

Time Complexity of Algorithms

You are expected to:

- use big-O notation to categorize an algorithm as constant, linear, quadratic, logarithmic and exponential time
- given two or more algorithms, rank them in terms of their time efficiency

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Complexity of Algorithms

- In the coming lectures, we'll be discussing different implementations of collections and comparing them with respect to certain operations.
- We need to have a good way to define the performance of an algorithm (or a piece of code).
- In this section, we examine a means of analyzing the performance of an algorithm. Usually we are interested in the algorithm's
 - *time complexity*: time taken for an algorithm to run
 - *space complexity*: amount of memory required by it
- In this course we mainly interested in time complexity .

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Time Complexity

- One approach to determining an algorithm's *time complexity* would be to count the number of CPU cycles (or CPU time) it takes the algorithm to perform its operation
 - tedious and not a very practical approach
 - depends on the machine
 - Instead we will count the number of *simple statements* (or *steps*) which are executed by the algorithm for a given input value n (time will be a function of n).
 - By *simple statement* we mean a statement whose running time does not depend on n :
 - an assignment (without function calls)
 - a comparison between variables, etc.
- For instance, a loop that executes n times would contribute n times the number of steps of the body

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Big-O Notation

- We are not interested in an exact count of steps. Instead we want to know how fast the time grows as n grows. So, we use the following approximation
- **Definition:** Let T and f be a functions of n . We say that T is $O(f(n))$ (pronounced "big-O $f(n)$ " or "O $f(n)$ ") if:
$$T(n) \leq c f(n) \quad \text{for any } n > n_0$$
where c and n_0 are constants.
- **Example:** Suppose that T is the time taken for an algorithm to sort an array of length n and that:
$$T(n) \leq c n^2$$
for all n then we say that the algorithm is $O(n^2)$.

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Example 1

```
int count = 0;
int sum = 0;
while( count < N )
{
    sum += count;
    count++;
}
System.out.print( " The sum is : " );
System.out.println( sum );
```

- The time complexity of it depends on N.
- So
$$T(N) = 2 + (3)N + 2 = 4 + 3N$$
- and
$$T(N) \leq 4N + 3N \leq 7N \leq c N \quad (c=7)$$
- Therefore T(N) is O(n)

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Linear Algorithms

- Algorithms like the previous one are called "**linear algorithms**"
- This means that the time taken to execute the algorithm $T(n)$ for large values of n is $O(n)$
- It also means that the time for the algorithm grows linearly as n grows
- Let's suppose that we double n . How does this affect the time taken to execute the algorithm?

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Example 2

```
int count = 0;
int sum = 0;
while( count < N )
{
    int index = 0;
    while( index < N )
    {
        sum += index * count;
        index++;
    }
    count++;
}
```

- $T(N) = 2 + N(2 + N(3) + 1) = 2 + N(3N + 3) = 3N^2 + 3N + 2$
- Then
$$T(N) \leq 3N^2 + 3N^2 + 2N^2$$
or
$$T(N) \leq 8N^2$$
- Therefore: T(N) is $O(N^2)$

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Quadratic Algorithms and More

- Algorithms like the previous one are called "**quadratic algorithms**"
- This means that the time taken to execute the algorithm $T(n)$ for large values of n is $O(n^2)$
- It also means that the time for the algorithm grows by n^2 as n grows
- In general we are interested in the following algorithm types:

<u>Algorithm Type</u>	<u>T(n)</u>
Constant	$O(1)$
Linear	$O(n)$
Logarithmic	$O(\log n)$
Polynomial	$O(n^k)$ where k is an int constant
Exponential	$O(k^n)$ where k is an int constant

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Complexity Example (Sorting)

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Selection Sort

- Sorts an array by repeatedly finding the smallest element of the unsorted tail region and moving it to the front
- Slow when run on large data sets
- Example: sorting an array of integers

11	9	17	5	12
----	---	----	---	----

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Sorting an Array of Integers

- Find the smallest and swap it with the first element

5	9	17	11	12
---	---	----	----	----

- Find the next smallest. It is already in the correct place

5	9	17	11	12
---	---	----	----	----

- Find the next smallest and swap it with first element of unsorted portion

5	9	11	17	12
---	---	----	----	----

- Repeat

5	9	11	12	17
---	---	----	----	----

- When the unsorted portion is of length 1, we are done

5	9	11	12	17
---	---	----	----	----

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ch14/selsort/SelectionSorter.java

```
/**
 * This class sorts an array, using the selection sort
 * algorithm
 */
public class SelectionSorter
{
    /**
     * Constructs a selection sorter.
     * @param anArray the array to sort
     */
    public SelectionSorter(int[] anArray)
    {
        a = anArray;
    }

    /**
     * Sorts the array managed by this selection sorter.
     */
    public void sort()
    {

```

Continued¹²

ch14/selsort/SelectionSorter.java (cont.)

```
    for (int i = 0; i < a.length - 1; i++)
    {
        int minPos = minimumPosition(i);
        swap(minPos, i);
    }
}

/**
 * Finds the smallest element in a tail range of the array.
 * @param from the first position in a to compare
 * @return the position of the smallest element in the
 *         range a[from] . . . a[a.length - 1]
 */
private int minimumPosition(int from)
{
    int minPos = from;
    for (int i = from + 1; i < a.length; i++)
        if (a[i] < a[minPos]) minPos = i;
    return minPos;
}
```

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ch14/selsort/SelectionSorter.java (cont.)

```
/**
 * Swaps two entries of the array.
 * @param i the first position to swap
 * @param j the second position to swap
 */
private void swap(int i, int j)
{
    int temp = a[i];
    a[i] = a[j];
    a[j] = temp;
}

private int[] a;
}
```

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ch14/selsort/SelectionSortDemo.java

```
01: import java.util.Arrays;
02:
03: /**
04:  * This program demonstrates the selection sort algorithm by
05:  * sorting an array that is filled with random numbers.
06:  */
07: public class SelectionSortDemo
08: {
09:     public static void main(String[] args)
10:     {
11:         int[] a = ArrayUtil.randomIntArray(20, 100);
12:         System.out.println(Arrays.toString(a));
13:
14:         SelectionSorter sorter = new SelectionSorter(a);
15:         sorter.sort();
16:
17:         System.out.println(Arrays.toString(a));
18:     }
19: }
20:
21:
```

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File ArrayUtil.java

Typical Output:

```
[65, 46, 14, 52, 38, 2, 96, 39, 14, 33, 13, 4, 24, 99, 89, 77,
73, 87, 36, 81] [2, 4, 13, 14, 14, 24, 33, 36, 38, 39, 46, 52,
65, 73, 77, 81, 87, 89, 96, 99]
```

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Question

Why do we need the `temp` variable in the `swap` method? What would happen if you simply assigned `a[i]` to `a[j]` and `a[j]` to `a[i]`?

Answer: Dropping the `temp` variable would not work. Then `a[i]` and `a[j]` would end up being the same value.

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Question

What steps does the selection sort algorithm go through to sort the sequence 6 5 4 3 2 1?

Answer:

1	5	4	3	2	6
---	---	---	---	---	---

1	2	4	3	5	6
---	---	---	---	---	---

1	2	3	4	5	6
---	---	---	---	---	---

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Analyzing the Performance of the Selection Sort Algorithm

- In an array of size n , count how many times an array element is visited
 - To find the smallest, visit n elements + 2 visits for the swap
 - To find the next smallest, visit $(n - 1)$ elements + 2 visits for the swap
 - The last term is 2 elements visited to find the smallest + 2 visits for the swap

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Analyzing the Performance of the Selection Sort Algorithm

- The number of visits:
 - $n + 2 + (n - 1) + 2 + (n - 2) + 2 + \dots + 2 + 2$
 - This can be simplified to $n^2 / 2 + 5n / 2 - 3$
 - $5n / 2 - 3$ is small compared to $n^2 / 2$ – so let's ignore it
 - Also ignore the $1/2$ – it cancels out when comparing ratios

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Analyzing the Performance of the Selection Sort Algorithm

- The number of visits is of the order n^2
- Using big-Oh notation: The number of visits is $O(n^2)$
- Multiplying the number of elements in an array by **2** multiplies the processing time by **4**
- Big-Oh notation " $f(n) = O(g(n))$ " expresses that f grows no faster than g
- To convert to big-Oh notation: locate fastest-growing term, and ignore constant coefficient

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Question

If you increase the size of a data set tenfold, how much longer does it take to sort it with the selection sort algorithm?

Answer: It takes about 100 times longer.

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Learning Goals Review

You are expected to:

- use big-O notation to categorize an algorithm as constant, linear, quadratic, logarithmic and exponential time
- given two or more algorithms, rank them in terms of their time efficiency

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Java Collections: the List Interface

You will be expected to:

- program to the generic List interface including read and use the List API (e.g., use Lists in ways similar to arrays)
- program using the ListIterator interface (be able to read and use the ListIterator API)
- explain the difference between Iterator and ListIterator
- compare and contrast ArrayList and LinkedList implementations of the List interface

Reading :

- 2nd Ed: 20.1
- 3rd/4th Eds: 15.1

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The List Interface

- A *list* is an ordered collection that can contain duplicates. Lists are also called *sequences*. **Example:** `ArrayList`.
- The `List` interface extends `Collection` and adds methods for:
 - **positional access:** can access
 - current position (using an iterator)
 - *i*-th element ($0 \leq i < \text{size}$)
 - **positional search**
 - returns the position of a given object
 - **special iteration**
 - defines special iterators for moving forwards *or backwards*
 - **subrange operations**
 - create sub-lists
 - add/delete elements at a given position

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List

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The List Interface (cont'd)

```
public interface List<E> extends Collection<E> {
    // Positional Access
    E get(int index);
    E set(int index, E element); // Optional
    void add(int index, E element); // Optional
    E remove(int index); // Optional
    boolean addAll(int index, Collection c); // Optional
    // Search
    int indexOf(Object o);
    int lastIndexOf(Object o);
    // Iteration
    ListIterator<E> listIterator();
    ListIterator<E> listIterator(int index);
    // Sublist
    List<E> subList(int fromIndex, int toIndex);
}
```

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List

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The List Interface (cont'd)

- New methods in addition to those inherited from `Collection`:
 - `add(i, e)` adds at position *i*
 - `addAll(i, c)` adds the given collection *c* starting at position *i*
 - `remove(i)` removes object at position *i*
- Methods whose behaviour is specified to be different than in the `Collection` interface (overridden):
 - `add(e)` – adds *e* at the end of the list
 - `addAll(c)` – adds collection *c* at the end of the list
 - `remove(o)` – removes first occurrence of *o*

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The List Interface (cont'd)

- The `subList` method returns a *view* of this list between `fromIndex` (inclusive) and `toIndex` (exclusive).
- Any non-structural changes to the sublist are reflected in this list and vice versa.
- You must not make structural changes (i.e., add or remove) to the original underlying list while using the sublist.
- Structural changes to the sublist *are* reflected in the backing list.

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List

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The List Interface (cont'd)

- **Example:** clear / remove all the items from a list between index 1 (inclusive) and 4 (exclusive):

```
myList.subList( 1, 4 ).clear();
```

- **Example:** a function that swaps two list elements:

```
public static <T> void swap(List<T> list, int i, int j)
{
```

```
}
```

- Why do we have <T> at the start of the method declaration?

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List

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ListIterator

- In addition to a general `Iterator`, a list can also create a more specialized `ListIterator`.
- A `ListIterator` is an example of a *bi-directional* iterator. You can traverse the list either forwards or backwards.

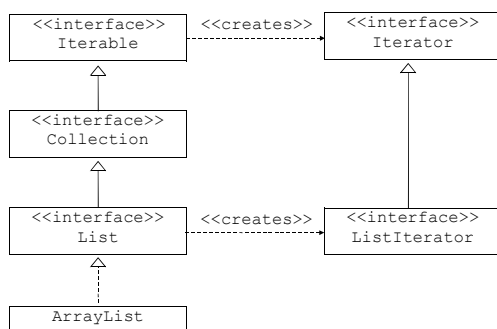
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Java Collection Framework



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The ListIterator Interface

```
public interface ListIterator<E>
    extends Iterator<E>
{
    boolean hasPrevious();
    E previous();

    int nextIndex();
    int previousIndex();

    void set(E o); // Optional
    void add(E o); // Optional
}
```

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ListIterator

- Can create an iterator that is positioned at
 - the first element
 - a specified position
- `next()` returns items in the order they are in the list
- List iterators can move forwards or backwards
 - `nextIndex()` returns the index of the next item
 - `previousIndex()` returns the index of the previous element
- Best way is to think that the iterator points *between* the

items: ↑ item 0 ↑ item 1 ↑ item 2 ↑ item 3 ↑
index 0 1 2 3 4

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ListIterator (cont')

- The `remove` and `set` method affect the last element that was returned by a call to `next` or `previous`.
 - Cannot be called if `remove()` or `add()` have been called since last call to `next()` or `previous()`. Throws `IllegalStateException`.
- The `add` method adds a new element after the one that will be returned by a call to `previous` and before the one that will be returned by `next`.
 - Cannot be called if `add()` has been called since last call to `next()` or `previous()`. Throws `IllegalStateException`.
- The restrictions we discuss for general iterators are also applicable to `ListIterator`'s. See the Java API for more details on restrictions.

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ListIterator (cont')

- After performing an `add`, a subsequent call to `previous` will return the element just added and a subsequent call to `next` is unaffected.
- Example:

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In-Class Exercise I

1. Write a method that takes a `List<String>` parameter and prints out each item in the list
 2. Write a second method that takes a `List<String>` parameter and prints out each item in reverse
- Indicate the time complexity of your methods

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List

Inserting an Element into a Linked List

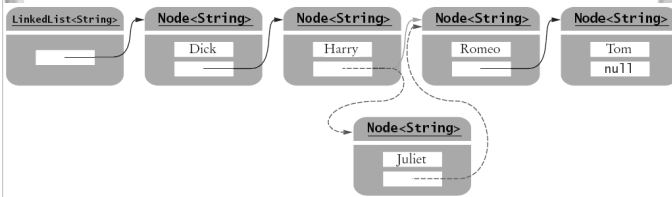


Figure 1 Inserting an Element into a Linked List

Java's `LinkedList` class

- Generic class
 - Specify type of elements in angle brackets: `LinkedList<Product>`
- Package: `java.util`
- Easy access to first and last elements with methods
 - `void addFirst(E obj)`
 - `void addLast(E obj)`
 - `E getFirst()`
 - `E getLast()`
 - `E removeFirst()`
 - `E removeLast()`

List Iterator

- `ListIterator` type
- Gives access to elements inside a linked list
- Encapsulates a position anywhere inside the linked list
- Protects the linked list while giving access

A List Iterator

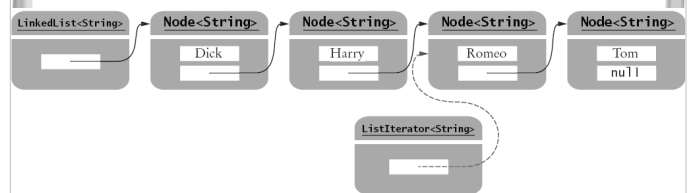


Figure 2 A List Iterator

A Conceptual View of the List Iterator

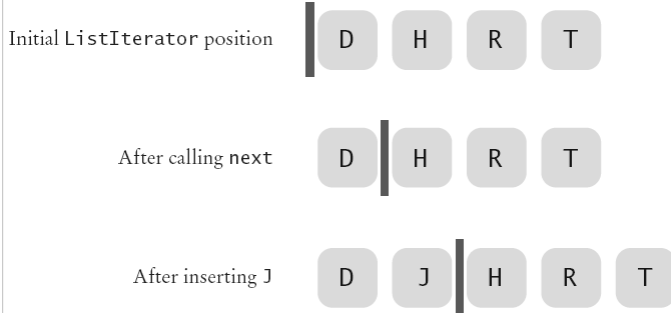


Figure 3 A Conceptual View of the List Iterator

List Iterator

- Think of an iterator as pointing between two elements
 - *Analogy: like the cursor in a word processor points between two characters*
- The `listIterator` method of the `LinkedList` class gets a list iterator

```
LinkedList<String> employeeNames = . . .; ListIterator<String>  
iterator =  
    employeeNames.listIterator();
```

List Iterator

- Initially, the iterator points before the first element
- The `next` method moves the iterator
`iterator.next();`
- `next` throws a `NoSuchElementException` if you are already past the end of the list
- `hasNext` returns true if there is a next element
`if (iterator.hasNext())
 iterator.next();`

List Iterator

- The `next` method returns the element that the iterator is passing

```
while iterator.hasNext()  
{  
    String name = iterator.next();  
    Do something with name  
}
```

- Shorthand:

```
for (String name : employeeNames)  
{  
    Do something with name  
}
```

Behind the scenes, the for loop uses an iterator to visit all list elements

List Iterator

- `LinkedList` is a *doubly linked list*
 - *Class stores two links:*
 - One to the next element, and
 - One to the previous element
- To move the list position backwards, use:
 - `hasPrevious`
 - `previous`

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Adding and Removing from a LinkedList

- The `add` method:
 - *Adds an object after the iterator*
 - *Moves the iterator position past the new element*

```
iterator.add("Juliet");
```

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Adding and Removing from a LinkedList

- The `remove` method
 - *Removes and*
 - *Returns the object that was returned by the last call to `next` or `previous`*
- ```
//Remove all names that fulfill a certain condition
while (iterator.hasNext())
{
String name = iterator.next();
if (name fulfills condition)
 iterator.remove(); }
```
- Be careful when calling `remove`:
    - *It can be called only once after calling `next` or `previous`*
    - *You cannot call it immediately after a call to `add`*
    - *If you call it improperly, it throws an `IllegalStateException`*

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## Sample Program

- `ListTester` is a sample program that
  - *Inserts strings into a list*
  - *Iterates through the list, adding and removing elements*
  - *Prints the list*

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### ch15/uselist/ListTester.java

```
01: import java.util.LinkedList;
02: import java.util.ListIterator;
03:
04: /**
05: * A program that tests the LinkedList class
06: */
07: public class ListTester
08: {
09: public static void main(String[] args)
10: {
11: LinkedList<String> staff = new LinkedList<String>();
12: staff.addLast("Dick");
13: staff.addLast("Harry");
14: staff.addLast("Romeo");
15: staff.addLast("Tom");
16:
17: // ! in the comments indicates the iterator position
18:
19: ListIterator<String> iterator
20: = staff.listIterator(); // |DHRT
21: iterator.next(); // D|HRT
22: iterator.next(); // DH|RT
```

Continued

### ch15/uselist/ListTester.java (cont.)

```
23:
24: // Add more elements after second element
25:
26: iterator.add("Juliet"); // DHJ|RT
27: iterator.add("Nina"); // DHJN|RT
28:
29: iterator.next(); // DHJNR|T
30:
31: // Remove last traversed element
32:
33: iterator.remove(); // DHJN|T
34:
35: // Print all elements
36:
37: for (String name : staff)
38: System.out.print(iterator.next() + " ");
39: System.out.println();
40: System.out.println("Expected: Dick Harry Juliet Nina Tom");
41: }
42: }
```

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### ch15/uselist/ListTester.java (cont.)

#### Output:

```
Dick Harry Juliet Nina Tom
Expected: Dick Harry Juliet Nina Tom
```

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## LinkedList

- Let's look at how LinkedList is actually implemented, since it differs from ArrayList
- This is actually a simplified version of LinkedList from Big Java

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### Adding a New First Element

- When a new node is added to the list
  - It becomes the head of the list
  - The old list head becomes its next node

### Adding a New First Element

```
public void addFirst(Object obj)
{
 Node newNode = new Node(); ①
 newNode.data = obj;
 newNode.next = first; first = newNode;
}
```

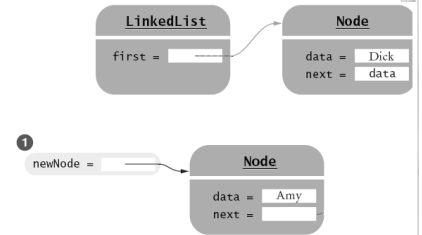


Figure 4 Adding a Node to the Head of a Linked List

### Adding a New First Element

```
public void addFirst(Object obj)
{
 Node newNode = new Node(); ①
 newNode.data = obj;
 newNode.next = first; ②
 first = newNode;
}
```

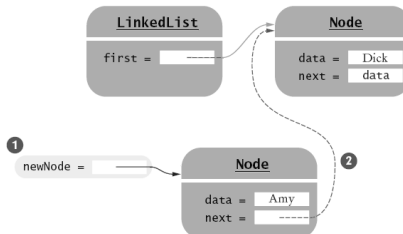


Figure 4 Adding a Node to the Head of a Linked List

### Adding a New First Element

```
public void addFirst(Object obj)
{
 Node newNode = new Node(); ①
 newNode.data = obj;
 newNode.next = first; ②
 first = newNode; ③
}
```

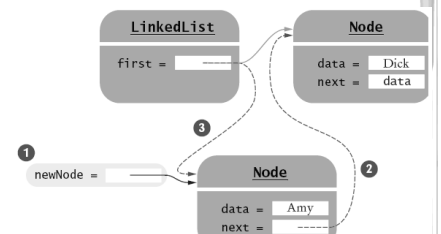


Figure 4 Adding a Node to the Head of a Linked List

## Removing the First Element

- When the first element is removed
  - The data of the first node are saved and later returned as the method result
  - The successor of the first node becomes the first node of the shorter list
  - The old node will be garbage collected when there are no further references to it

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## Removing the First Element

```
public Object removeFirst()
{
 if (first == null)
 throw new NoSuchElementException();
 Object obj = first.data;
 first = first.next;
 return obj;
}
```

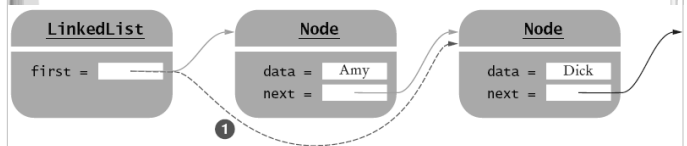


Figure 5 Removing the First Node from a Linked List

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## Linked List Iterator

- We define `LinkedListIterator`: private inner class of `LinkedList`
- Implements a simplified `ListIterator` interface
- Has access to the `first` field and private `Node` class
- Clients of `LinkedList` don't actually know the name of the iterator class
  - They only know it is a class that implements the `ListIterator` interface

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## LinkedListIterator

### The LinkedListIterator class

```
public class LinkedList
{
 . . .
 public ListIterator listIterator()
 {
 return new LinkedListIterator();
 }

 private class LinkedListIterator implements
 ListIterator
 {
 public LinkedListIterator()
 {
 position = null;
 previous = null;
 }
 }
}
```

Continued



### LinkedListIterator (cont.)

```
...
private Node position;
private Node previous;
}
...
```

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### The Linked List Iterator's next Method

- `position`: reference to the last visited node
- Also, store a reference to the last reference before that
- `next` method: `position` reference is advanced to `position.next`
- Old position is remembered in `previous`
- If the iterator points before the first element of the list, then the old `position` is `null` and `position` must be set to `first`

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### The Linked List Iterator's next Method

```
public Object next()
{
 if (!hasNext())
 throw new NoSuchElementException();
 previous = position; // Remember for remove
 if (position == null)
 position = first;
 else position = position.next;
 return position.data;
}
```

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### The Linked List Iterator's hasNext Method

- The `next` method should only be called when the iterator is not at the end of the list
- The iterator is at the end
  - if the list is empty (`first == null`)
  - if there is no element after the current position (`position.next == null`)

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### The Linked List Iterator's hasNext Method

```
private class LinkedListIterator implements ListIterator
{
 . . .
 public boolean hasNext ()
 {
 if (position == null)
 return first != null;
 else
 return position.next != null;
 }
 . . .
}
```

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### The Linked List Iterator's remove Method

- If the element to be removed is the first element, call `removeFirst`
- Otherwise, the node preceding the element to be removed needs to have its `next` reference updated to skip the removed element
- If the `previous` reference equals `position`:
  - *this call does not immediately follow a call to `next`*
  - *throw an `IllegalArgumentException`*
- It is illegal to call `remove` twice in a row
  - *`remove` sets the `previous` reference to `position`*

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### The Linked List Iterator's remove Method

```
public void remove ()
{
 if (previous == position)
 throw new IllegalStateException();
 if (position == first)
 {
 removeFirst ();
 }
 else
 {
 previous.next = position.next; ❶
 }
 position = previous;
}
```

Continued

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### The Linked List Iterator's remove Method (cont.)

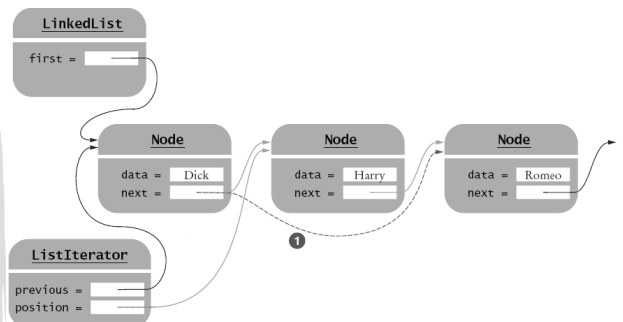


Figure 6 Removing a Node from the Middle of a Linked List

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### The Linked List Iterator's remove Method

```
public void remove()
{
 If (previous == position)
 throw new IllegalStateException();
 if (position == first)
 {
 removeFirst();
 }
 else
 {
 previous.next = position.next; ❶
 }
 position = previous; ❷
}
```

Continued 73

### The Linked List Iterator's remove Method (cont.)

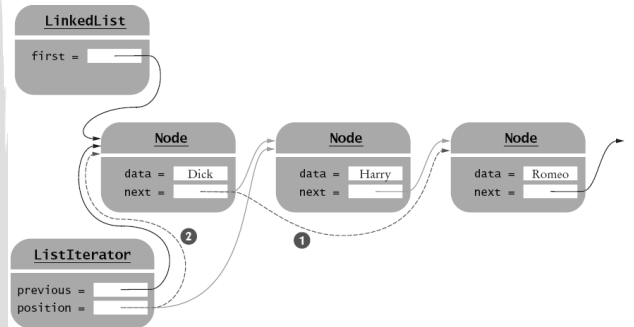


Figure 6 Removing a Node from the Middle of a Linked List

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### The Linked List Iterator's set Method

- Changes the data stored in the previously visited element
- The **set** method

```
public void set(Object obj)
{
 if (position == null)
 throw new NoSuchElementException();
 position.data = obj;
}
```

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### The Linked List Iterator's add Method

- The most complex operation is the addition of a node
  - *add* inserts the new node after the current position
  - Sets the successor of the new node to the successor of the current position

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### The Linked List Iterator's add Method

```

public void add(Object obj)
{
 if (position == null)
 {
 addFirst(obj);
 position = first;
 }
 else
 {
 Node newNode = new Node();
 newNode.data = obj;
 newNode.next = position.next; ❶
 position.next = newNode;
 position = newNode;
 }
 previous = position;
}

```

Continued 77

### The Linked List Iterator's add Method (cont.)

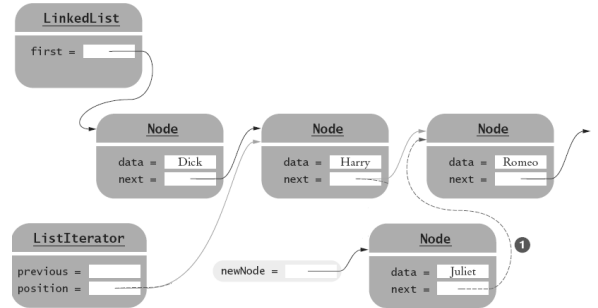


Figure 7 Adding a Node to the Middle of a Linked List

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### The Linked List Iterator's add Method

```

public void add(Object obj)
{
 if (position == null)
 {
 addFirst(obj);
 position = first;
 }
 else
 {
 Node newNode = new Node();
 newNode.data = obj;
 newNode.next = position.next; ❶
 position.next = newNode; ❷
 position = newNode;
 }
 previous = position;
}

```

Continued 79

### The Linked List Iterator's add Method (cont.)

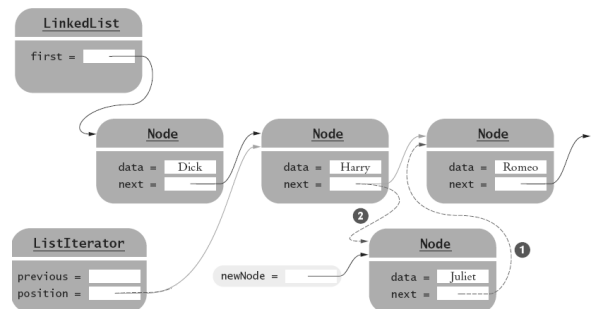


Figure 7 Adding a Node to the Middle of a Linked List

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### The Linked List Iterator's add Method

```

public void add(Object obj)
{
 if (position == null)
 {
 addFirst(obj);
 position = first;
 }
 else
 {
 Node newNode = new Node();
 newNode.data = obj;
 newNode.next = position.next; 1
 position.next = newNode; 2
 position = newNode; 3
 }
 previous = position;
}

```

Continued 81

### The Linked List Iterator's add Method (cont.)

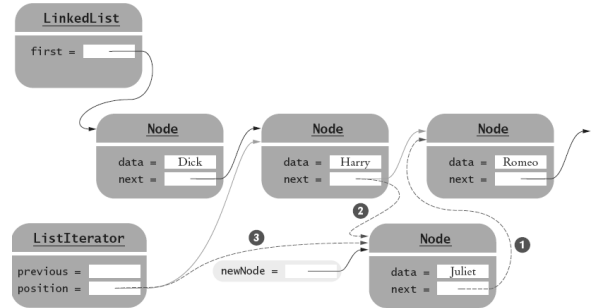


Figure 7 Adding a Node to the Middle of a Linked List

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### The LinkedList Class

- Let's look at some differences between ArrayList and LinkedList. Let's consider the time complexity of some common operations in the worst case:

|                        | LinkedList | ArrayList |
|------------------------|------------|-----------|
| get( int index )       | O(n)       | O(1)      |
| add( int i, E e )      | O(n)       | O(n)      |
| add( E e )             | O(1)       | O(1)      |
| remove( int index )    | O(n)       | O(n)      |
| contains( Object o )   | O(n)       | O(n)      |
| ListIterator -> add    | O(1)       | O(n)      |
| ListIterator -> remove | O(1)       | O(n)      |

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### Efficiency of Operations for Arrays and Lists

| Operation             | ArrayList | LinkedList |
|-----------------------|-----------|------------|
| Random access         | O(1)      | O(n)       |
| Linear traversal step | O(1)      | O(1)       |
| Add/remove an element | O(n)      | O(1)       |

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## List Example

- Reverse a list

```
public static <E> List<E> reverse (List<E> list) {

 List<E> newList = new ArrayList<E> ();

 Iterator<E> it = list.iterator();
 while (it.hasNext()) {
 newList.add (0, it.next());
 }
 return newList;
}
```

What is its complexity?

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List

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## List Example

- A better way to write this method:

```
public static <E> List<E> reverse (List<E> list) {
```

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List

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## In-Class Exercise II

- Write a method that takes an `ArrayList<String>`, and visits each item in order, printing out the item and then removing it
- Write a method that takes a `LinkedList<String>`, and visits each item in reverse order, printing out the item and then removing it
- Indicate the complexity of each method

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## Learning Goals Review

You will be expected to:

- program to the generic `List` interface including read and use the `List` API (e.g., use Lists in ways similar to arrays)
- program using the `ListIterator` interface ( be able to read and use the `ListIterator` API)
- explain the difference between `Iterator` and `ListIterator`
- compare and contrast `ArrayList` and `LinkedList` implementations of the `List` interface

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## Midterm Exam

- Class contracts
  - Preconditions
  - Postconditions
  - Invariants

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## Midterm Exam

- Exceptions
  - Throwing
  - Catching
  - Propagating
  - Defining

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## Midterm Exam

- Testing
  - Unit testing
  - Blackbox testing
  - Equivalence classes
  - Test cases: typical values, boundary values

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## Midterm Exam

- Good and bad design
  - High cohesion, low coupling
  - Open-closed principle
  - Liskov substitution principle
  - Weakening precondition, strengthening postcondition

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## Midterm Exam

- Java collections
  - Interfaces: Iterable, Collection, List, Iterator
  - Classes: ArrayList
- Generic programming
  - Generic classes (defining and using)
  - Generic methods (defining and using)
  - Type parameters
  - Bounded wildcards