CPSC 322 Lecture 33

April 4, 2007 Textbook §12.5



Recap

Decision Processes

Lecture Overview

- Recap
- Value of Information, Control

Sequential decision problems

- A sequential decision problem consists of a sequence of decision variables D_1, \ldots, D_n .
- Each D_i has an information set of variables pD_i , whose value will be known at the time decision D_i is made.

- What should an agent do?
 - What an agent should do at any time depends on what it will do in the future.
 - What an agent does in the future depends on what it did before.

Policies

- A policy specifies what an agent should do under each circumstance.
- A policy is a sequence $\delta_1, \dots, \delta_n$ of decision functions

$$\delta_i: dom(pD_i) \to dom(D_i).$$

This policy means that when the agent has observed $O \in dom(pD_i)$, it will do $\delta_i(O)$.

ullet The expected utility of policy δ is

$$\mathbb{E}(U|\delta) = \sum_{\omega \models \delta} P(\omega)U(\omega)$$

An optimal policy is one with the highest expected utility.



Finding the optimal policy

- Remove all variables that are not ancestors of a value node
- Create a factor for each conditional probability table and a factor for the utility.
- Sum out variables that are not parents of a decision node.
- Select a variable D that is only in a factor f with (some of) its parents.
 - this variable will be one of the decisions that is made latest
- Eliminate D by maximizing. This returns:
 - ullet the optimal decision function for D, $rg \max_D f$
 - a new factor to use in VE, $\max_D f$
- Repeat till there are no more decision nodes.
- Sum out the remaining random variables. Multiply the factors: this is the expected utility of the optimal policy.



Lecture Overview

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- 2 Value of Information, Control
- 3 Decision Processes
- 4 MDPs

Value of Information

- The value of information X for decision D is the utility of the the network with an arc from X to D minus the utility of the network without the arc.
 - The value of information is always non-negative.
 - ullet It is positive only if the agent changes its action depending on X.
- The value of information provides a bound on how much you should be prepared to pay for a sensor. How much is a better weather forecast worth?

Value of Control

- The value of control of a variable X is the value of the network when you make X a decision variable minus the value of the network when X is a random variable.
- You need to be explicit about what information is available when you control X.
 - If you control X without observing, controlling X can be worse than observing X.
 - If you keep the parents the same, the value of control is always non-negative.

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- 3 Decision Processes

Agents as Processes

Agents carry out actions:

- forever infinite horizon
- until some stopping criteria is met indefinite horizon
- finite and fixed number of steps finite horizon



Decision-theoretic Planning

What should an agent do under these different planning horizons, when

- it gets rewards (and punishments) and tries to maximize its rewards received
- actions can be noisy; the outcome of an action can't be fully predicted
- there is a model that specifies the probabilistic outcome of actions
- the world is fully observable

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- MDPs

World State

- The world state is the information such that if you knew the world state, no information about the past is relevant to the future. Markovian assumption.
- Let S_i be the state at time i

$$P(S_{t+1}|S_0, A_0, \dots, S_t, A_t) = P(S_{t+1}|S_t, A_t)$$

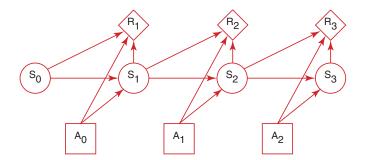
P(s'|s,a) is the probability that the agent will be in state s' immediately after doing action a in state s.

 The dynamics is stationary if the distribution is the same for each time point.

Decision Processes

Recap

 A Markov decision process augments a stationary Markov chain with actions and values:



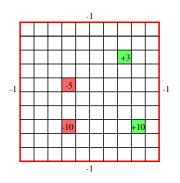
Markov Decision Processes

Recap

An MDP is defined by:

- set S of states.
- set A of actions.
- $P(S_{t+1}|S_t, A_t)$ specifies the dynamics.
- $R(S_t, A_t, S_{t+1})$ specifies the reward. The agent gets a reward at each time step (rather than just a final reward).
 - R(s, a, s') is the reward received when the agent is in state s, does action a and ends up in state s'.

Example: Simple Grid World



- Actions: up, down, left, right.
- 100 states corresponding to the positions of the robot.
- Robot goes in the commanded direction with probability 0.7, and one of the other directions with probability 0.1.
- If it crashes into an outside wall, it remains in its current position and has a reward of -1.
- Four special rewarding states; the agent gets the reward when leaving.

Decision Processes

Planning Horizons

The planning horizon is how far ahead the planner looks to make a decision.

- The robot gets flung to one of the corners at random after leaving a positive (+10 or +3) reward state.
 - the process never halts
 - infinite horizon
- The robot gets +10 or +3 entering the state, then it stays there getting no reward. These are absorbing states.
 - The robot will eventually reach the absorbing state.
 - indefinite horizon

Information Availability

What information is available when the agent decides what to do?

- fully-observable MDP the agent gets to observe S_t when deciding on action A_t .
- partially-observable MDP (POMDP) the agent has some noisy sensor of the state. It needs to remember its sensing and acting history.

We'll only consider (fully-observable) MDPs.

Value of Information. Control