Uninformed Search

CPSC 322 Lecture 5

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Uninformed Search

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2 Searching





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Search

• What we want to be able to do:

- find a solution when we are not given an algorithm to solve a problem, but only a specification of what a solution looks like
- idea: search for a solution
- What we need:
 - A set of states
 - A start state
 - A goal state or set of goal states
 - or, equivalently, a goal test: a boolean function which tells us whether a given state is a goal state
 - A set of actions
 - An action function: a mapping from a state and an action to a new state

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How to search

- Start at the start state
- Consider the effect of taking different actions starting from states that have been encountered in the search so far
- Stop when a goal state is encountered

To make this more formal, we'll need to talk about graphs...

- A graph consists of
 - a set N of nodes;
 - $\bullet\,$ a set A of ordered pairs of nodes, called arcs or edges.
- Node n_2 is a neighbor of n_1 if there is an arc from n_1 to n_2 .

• i.e., if $\langle n_1, n_2 \rangle \in A$

- A path is a sequence of nodes $\langle n_0, n_1, \ldots, n_k \rangle$ such that $\langle n_{i-1}, n_i \rangle \in A$.
- Given a start node and a set of goal nodes, a solution is a path from the start node to a goal node.

Example Domain for the Delivery Robot



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Example Graph for the Delivery Robot



- Generic search algorithm: given a graph, start nodes, and goal nodes, incrementally explore paths from the start nodes.
- Maintain a frontier of paths from the start node that have been explored.
- As search proceeds, the frontier expands into the unexplored nodes until a goal node is encountered.

Problem Solving by Graph Searching



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- Maintain a frontier of paths from the start node that have been explored.
- As search proceeds, the frontier expands into the unexplored nodes until a goal node is encountered.
- The way in which the frontier is expanded defines the search strategy.









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Input: a graph,

a set of start nodes,

Boolean procedure goal(n) that tests if n is a goal node.

frontier := {\langle s \rangle : s is a start node};

while frontier is not empty:

select and remove path \langle n_0, \dots, n_k \rangle from frontier;

if goal(n_k)

return \langle n_0, \dots, n_k \rangle;

for every neighbor n of n_k

add \langle n_0, \dots, n_k, n \rangle to frontier;

end while
```

- After the algorithm returns, it can be asked for more answers and the procedure continues.
- Which value is selected from the frontier defines the search strategy.
- The *neighbor* relationship defines the graph.
- The *goal* function defines what is a solution.

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- The forward branching factor of a node is the number of arcs going out of that node
- The backward branching factor of a node is the number of arcs going into the node
- If the forward branching factor of every node is *b* and the graph is a tree, how many nodes are exactly *n* steps away from the start node?

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- The backward branching factor of a node is the number of arcs going into the node
- If the forward branching factor of every node is *b* and the graph is a tree, how many nodes are exactly *n* steps away from the start node?
 - b^n nodes.
- We'll assume that all branching factors are finite.

Completeness

• if at least one solution exists, the algorithm is guaranteed to find a solution within a finite amount of time

Time Complexity

• in terms of the maximum path length *m*, and the maximum branching factor *b*, what is the worst-case amount of time that the algorithm will take to run?

Space Complexity

• in terms of *m* and *b*, what is the worst-case amount of memory that the algorithm must use?

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- Depth-first search treats the frontier as a stack
- It always selects one of the last elements added to the frontier.

• Example:

- the frontier is $[p_1, p_2, \ldots, p_r]$
- neighbours of p_1 are $\{n_1, \ldots, n_k\}$

What happens?

- p_1 is selected, and tested for being a goal.
- Neighbours of p_1 replace p_1 at the beginning of the frontier.
- Thus, the frontier is now $[n_1, \ldots, n_k, p_2, \ldots, p_r]$.
- p_2 is only selected when all paths from p_1 have been explored.

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Illustrative Graph — Depth-first Search



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Analysis of Depth-first Search

• Is DFS complete?



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- What is the time complexity, if the maximum path length is *m* and the maximum branching factor is *b*?
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• What is the space complexity?

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 - Depth-first search isn't guaranteed to halt on infinite graphs or on graphs with cycles.
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 - The time complexity is ${\cal O}(b^m)$: must examine every node in the tree.
 - Search is unconstrained by the goal until it happens to stumble on the goal.
- What is the space complexity?
 - Space complexity is O(bm): the longest possible path is m, and for every node in that path must maintain a fringe of size b.

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• When is DFS appropriate?



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 - space is restricted
 - solutions tend to occur at the same depth in the tree
 - you know how to order nodes in the list of neighbours so that solutions will be found relatively quickly

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 - space is restricted
 - solutions tend to occur at the same depth in the tree
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- When is DFS inappropriate?
 - some paths have infinite length
 - the graph contains cycles
 - some solutions are very deep, while others are very shallow