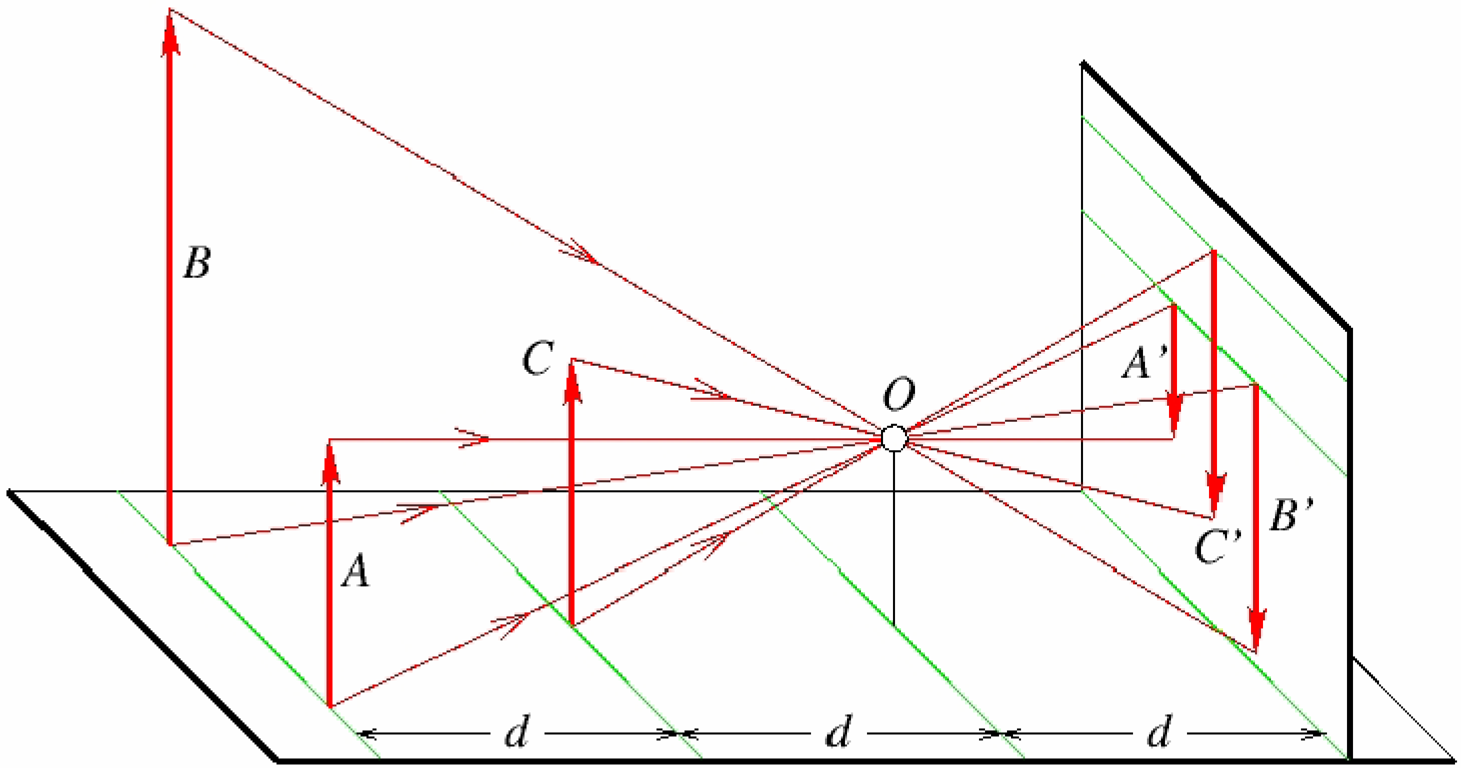
Pinhole camera in 2D
(with reflected image plane)



The image is the same after reflection of the image plane, except that image is the right way up!

Distant objects are smaller

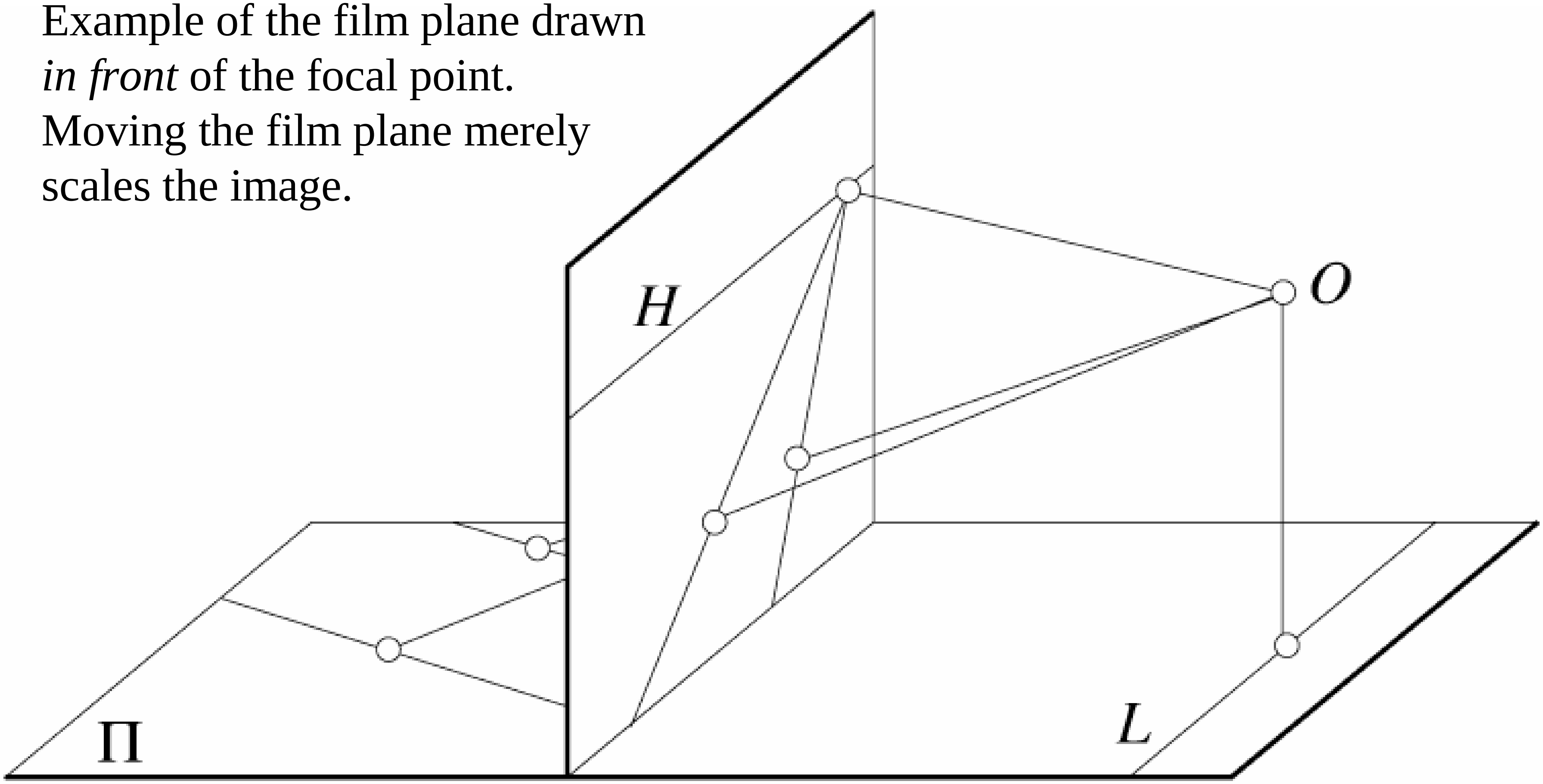
Size is inversely proportional to distance.



Forsyth & Ponce Figure 1.3a

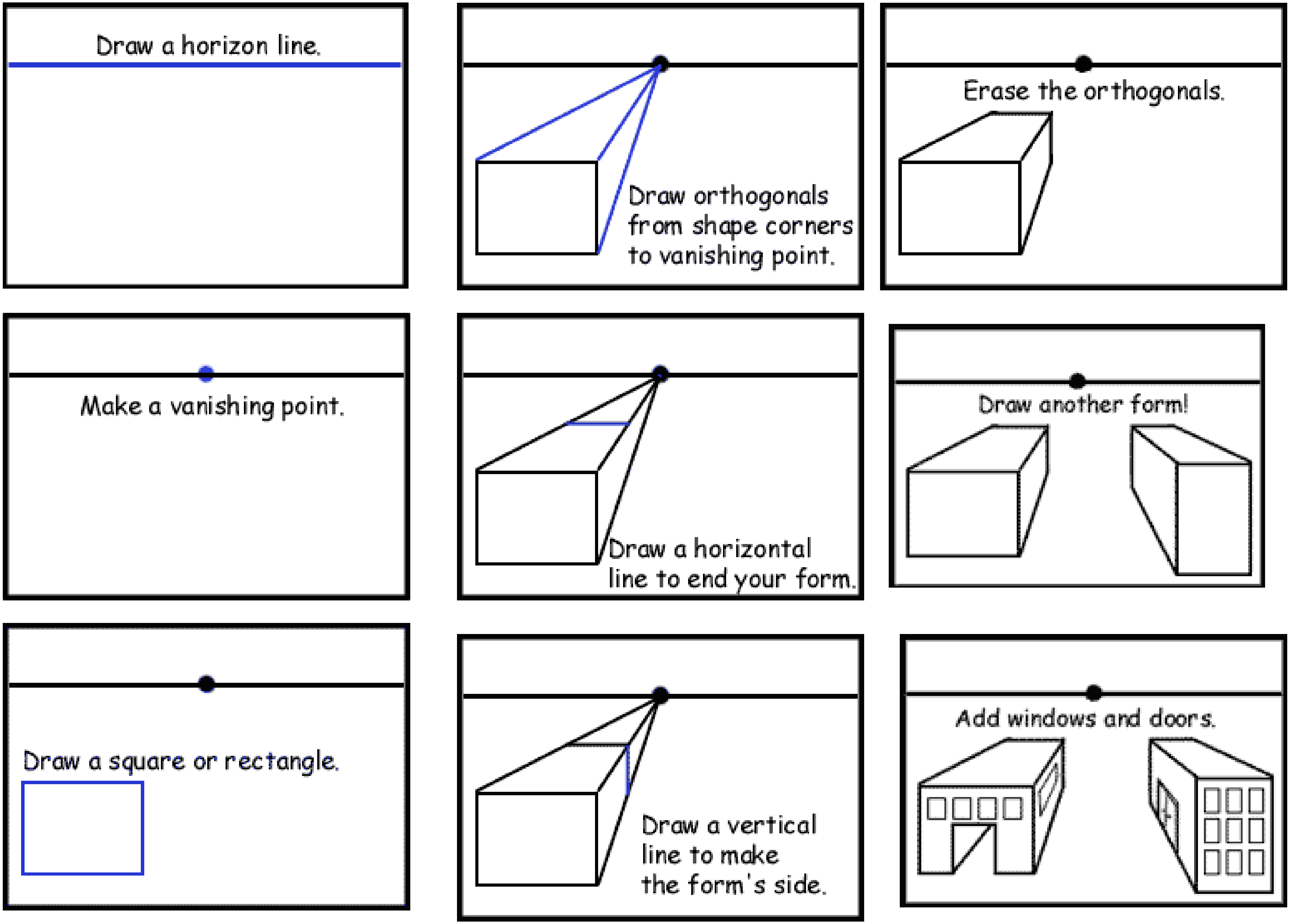
Parallel lines meet

Example of the film plane drawn *in front* of the focal point. Moving the film plane merely scales the image.



Vanishing points

- each set of parallel lines meets at a different point
  - The *vanishing point* for this direction
- Sets of parallel lines on the same plane lead to *collinear* vanishing points.
  - The line is called the *horizon* for that plane
- Good ways to spot faked images
  - scale and perspective don't work
  - vanishing points behave badly

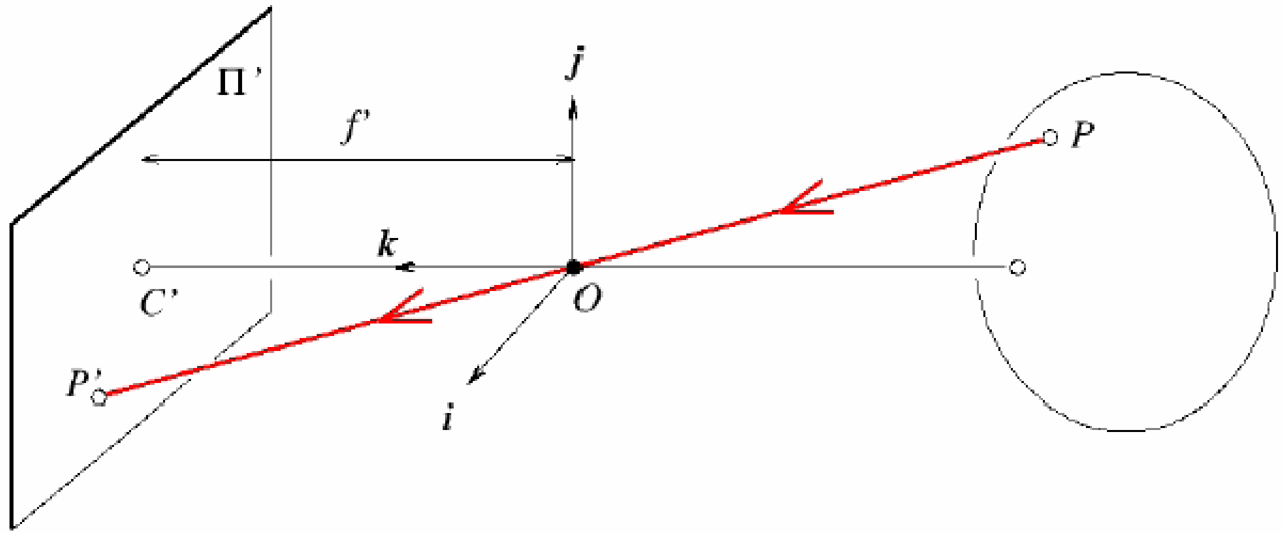


Slide credit: David Jacobs

Properties of perspective projection

- Points project to points
- Lines project to lines
- Planes project to the whole or half image
- Angles are not preserved
- Degenerate cases
  - Line through focal point projects to a point.
  - Plane through focal point projects to line

The equation of perspective projection



Forsyth & Ponce Figure 1.4

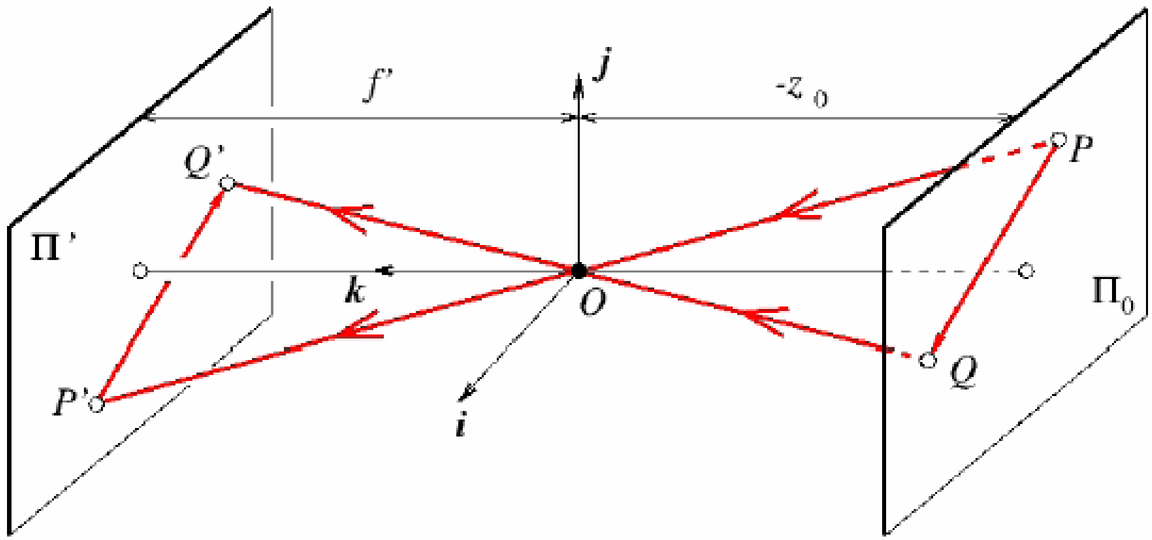
3D object point, $P[x, y, z]$, projects to 2D image point $P'[x', y']$ where

$$x' = f' \frac{x}{z}$$

$$y' = f' \frac{y}{z}$$

Weak perspective

Assume object points are all at same depth $-z_0$



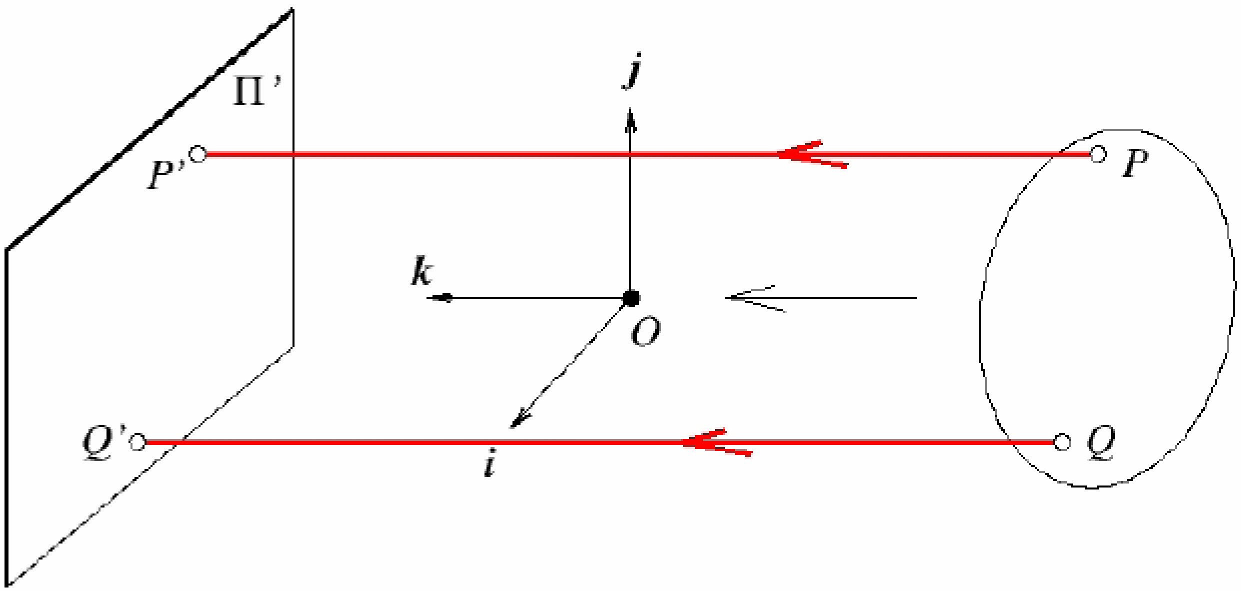
Forsyth & Ponce Figure 1.5

3D object point, $P[x, y, z]$ in Π_0, projects to 2D image point $P'[x', y']$ where

$$\begin{aligned} x' &= -m\,x \\ y' &= -m\,y \end{aligned}$$

where $m = -\frac{f'}{z_0}$

Orthographic projection



Forsyth & Ponce Figure 1.6

3D object point, $P[x, y, z]$, projects to 2D image point $P'[x', y']$ where

$$\begin{aligned} x' &= x \\ y' &= y \end{aligned}$$

Pros and Cons of These Models

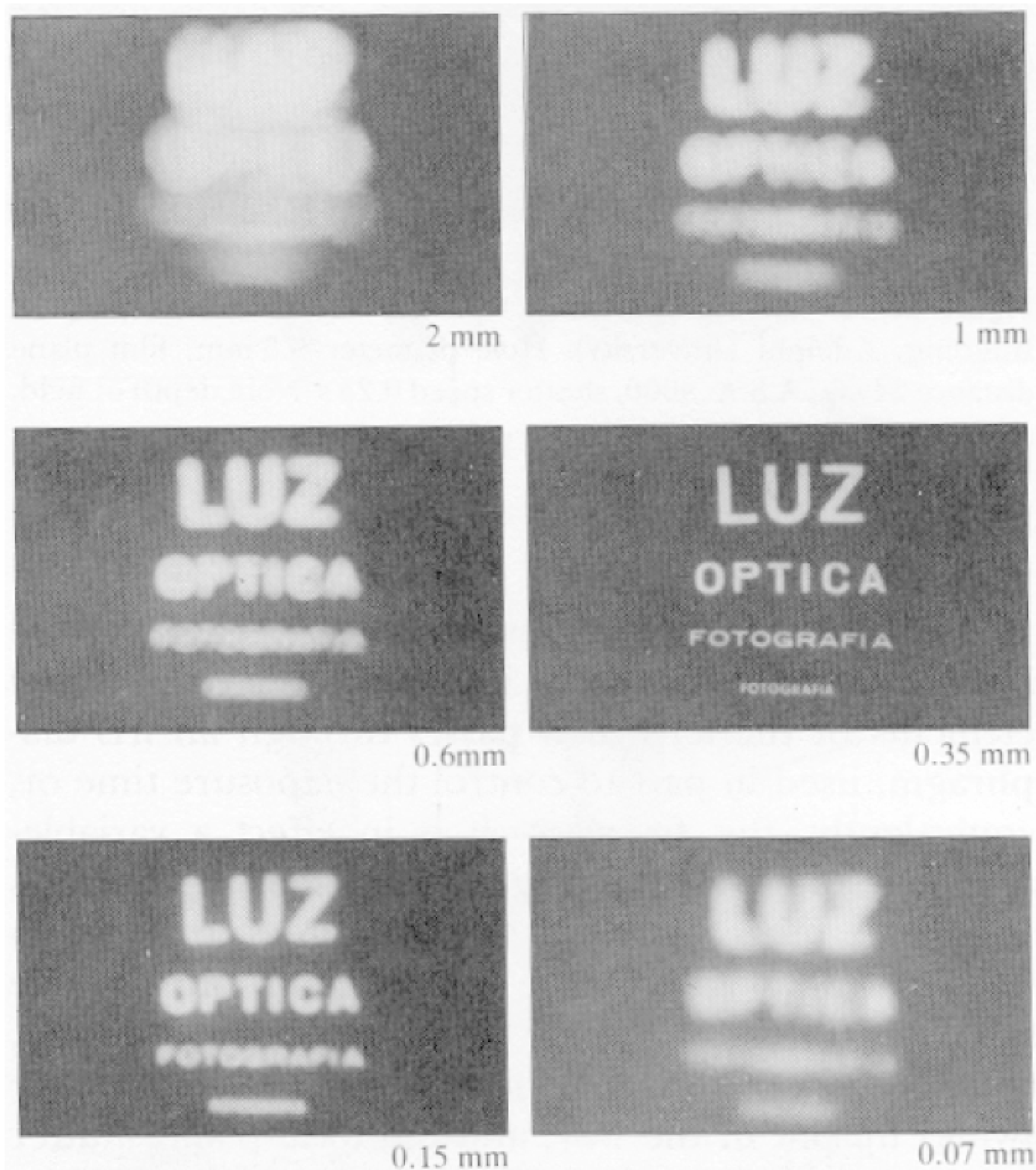
- Weak perspective (including orthographic) has simpler mathematics
  - Accurate when object is small relative to its distance.
  - Most useful for recognition.
- Perspective is much more accurate for scenes.
  - Used in structure from motion.
- When accuracy really matters, we must model the real camera
  - Use perspective projection with other calibration parameters (e.g., radial lens distortion)

Why not use pinhole cameras?

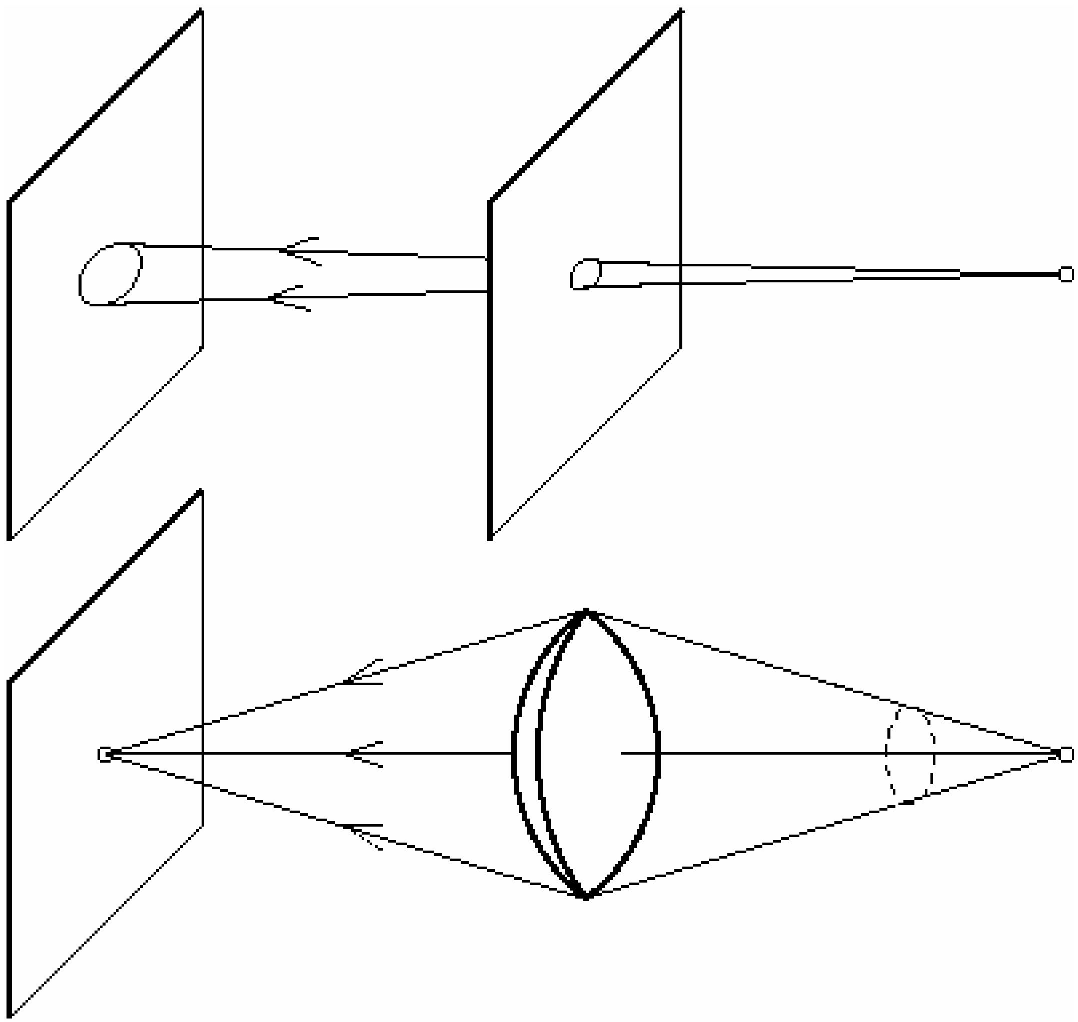
If pinhole is too big - many directions are averaged, blurring the image

Pinhole too small- diffraction effects blur the image

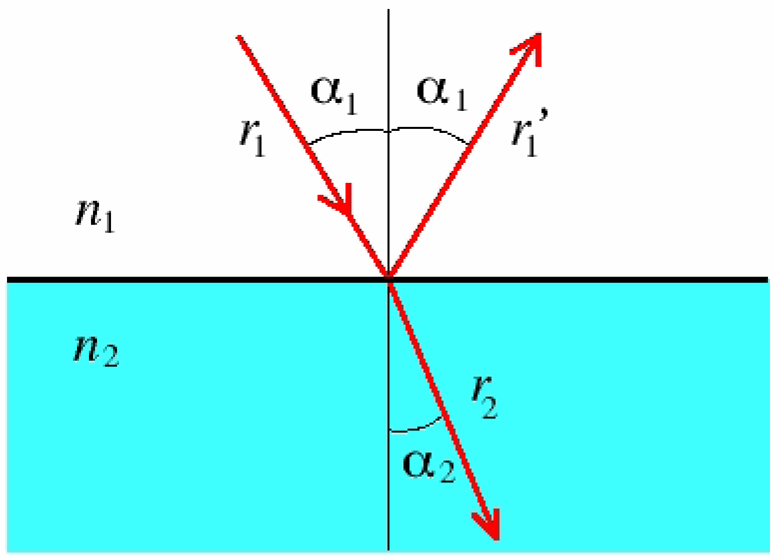
Generally, pinhole cameras are *dark*, because a very small set of rays from a particular point hits the screen.



The reason for lenses



Snell's law

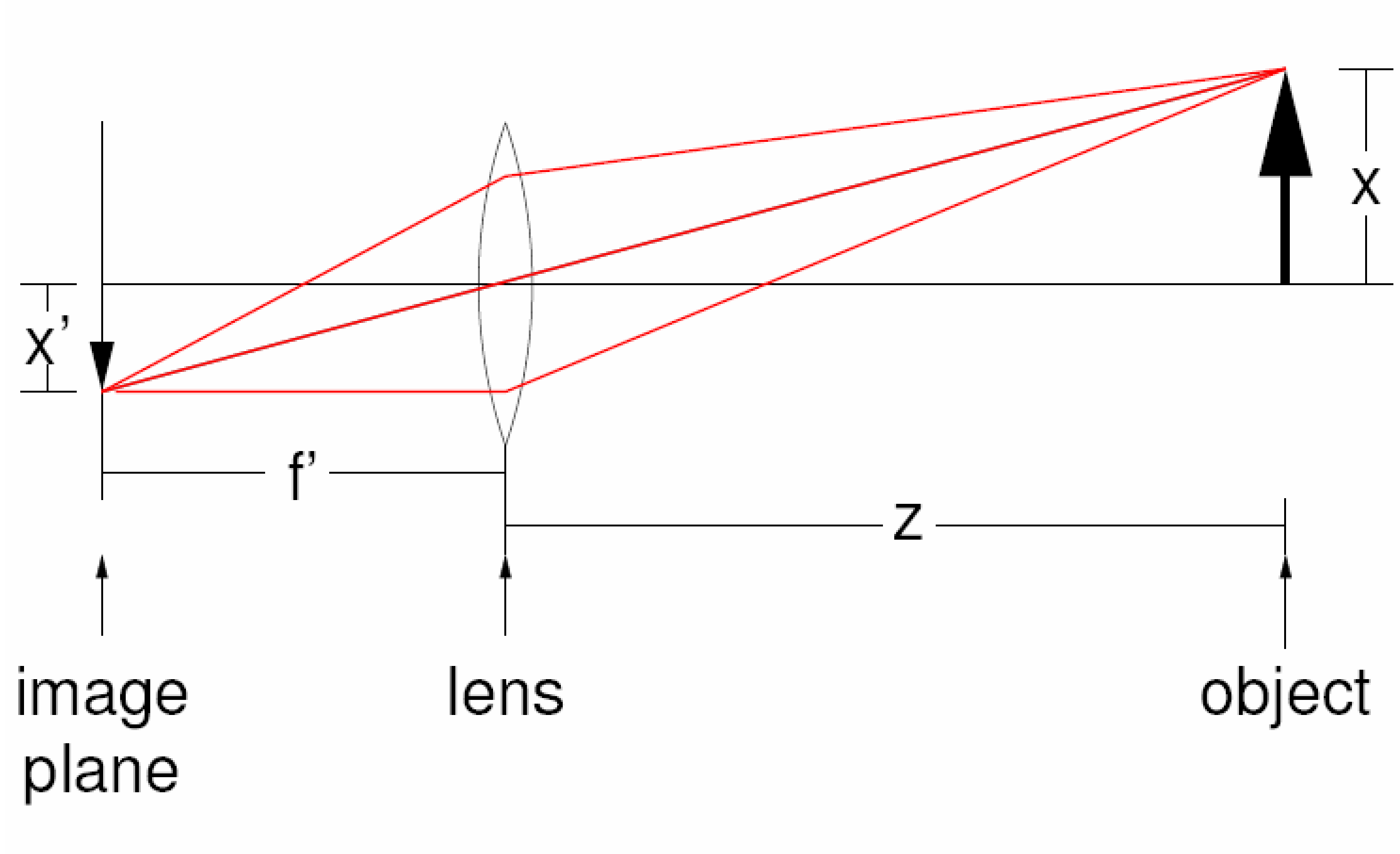


Forsyth & Ponce Figure 1.7

$$n_1 \sin\alpha_1 = n_2 \sin\alpha_2$$

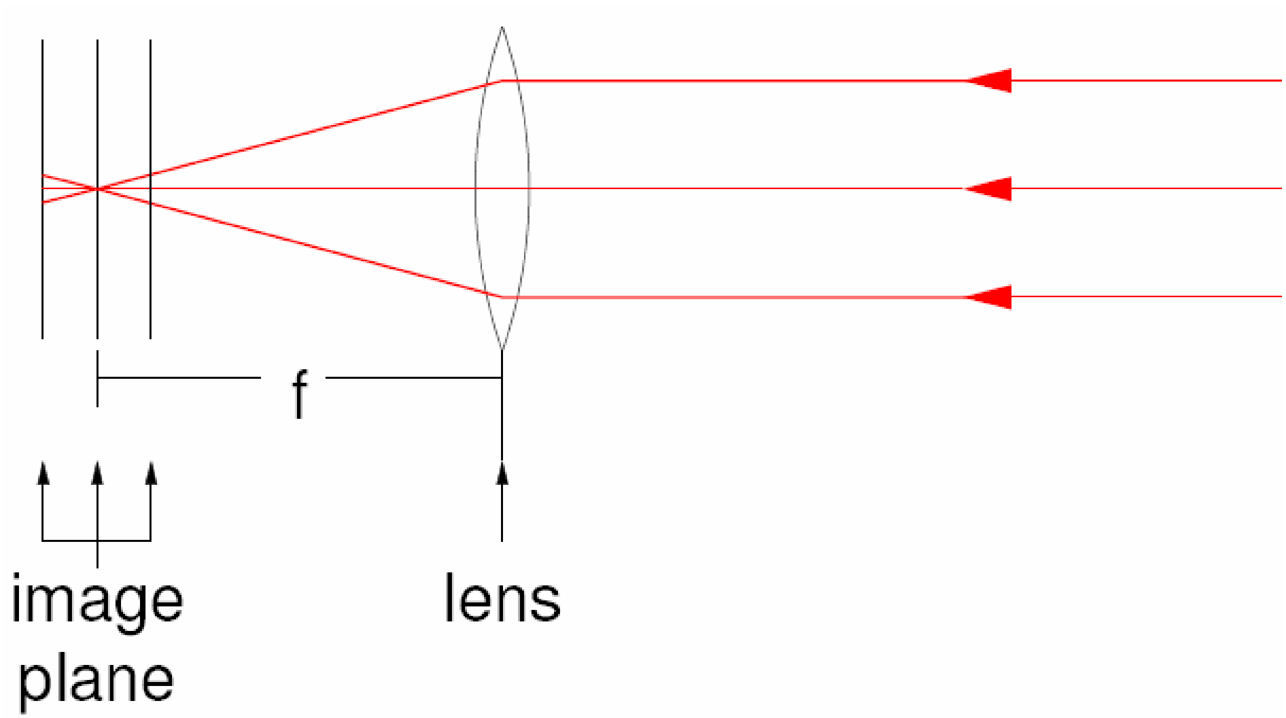
n_1 and n_2 are the indices of refraction of each material

Pinhole model with a single lens



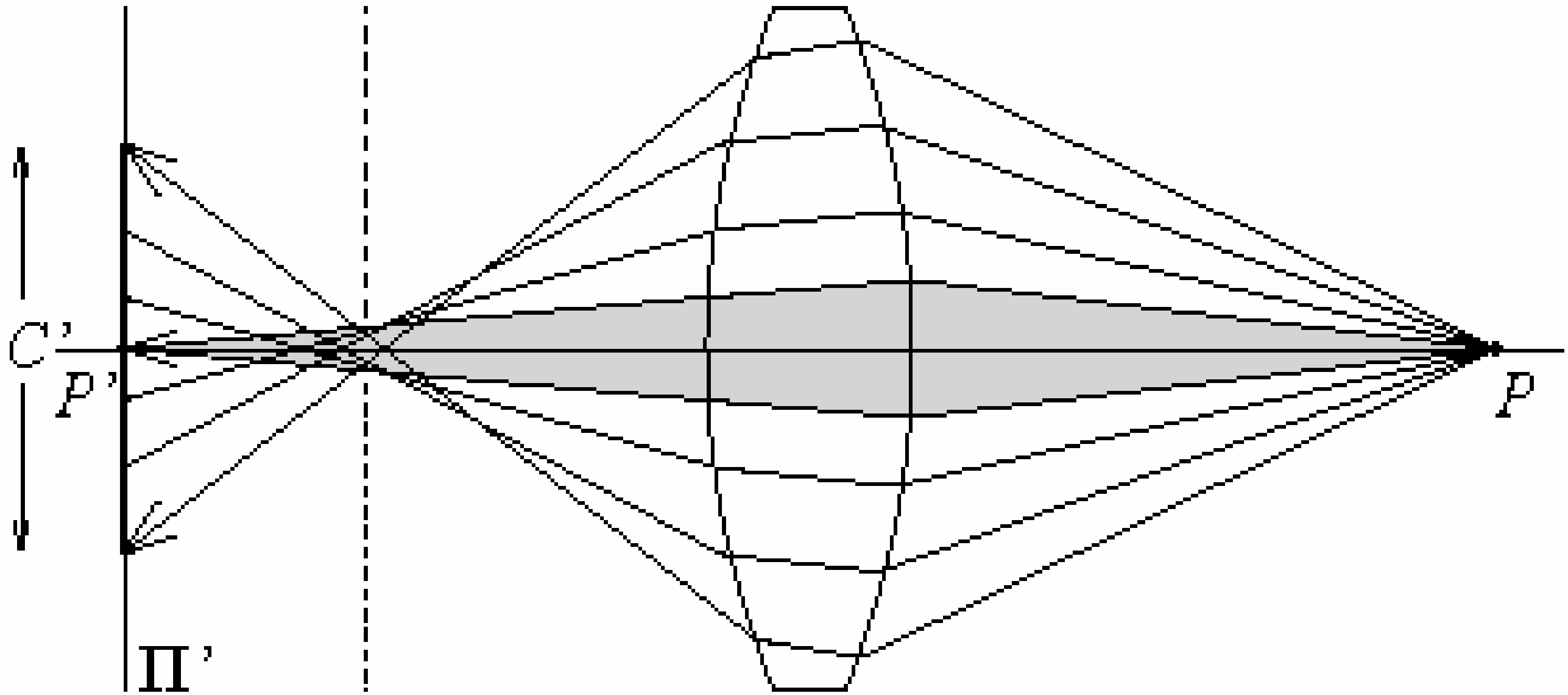
A lens follows the pinhole model for objects that are in focus.

An out-of-focus lens



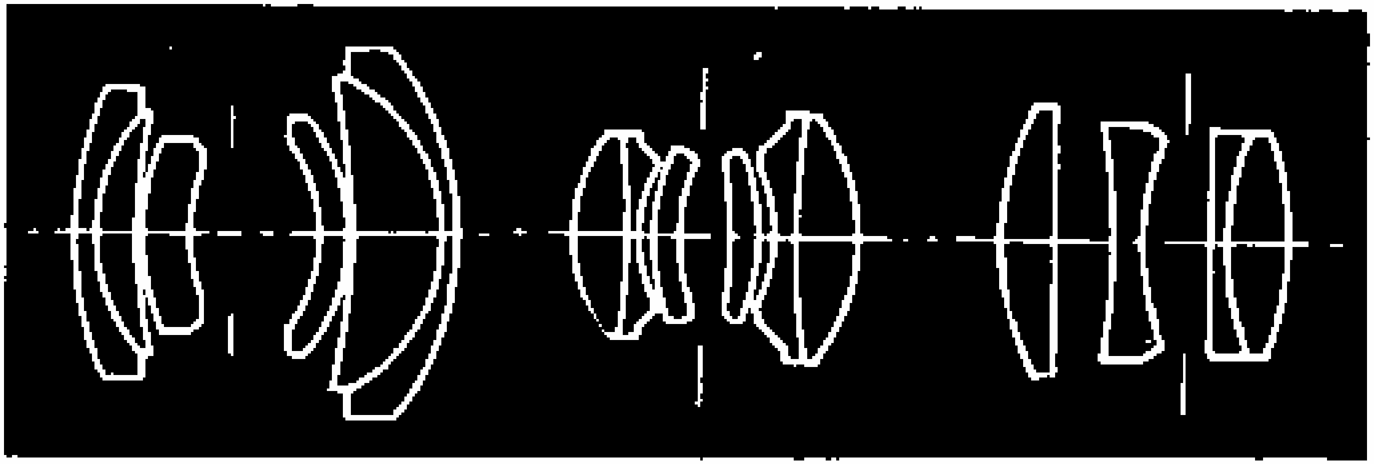
An image plane at the wrong distance means that rays from different parts of the lens create a blurred region (the "point spread function").

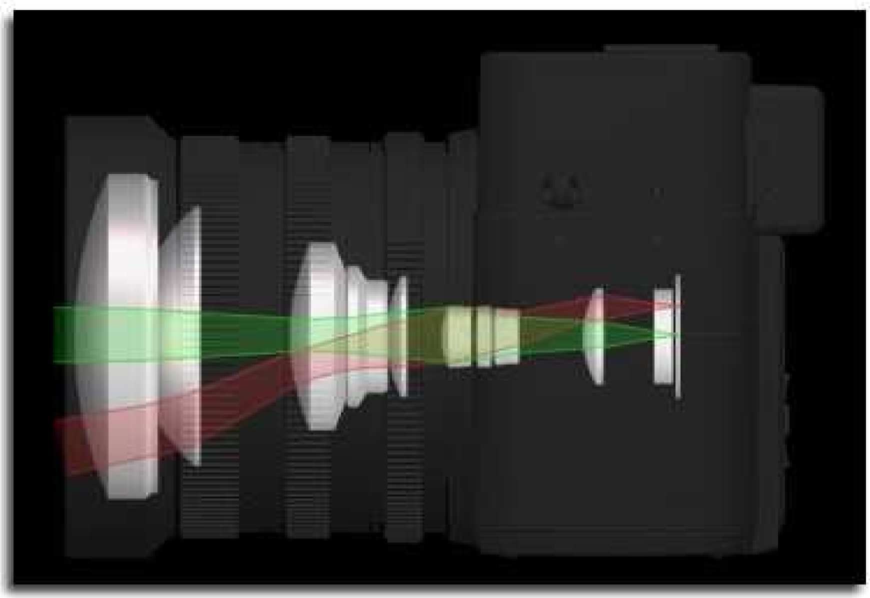
Spherical aberration



Historically, spherical lenses were the only easy shape to manufacture, but are not correct for perfect focus.

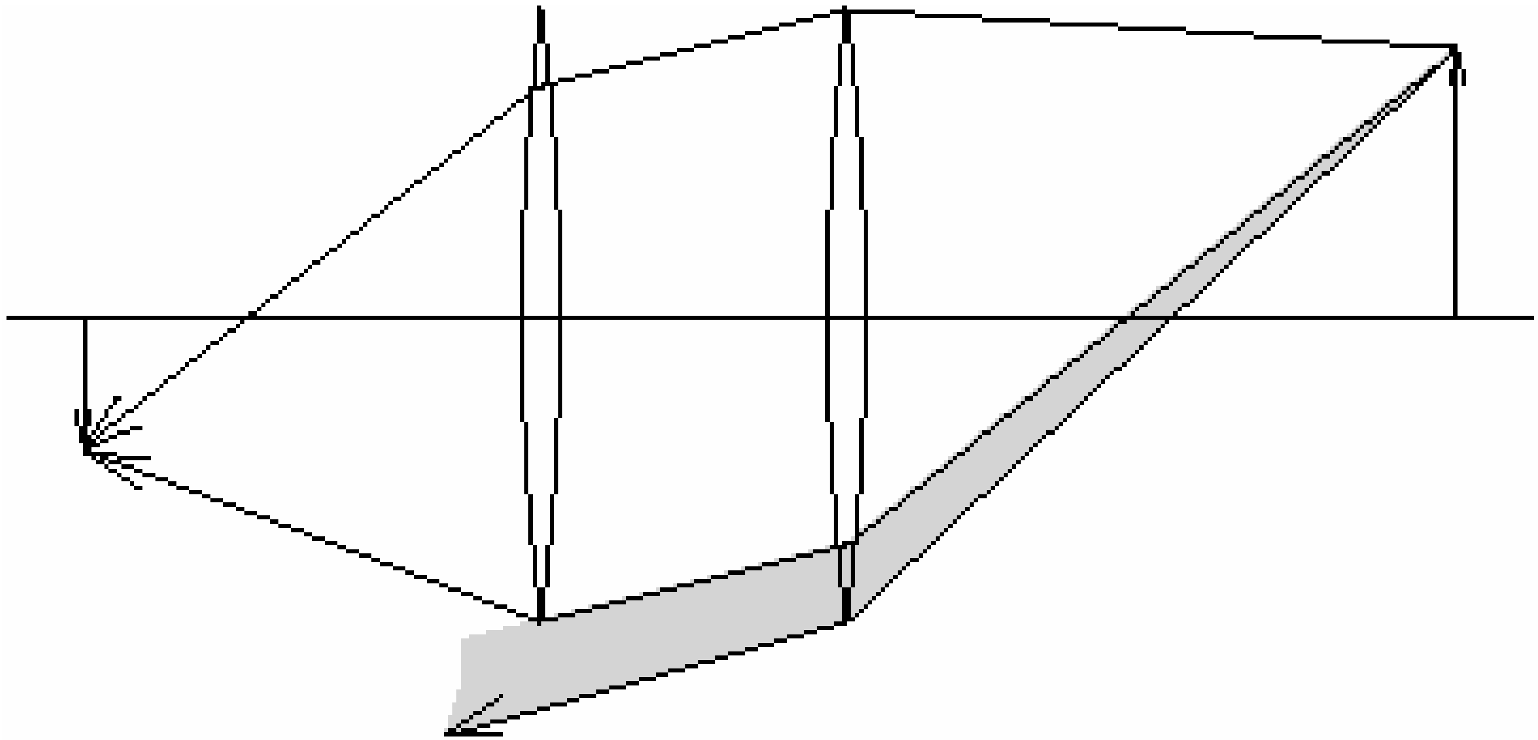
Lens systems





- A good camera lens may contain 15 elements and cost a thousand dollars
- The best modern lenses may contain aspherical elements

Vignetting



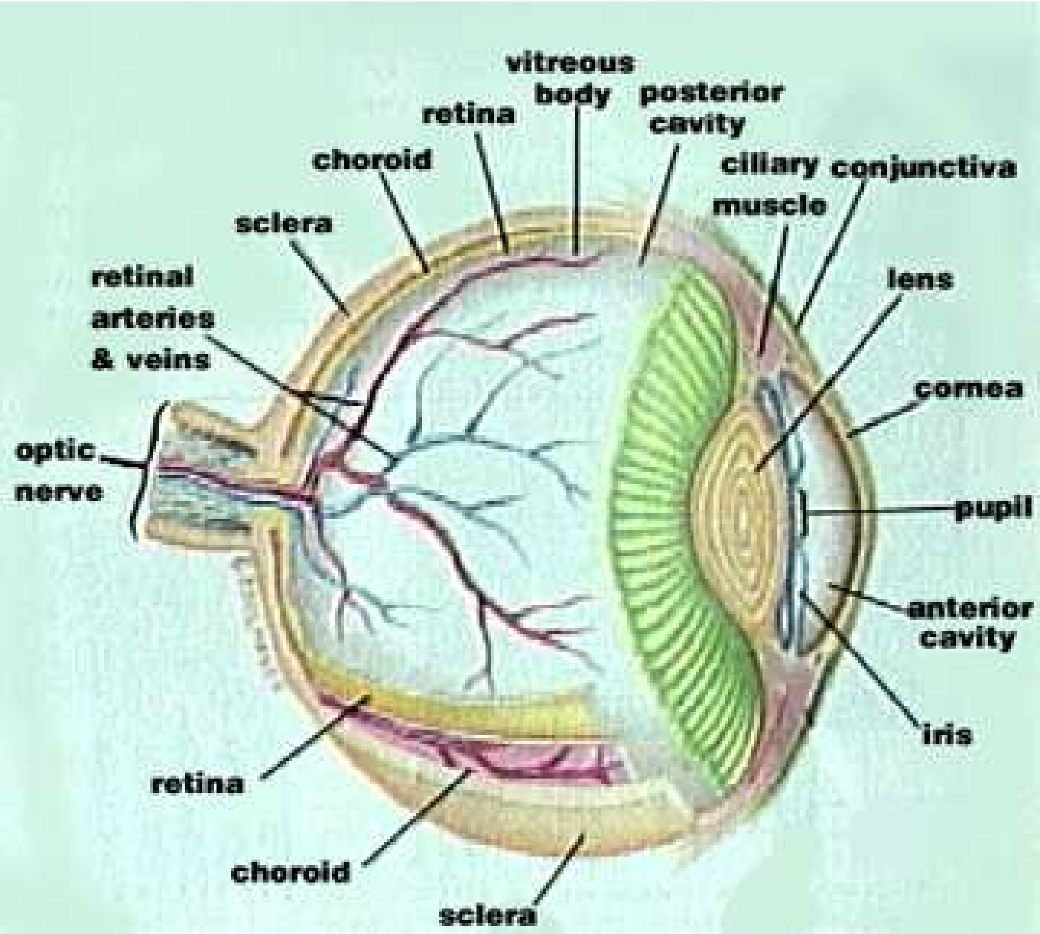
- Human vision is quite insensitive to slow change in brightness.
- However, computer vision systems may be affected.

Other (possibly annoying) phenomena

- Chromatic aberration
  - Light at different wavelengths follows different paths; hence, some wavelengths are defocussed
- Scattering at the lens surface
  - Some light entering the lens system is reflected off each surface it encounters (Fresnel's law gives details)
  - Cameras: coat the lens, interior
  - Human vision: lives with it (various scattering phenomena are visible in the human eye)
- Geometric phenomena (radial distortion, etc.)

Human Eye

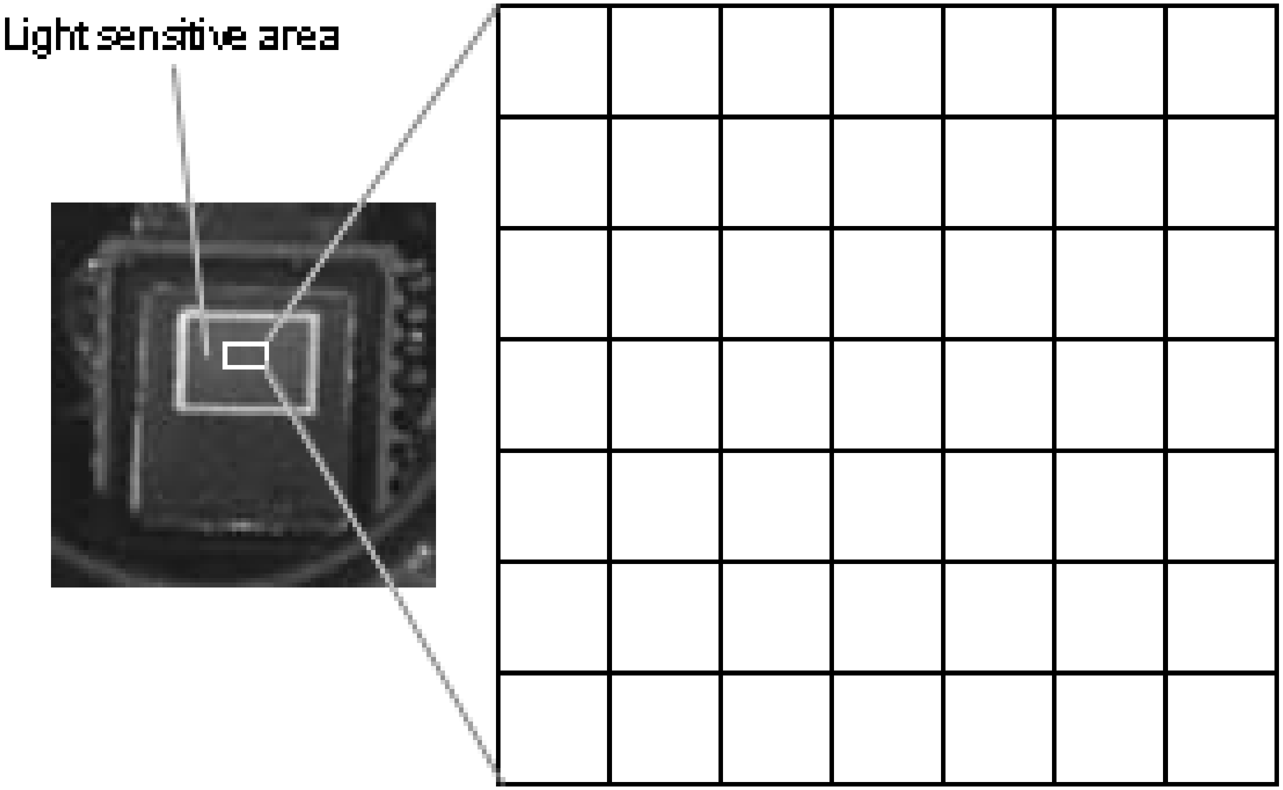
- The eye has an iris like a camera
- Focusing is done by changing shape of lens
- Retina contains cones (mostly used) and rods (for low light)
- The fovea is small region of high resolution containing mostly cones
- Optic nerve: 1 million flexible fibres



http://www.cas.vanderbilt.edu/bsci111b/eye/human-eye.jpg

Slide credit: David Jacobs

CCD Cameras



http://huizen.ddsw.nl/bewoners/maan/imaging/camera/ccd1.gif

Slide credit: David Jacobs