

Things get sorted

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Sorting

- We've looked at Arrays, ArrayLists and LinkedLists
- We're about to look at Sets
- Before we do, let's consider the case where we want to *sort* an Array or a List...

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Sorting

- The Arrays class and Collections class in java supply sorting algorithms for arrays and collections
- This is straightforward for cases like sorting an array of integers:

```
int[] intArr = { 5, 4, 3, 2, 1 };  
Arrays.sort(intArr);  
for (int num : intArr) {  
    System.out.println(num);  
}
```

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Sorting Objects

- Seems easy enough, but...
- What if we want to sort an array of Employees, or Bikes, or Accounts?
- Sorting integers is easy, but how does Java know how to sort these complex objects?
- We have to *tell Java* how to sort them

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Comparable

- We do that by having our class implement the Comparable interface
- The Comparable interface lists a single method compareTo()
- We have our class implement that method in a way that tells Java how objects of the class should be sorted

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The Comparable Interface

- The Comparable interface is declared as follows:

```
public interface Comparable<T> {  
    int compareTo(T other)  
}
```

- the integer returned by `a.compareTo(b)` must adhere to the following convention:
 - negative if `a < b`
 - zero if `a.equals(b)`
 - positive if `a > b`

- `compareTo` defines the *natural ordering* for the class

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Golfers

- Let's say we have a class Golfer
- It might have attributes and methods like this:

```
public class Golfer {  
    private int handicap;  
    private int bestscore;  
    private String name;  
  
    public Golfer(int hand, int best, String name)  
    {  
        bestscore = best;  
        handicap = hand;  
        this.name = name;  
    }  
}
```

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continued

Golfer

```
public int getHand()  
{  
    return handicap;  
}  
  
public int getBest()  
{  
    return bestscore;  
}  
  
public String getName()  
{  
    return name;  
}
```

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Golfer

- We want to create a sorted Array of Golfers, and we want them sorted by handicap
- We need to tell Java that they should be sorted this way

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Golfers

- Let's say we have a class Golfer
- It might have attributes and methods like this:

```
public class Golfer implements Comparable<Golfer>{  
    private int handicap;  
    private int bestscore;  
    private String name;  
  
    public Golfer(int hand, int best, String name)  
    {  
        bestscore = best;  
        handicap = hand;  
        this.name = name;  
    }  
}
```

We make our class
implement
Comparable

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continued

Golfers

- Let's say we have a class Golfer
- It might have attributes and methods like this:

```
public class Golfer implements Comparable<Golfer>{  
    private int handicap;  
    private int bestscore;  
    private String name;  
  
    public Golfer(int hand, int best, String name)  
    {  
        bestscore = best;  
        handicap = hand;  
        this.name = name;  
    }  
}
```

And if we implement
Comparable, then we
need to define the
compareTo method

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continued

Comparing Golfers

- We add this method to our Golfer class

```
public int compareTo(Golfer g)  
{  
    int ohand = g.getHand();  
    if (this.handicap < ohand)  
    {  
        return -1;  
    }  
    else if (this.handicap == ohand)  
    {  
        return 0;  
    }  
    else return 1;  
}
```

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Comparing Golfers

- We add this method to our Golfer class

```
public int compareTo(Golfer g)
{
    int ohand = g.getHand();
    if (this.handicap < ohand)
    {
        return -1;
    }
    else if (this.handicap == ohand)
    {
        return 0;
    }
    else return 1;
}
```

So when compareTo gets called on a Golfer object, with another Golfer passed as a parameter, we compare their handicaps and return -1, 0 or 1 indicating how they should be sorted

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Comparing Golfers

- We add this method to our Golfer class

```
public int compareTo(Golfer g)
{
    int ohand = g.getHand();
    if (this.handicap < ohand)
    {
        return -1;
    }
    else if (this.handicap == ohand)
    {
        return 0;
    }
    else return 1;
}
```

Now when we put a bunch of Golfers in an array and call Arrays.sort(), Java will use the compareTo method to put each in its correct place

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Comparing Golfers

```
Golfer[] golfBuddies = new Golfer[3];
Golfer bob = new Golfer(9, 85, "bob");
Golfer jane = new Golfer(5, 76, "jane");
Golfer jim = new Golfer(15, 105, "jim");
golfBuddies[0] = bob;
golfBuddies[1] = jane;
golfBuddies[2] = jim;
Arrays.sort(golfBuddies);
for (Golfer g: golfBuddies)
{
    System.out.println(g.getName());
}
```

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Comparing Golfers

```
Golfer[] golfBuddies = new Golfer[3];
Golfer bob = new Golfer(9, 85, "bob");
Golfer jane = new Golfer(5, 76, "jane");
Golfer jim = new Golfer(15, 105, "jim");
golfBuddies[0] = bob;
golfBuddies[1] = jane;
golfBuddies[2] = jim;
Arrays.sort(golfBuddies);
for (Golfer g: golfBuddies)
{
    System.out.println(g.getName());
}
```

>
jane
bob
jim

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Comparing Golfers

- How could we change the compareTo method to rank them in reverse order?

```
public int compareTo(Golfer g)
{
    int ohand = g.getHand();
    if (this.handicap < ohand)
    {
        return -1;
    }
    else if (this.handicap == ohand)
    {
        return 0;
    }
    else
    {
        return 1;
    }
}
```

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Comparing Golfers

- How could we change the compareTo method to rank them in reverse order?

```
public int compareTo(Golfer g)
{
    int ohand = g.getHand();
    if (this.handicap > ohand) ← We could change the if statement
    {
        return -1;
    }
    else if (this.handicap == ohand)
    {
        return 0;
    }
    else
    {
        return 1;
    }
}
```

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Comparing Golfers

- How could we change the compareTo method to rank them in reverse order?

```
public int compareTo(Golfer g)
{
    int ohand = g.getHand();
    if (this.handicap < ohand)
    {
        return 1;
    }
    else if (this.handicap == ohand)
    {
        return 0;
    }
    else
    {
        return -1;
    }
}
```

Or instead we could change the return values

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Comparing Golfers

- How could we change the compareTo method to rank them in reverse order?

```
public int compareTo(Golfer g)
{
    int ohand = g.getHand();
    if (this.handicap < ohand)
    {
        return 1;
    }
    else if (this.handicap == ohand)
    {
        return 0;
    }
    else
    {
        return -1;
    }
}
```

Either way:
>
jim
bob
jane

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compareTo

- When `a.compareTo(b)` is called, the return values mean:
 - -1 a comes before b
 - 1 b comes before a
 - 0 they are equal

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Comparing Golfers

- What if we decided we want to rank Golfers by their best score instead?
- We could simply define `compareTo()` differently

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Comparing Golfers

```
public int compareTo(Golfer g)
{
    int obest = g.getBest();
    if (this.best < obest)
    {
        return -1;
    }
    else if (this.best == obest)
    {
        return 0;
    }
    else return 1;
}
```

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Implementing compareTo

- So if we decide we want to sort objects based on a different attribute, do we need to rewrite `compareTo`?
- Some objects might have a single natural ordering, but others may have many attributes and sometimes we want to sort by one and sometimes by another
- Also, what if we want to sort objects of a class defined by someone else? In that case, we can't go in and redefine their `compareTo` method

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Comparators

- There is an alternative to implementing Comparable and its compareTo method
- We can use *Comparators*

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The Comparator Interface

- A comparator has to implement:

```
public interface Comparator<T> {  
    int compare(T object1, T object2);  
}
```

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The Comparator Interface

- The return value for this method
 - is defined in the same way as for the compareTo method of the Comparable interface:

compare(a,b) is like *a.compareTo(b)*

- We may define many comparators for a class if we need to order objects of that type in different ways.

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Golf Comparators

- We could define two different Golfer comparators:

```
public class HandicapComparator implements  
    Comparator<Golfer>{
```

```
    public int compare(Golfer g1, Golfer g2)
```

```
    {
```

```
        return g1.getHand() - g2.getHand();
```

```
    }
```

```
}
```

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Golf Comparators

- And other for best scores:

```
public class BestScoreComparator implements
Comparator<Golfer>{

public int compare(Golfer g1, Golfer g2)
{
return g1.getBest() - g2.getBest();
}
}
```

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Golf Comparators

- And other for best scores:

```
public class BestScoreComparator implements
Comparator<Golfer>{

public int compare(Golfer g1, Golfer g2)
{
return g1.getBest() - g2.getBest();
}
}
```

What's going on here? Don't we need to return -1, 0 or 1? This isn't guaranteed to do so.

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Golf Comparators

- And other for best scores:

```
public class BestScoreComparator implements
Comparator<Golfer>{

public int compare(Golfer g1, Golfer g2)
{
return g1.getBest() - g2.getBest();
}
}
```

Actually, no. We just need to return a negative value, positive value, or zero. Often people use -1, 0 and 1, but not always. For that reason, be careful doing something like `if (this.compareTo(g1) == -1)` because it may be a different negative value

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Using Comparators

- So how do we use these Comparator classes?
- Methods such as `sort()` are overloaded
 - If the class implements `Comparable` and has a `compareTo` method, we just call `sort()` on our array or collection
 - There is also a version of `sort()` that takes a `Comparator` as a second parameter
- We can take one of those two approaches
- Note: if the class implements `Comparable` **and** we pass a `Comparator`, it is the `Comparator` that gets used for sorting

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Using Comparators

```
Golfer[] golfBuddies = new Golfer[3];
Golfer bob = new Golfer(9, 85, "bob");
Golfer jane = new Golfer(5, 76, "jane");
Golfer jim = new Golfer(15, 105, "jim");
golfBuddies[0] = bob;
golfBuddies[1] = jane;
golfBuddies[2] = jim;
Arrays.sort(golfBuddies, new HandicapComparator());
for (Golfer g: golfBuddies)
{
    System.out.println(g.getName());
}
```

Now we can just provide whatever
Comparator we want

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In-Class Exercise I

- Change this class Worker so that it implements Comparable

```
public class Worker {
    private int id;
    private int age;

    public Worker(int anID, int anAge)
    {
        this.id = anID;
        this.age = anAge;
    }
}
```

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In-Class Exercise I

- Now write two Comparator classes to give us more flexibility on how we sort Workers

```
public class Worker {
    private int id;
    private int age;

    public Worker(int anID, int anAge)
    {
        this.id = anID;
        this.age = anAge;
    }
}
```

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Sorting

- We'll come back to Comparable and Comparator shortly, and in more detail, when we talk about Sets

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The Set Interface

You will be expected to:

- program to the generic Set and SortedSet interfaces including read and use the API's
- justify the use of a set vs a list for a given problem
- compare and contrast the HashSet and TreeSet classes (benefits of using each, basic run time analysis)
- design and implement a class in such a way that it can be used with the Java collections framework
 - overrides equals and hashCode
 - implements the generic Comparable and Comparator interfaces to account for multiple sorting criteria

Reading:

- 2nd Ed: 19.8, 21.1, briefly: 21.3, 21.4
- 3rd/4th Ed: 14.8, 16.1, briefly: 16.3, 16.4

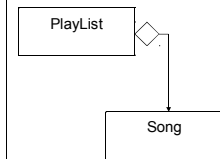
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Using a Set

- A playlist is a set of songs:

Chris's Play List
Meet Me Halfway
Jingle Bells
21 Guns
Thriller



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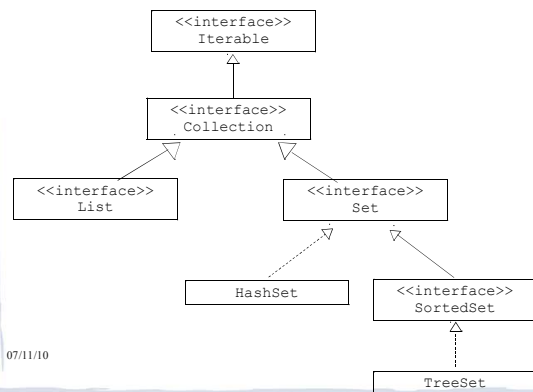
Using a Set (continued)

- In a List,
 - Each object has a position
 - We can put the same object in the list multiple times
- Sometimes, we need the functionality of a mathematical set
 - No duplicates in the set
 - Members do not have a position in the set
- For example...
 - MenuItems that appear in the Menu of a restaurant
 - Songs that appear on a Playlist
 - Student enrolled in a Course
- In these cases we use a Set not a List

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The set interface



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Methods of the Set interface

- Note that the `Set` interface extends the `Collection` interface. An implementation of `Set` therefore supports the methods defined in the `Collection` interface:
 - `add(o)` – add a specified element to the set (if not already a member)
 - `remove(o)` – remove the specified element from the set
 - `contains(o)` – is the specified element in the set?
 - etc.
- Note that the `add` method:

```
public boolean add( E item );
```

adds the item only if it isn't already in the set. The method returns true if the item is added and false if it's already in the set.
- Similarly the `addAll` method does not add duplicates.

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Methods of the Set interface

- We can use these methods to define known set operations:
 - `c1.containsAll(c2)` - true if `c2` is a subset of `c1`
 - `c1.addAll(c2)` - `c1` becomes union of `c1` and `c2`
 - `c1.retainAll(c2)` - `c1` becomes intersection of `c1` and `c2`
 - `c1.removeAll(c2)` - `c1` becomes set difference of `c1` and `c2`

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Using Sets

- Since `Set` is specified as an interface, to use it we have to pick a particular implementation (e.g., `HashSet`, or `TreeSet`)
- Example:

```
public class Playlist
{
    private Set<Song> songs;

    public Playlist()
    {
        songs= new HashSet< Song >();
    }
}
```

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The HashSet implementation

- The `HashSet` implementation provides an efficient implementation of the `Set` interface that allows us to add or remove an item or check if the set contains an item in $O(1)$ time provided certain conditions are met (more later).
- That is, if

```
Set<...> s = new HashSet<...>();
```

 - `s.add(o)` is $O(1)$
 - `s.remove(o)` is $O(1)$
 - `s.contains(o)` is $O(1)$

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The HashSet implementation

- As mentioned, certain conditions must be met if we are to add, remove or determine if the set contains an item in $O(1)$ time.
- To understand these conditions, we must have a basic understanding of how the hash set works.
- A hash set uses a **hash table** as the underlying structure in which data is stored.
- A hash table is an array of linked lists...

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The HashSet implementation

- We add elements to the table using a hash code, an integer that represents the object
- A hash set maintains a list of groups.
- All members of the group at position i have a hashCode of i .
- We'll talk more in a moment about where these hashCodes come from
- Let's see an example....

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Hash Table Example

- Suppose we want to add integers to a hash table using the following hash code:

```
hashCode = value%10;
```

- What does the table look like after inserting:

243556,
329394,
3348,
436,
3234,
424

0	
1	
2	
3	
4	
5	
6	
7	
8	
9	

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Hash Table Example

- Suppose we want to add integers to a hash table using the following hash code:

```
hashCode = value%10;
```

- What does the table look like after inserting:

243556,
329394,
3348,
436,
3234,
424

0	
1	
2	
3	
4	329394, 3234, 424
5	
6	243556, 436
7	
8	3348
9	

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Hash Tables

- Hashing can be used to find elements in a data structure quickly without making a linear search
- A *hash table* can be used to implement sets and maps
- A *hash function* computes an integer value (called the *hash code*) from an object
- A good hash function minimizes *collisions* – identical hash codes for different objects
- To compute the hash code of object *x*:

```
int h = x.hashCode();
```

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Collisions

- Notice in the previous example that we had quite a few collisions – items that are stored in the same location (or bucket)
- We want a good hash code that will reduce these collisions

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Sample Strings and Their Hash Codes

String	Hash Code
"Adam"	2035631
"Eve"	700068
"Harry"	69496448
"Jim"	74478
"Joe"	74656
"Juliet"	-2065036585
"Katherine"	2079199209
"Sue"	83491

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Sample Strings and Their Hash Codes

String	Hash Code
"Adam"	2035631
"Eve"	700068
"Harry"	69496448
"Jim"	74478
"Joe"	74656
"Juliet"	-2065036585
"Katherine"	2079199209
"Sue"	83491

Note: the String class has an already defined hashCode method we can use

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Simplistic Implementation of a Hash Table

- To implement
 - *Generate hash codes for objects*
 - *Make an array*
 - *Insert each object at the location of its hash code*
- To test if an object is contained in the set
 - *Compute its hash code*
 - *Check if the array position with that hash code is already occupied*

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Problems with Simplistic Implementation

- It is not possible to allocate an array that is large enough to hold all possible integer index positions
- It is possible for two different objects to have the same hash code

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Solutions

- Pick a reasonable array size and reduce the hash codes to fall inside the array

```
int h = x.hashCode();  
if (h < 0) h = -h;  
h = h % size;
```

- When elements have the same hash code:
 - *Use a node sequence to store multiple objects in the same array position*
 - *These node sequences are called buckets*

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Buckets

- So instead of a single object being stored at each point in the array, we have a LinkedList of objects at each point
- This allows for the possibility that some different objects will have the same hash code by chance and thus be stored at the same array index
- We say they are in the same bucket

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Hash Table with Buckets to Store Elements with Same Hash Code

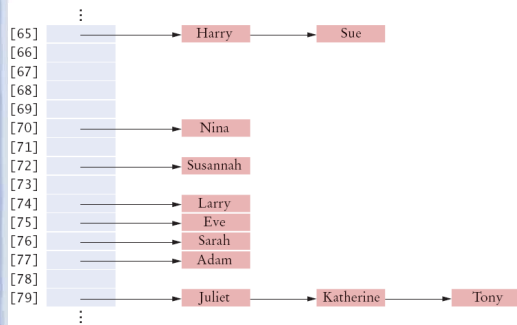


Figure 6 A Hash Table with Buckets to Store Elements with the Same Hash Code

Algorithm for Finding an Object x in a Hash Table

1. Get the index h into the hash table
 - Compute the hash code
 - Reduce it modulo the table size
2. Iterate through the elements of the bucket at position h
 - For each element of the bucket, check whether it is equal to x
3. If a match is found among the elements of that bucket, then x is in the set
 - Otherwise, x is not in the set

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Hash Tables

- A hash table can be implemented as an array of buckets
- Buckets are sequences of nodes that hold elements with the same hash code
- If there are few collisions, then adding, locating, and removing hash table elements takes constant time
 - Big-Oh notation: $O(1)$
- For this algorithm to be effective, the bucket sizes must be small
- The table size should be a prime number larger than the expected number of elements
 - An excess capacity of 30% is typically recommended

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Hash Tables

- Adding an element: simple extension of the algorithm for finding an object
 - Compute the hash code to locate the bucket in which the element should be inserted
 - Try finding the object in that bucket
 - If it is already present, do nothing; otherwise, insert it
- Removing an element is equally simple
 - Compute the hash code to locate the bucket in which the element should be inserted
 - Try finding the object in that bucket
 - If it is present, remove it; otherwise, do nothing
- If there are few collisions, adding or removing takes $O(1)$ time

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The `HashSet` implementation

- In a `HashSet` the operations are performed as following:

`add(o)`

- compute the hashCode of `o`, say `i`
- add `o` in the `i`th group

`remove(o)`

- compute the hashCode of `o`, say `i`
- search the `i`th group and remove `o`

`contains(o)`

- compute the hashCode of `o`, say `i`
- search the `i`th group to find `o`

- If each group is small (and of constant size) each of the above operations is $O(1)$.

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The `HashSet` Implementation

- What makes these operations so efficient?
 - Take `add()` for example
- Rather than iterating over a collection and checking at each step whether the object already exists, we just compute the hashCode and check that index in the array
- We then check whether the object exists in that bucket
- If we have a good hashCode and hash table, there will be few collisions, meaning few items to search through in the bucket
- If we can get close to 1 item per bucket, these operations will be $O(1)$ – constant time

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Where do hash codes come from?

- Each Java class inherits a `hashCode()` method from the Java class `Object`
 - when invoked, `hashCode()` returns an integer that represents the object
 - a class' `hashCode()` is usually defined in terms of the hash codes of its attributes
 - if two objects are equal according to `equals()`, they must have the same hash code
 - objects with the same hash code are not necessarily equal

- It would be nice to rely upon the Java `Object`'s class definition of `hashCode()` but you can't if you override `equals()` because two instances of an object that are equal according to `equals()` may not return the same `hashCode()` unless you ensure they do!

The rule is then:

"If you override `equals()` you should always override `hashCode()`"

- See page 36 of <http://java.sun.com/developer/Books/effectivejava/Chapter3.pdf> for a complete description

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Default `hashCode()` and `equals()`

- If you rely on the default inherited `equals()` and `hashCode()`, you are okay in the sense that they both rely on the memory location of the object and are therefore consistent with one another
- But then you are left with a very restrictive definition of `equals()` which might not be what you want

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How do you write a good hashCode()

- Writing a fantastic hashCode() method for a class is hard
 - The kind of thing people write PhD theses about
- Writing a decent hashCode() method for a class is straightforward
 - Page 38 of <http://java.sun.com/developer/Books/effectivejava/Chapter3.pdf> provides a recipe.
 - Start with a non-zero value (preferably a prime number, like 11, 17, etc.) in the result value
 - Pick another prime number, say 37, as a multiplier
 - For each attribute that is taken into account in the equals() method
 - if attribute is of a primitive type (i.e. an integer, float, etc.),
result = 37 * result + attribute's value casted to an integer
 - if attribute is an object,
result = 37 * result + attribute.hashCode()
 - and so on...

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Song Example

```
public class Song{
    private String title;
    private Artist artist;
    private int lengthInSeconds;
    private Album album;
    private int playCount;
```

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Song Example (cont.)

```
public boolean equals( Object other ){
    if (other == null)
        return false;
    if( getClass() != other.getClass() )
        return false;
    Song otherItem = (Song) other;

    return(title.equals(other.title) &&
        artist.equals(other.artist));
}
```

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Song Example (cont.)

```
public int hashCode() {
    int result = 17;
    final int MULT = 31;
    result = MULT*result + title.hashCode();
    result = MULT*result + artist.hashCode();
    return result;
}
...
} //end Song
```

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Computing Hash Codes

- A hash function computes an integer hash code from an object
- Choose a hash function so that different objects are likely to have different hash codes.
- Bad choice for hash function for a string
 - *Adding the unicode values of the characters in the string*

```
int h = 0;
for (int i = 0; i < s.length(); i++)
    h = h + s.charAt(i);
```

- *Because permutations ("eat" and "tea") would have the same hash code*

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Computing Hash Codes

- Hash function for a string s from standard library

```
final int HASH_MULTIPLIER = 31;
int h = 0;
for (int i = 0; i < s.length(); i++)
    h = HASH_MULTIPLIER * h + s.charAt(i)
```

- For example, the hash code of "eat" is

```
31 * (31 * 'e' + 'a') + 't' = 100184
```

- The hash code of "tea" is quite different, namely

```
31 * (31 * 't' + 'e') + 'a' = 114704
```

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A hashCode Method for the Coin Class

- There are two instance fields: `String` coin name and double coin value
- Use `String`'s `hashCode` method to get a hash code for the name
- To compute a hash code for a floating-point number:
 - *Wrap the number into a `Double` object*
 - *Then use `Double`'s `hashCode` method*
- Combine the two hash codes using a prime number as the `HASH_MULTIPLIER`

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A hashCode Method for the Coin Class

```
class Coin
{
    public int hashCode()
    {
        int h1 = name.hashCode();
        int h2 = new Double(value).hashCode();
        final int HASH_MULTIPLIER = 29;
        int h = HASH_MULTIPLIER * h1 + h2; return h;
    }
    . . .
}
```

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Creating Hash Codes for your Classes

Use a prime number as the `HASH_MULTIPLIER`

Compute the hash codes of each instance field

For an integer instance field just use the field value

Combine the hash codes

```
int h = HASH_MULTIPLIER * h1 + h2;
h = HASH_MULTIPLIER * h + h3;
h = HASH_MULTIPLIER * h + h4;
. . .
return h;
```

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Creating Hash Codes for your Classes

- Your `hashCode` method must be compatible with the `equals` method
 - if `x.equals(y)` then `x.hashCode() == y.hashCode()`
- You get into trouble if your class defines an `equals` method but not a `hashCode` method
 - If we forget to define `hashCode` method for `Coin` it inherits the method from `Object` superclass
 - That method computes a hash code from the memory location of the object
 - Effect: any two objects are very likely to have a different hash code

```
Coin coin1 = new Coin(0.25, "quarter");
Coin coin2 = new Coin(0.25, "quarter");
```

- In general, define either both `hashCode` and `equals` methods or neither

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The `SortedSet` Interface

- Allows the user to retrieve objects from the set in sorted order
- To sort a collection, the objects within the collection must be comparable:
 - the corresponding class must implement either the `Comparable` interface or the `Comparator` interface.

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The `Comparable` Interface

- The `Comparable` interface is declared as follows:

```
public interface Comparable<T> {
    int compareTo(T other)
}
```

- the integer returned by `a.compareTo(b)` must adhere to the following convention:
 - negative if `a < b`
 - zero if `a.equals(b)`
 - positive if `a > b`

- `compareTo` defines the **natural ordering** for the class

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Implementing `compareTo`

- Rules to follow when you implement this method in a class C:
 - C must implement `Comparable<C>`
 - must be asymmetric
 - `a.compareTo(b)` and `b.compareTo(a)` must both equal 0 or have opposite signs
 - must be transitive
 - if `a.compareTo(b) < 0` and `b.compareTo(c) < 0` then `a.compareTo(c) < 0`
 - must be consistent with `equals()`
 - `a.equals(b)` is true iff `a.compareTo(b)` is zero and `b.compareTo(a)` is zero

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The `Comparator` Interface

- Some classes may not have a single natural ordering
 - employees may be ordered by name or by salary or...
- A comparator is an object that defines (encapsulates) one ordering for a class
- A comparator has to implement:

```
public interface Comparator<T> {  
    int compare(T object1, T object2);  
}
```

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The `Comparator` Interface

- The return value for this method
 - is defined in the same way as for the `compareTo` method of the `Comparable` interface:

`compare(a,b)` is like `a.compareTo(b)`

- We may define many comparators for a class if we need to order objects of that type in different ways.

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Example

- Create a `Comparator` that compares `Accounts` by id numbers.

```
public class AccountIdComparator  
    implements Comparator<Account>  
{  
    public int compare( Account ac1, Account ac2 )  
    {  
        return (ac1.getId() - ac2.getId() );  
    }  
}
```

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The SortedSet Interface

```
public interface SortedSet<E> extends Set<E>
{
    // Views on the sorted set
    SortedSet<E> subSet(E from, E to);
    SortedSet<E> headSet(E toElement);
    SortedSet<E> tailSet(E fromElement);

    // Endpoints
    E first();
    E last();

    // Comparator access
    Comparator<? super E> comparator();
}
```

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The SortedSet Interface

- Like Set but keeps elements in ascending order according to
 - the *natural order* defined by the `compareTo` method of `Comparable`, or
 - the `compare` method of a `Comparator`
- Iterator will traverse elements in the defined order
- Array produced by `toArray` methods is sorted
- Additional operations:
 - `first()` and `last()` return min and max elements in set
 - `comparator()` returns the `Comparator` used to sort the set, or null if the *natural order* is used

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The TreeSet Class

- The `TreeSet` class implements the `SortedSet` interface. It has the following constructors (among others):

```
public TreeSet()
// orders the elements according to their
// natural order

public TreeSet( Comparator< ? super E > c )
// orders the elements according to the
// comparator c
```

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The TreeSet Class

- Note the use of the bounded wildcard:
 - `Comparator< ? super E > c`
- This indicates that the `Comparator` must compare types that are supertypes of `E` (including `E` itself).
- For example, if `SavingsAccount` is a subclass of `Account` and `BalanceComparator` implements the `Comparator<Account>` interface, then we can create the following `TreeSet` of `SavingsAccount` objects:

```
TreeSet<SavingsAccount> acctS
= new TreeSet<SavingsAccount>(
    new BalanceComparator() );
```

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TreeSet - Time Complexity

- The add, remove and contains methods all have a guaranteed $O(\log N)$ time complexity.
- So these operations on a `TreeSet` are less efficient than for a `HashSet` (assuming a good `hashCode()` implementation) but we have to remember that the `TreeSet` maintains the data in sorted order.

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TreeSet vs. HashSet

- If you don't care about sorting but just want efficient `add()`, `remove()` and `contains()` operations, the question of which `Set` to use depends on how confident you are in your hash code method
- If you have a good hash code, there will be few collisions, which means few objects in each bucket, which means less to search through

07/11/10 Otherwise, you might want to use a `TreeSet`

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Using TreeSet

- Now we can do this:

```
Set<Golfer> gSet = new TreeSet<Golfer>();
gSet.add(bob);
gSet.add(jane);
gSet.add(jim);
Iterator<Golfer> itr = gSet.iterator();
while (itr.hasNext())
{
    System.out.println(itr.next().getName());
}
```

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Using TreeSet

- Or we can supply a `Comparator`

```
Set<Golfer> gSet = new TreeSet<Golfer>(new
HandicapComparator());
gSet.add(bob);
gSet.add(jane);
gSet.add(jim);
Iterator<Golfer> itr = gSet.iterator();
while (itr.hasNext())
{
    System.out.println(itr.next().getName());
}
```

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Using TreeSet

- A different Comparator if we choose...

```
Set<Golfer> gSet = new TreeSet<Golfer>(new  
BestScoreComparator());  
gSet.add(bob);  
gSet.add(jane);  
gSet.add(jim);  
Iterator<Golfer> itr = gSet.iterator();  
while (itr.hasNext())  
{  
System.out.println(itr.next().getName());  
}
```

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Using TreeSet

- Now Java will use either the compareTo() method if we implement Comparable, or the compare() method if we use Comparators, and will keep our items nicely sorted
- Whenever we add something, Java will determine where it belongs by calling those methods
- Note: if we don't supply a Comparator and our class doesn't implement Comparable, we will get an error. We need one or the other.

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Exercises

- More Exercises:
 - 2nd Ed: P19.12, P21.1, P21.11 (but use HashSet<Integer> rather than their IntSet class)
 - 3rd Ed: P14.12, P16.1, P16.12 (but use HashSet<Integer> rather than their IntSet class)

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In-Class Exercise II

- Write the equals() and hashCode() methods for our Golfer class

```
public class Golfer {  
private int handicap;  
private int bestscore;  
private String name;  
  
public Golfer(int hand, int best, String name)  
{  
bestscore = best;  
handicap = hand;  
this.name = name;  
}
```

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Learning Goals Review

You will be expected to:

- program to the generic Set and SortedSet interfaces including read and use the API's
- justify the use of a set vs a list for a given problem
- compare and contrast the HashSet and TreeSet classes (benefits of using each, basic run time analysis)
- design and implement a class in such a way that it can be used with the Java collections framework
 - overrides equals and hashCode
 - implements the generic Comparable and Comparator interfaces to account for multiple sorting criteria