

## A tentative outline for cs406

Term 1 of 2016/17, Tue Thu 11:00-12:30pm

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1. Introduction
  - (a) Types of problems, and what we concentrate on
  - (b) Basics: convexity, gradient and Hessian, Taylor expansions, linearity, optimality
2. Unconstrained optimization
  - (a) Necessary and sufficient conditions
  - (b) Basic methods: gradient descent and Newton
  - (c) Line search and trust region
  - (d) Quasi-Newton: secant; BFGS
  - (e) Derivative-free optimization; Nelder-Mead
  - (f) Linear and nonlinear least squares; Truncated SVD; Gauss-Newton
  - (g) Case study: Kalman filter
3. Constrained optimization
  - (a) Necessary and sufficient conditions; KKT; duality
  - (b) Linear programming: simplex
  - (c) Linear programming: primal-dual; interior point
  - (d) Augmented Lagrangian; proximal method and ADMM
  - (e) Case study: sparse solution to unconstrained equations via  $\ell_1$
  - (f) Convex quadratic programming
  - (g) Sequential quadratic programming
4. Very large problems (time permitting)
  - (a) Preconditioned conjugate gradient method
  - (b) Krylov subspace methods
  - (c) Inexact Newton applications
  - (d) Limited memory BFGS
  - (e) Large scale least squares and saddle point