

Intelligent Systems (AI-2)

Computer Science cpsc422, Lecture 31

Nov, 24, 2017

Slide source: from Pedro Domingos UW & Markov Logic: An Interface Layer for Artificial Intelligence Pedro Domingos and Daniel Lowd University of Washington, Seattle

Lecture Overview

- **Finish Inference in MLN**
 - Probability of a formula, Conditional Probability
- **Markov Logic: applications**
 - Entity resolution
 - Statistical Parsing!

Markov Logic: Definition



- A Markov Logic Network (MLN) is
 - a set of pairs (F, w) where
 - F is a **formula** in first-order logic
 - w is a **real number**
 - Together with a set C of **constants**,
- It defines a **Markov network** with
 - One *binary node* for each **grounding** of each **predicate** in the MLN
 - One *feature/factor* for each **grounding** of each **formula F** in the MLN, with the corresponding weight w

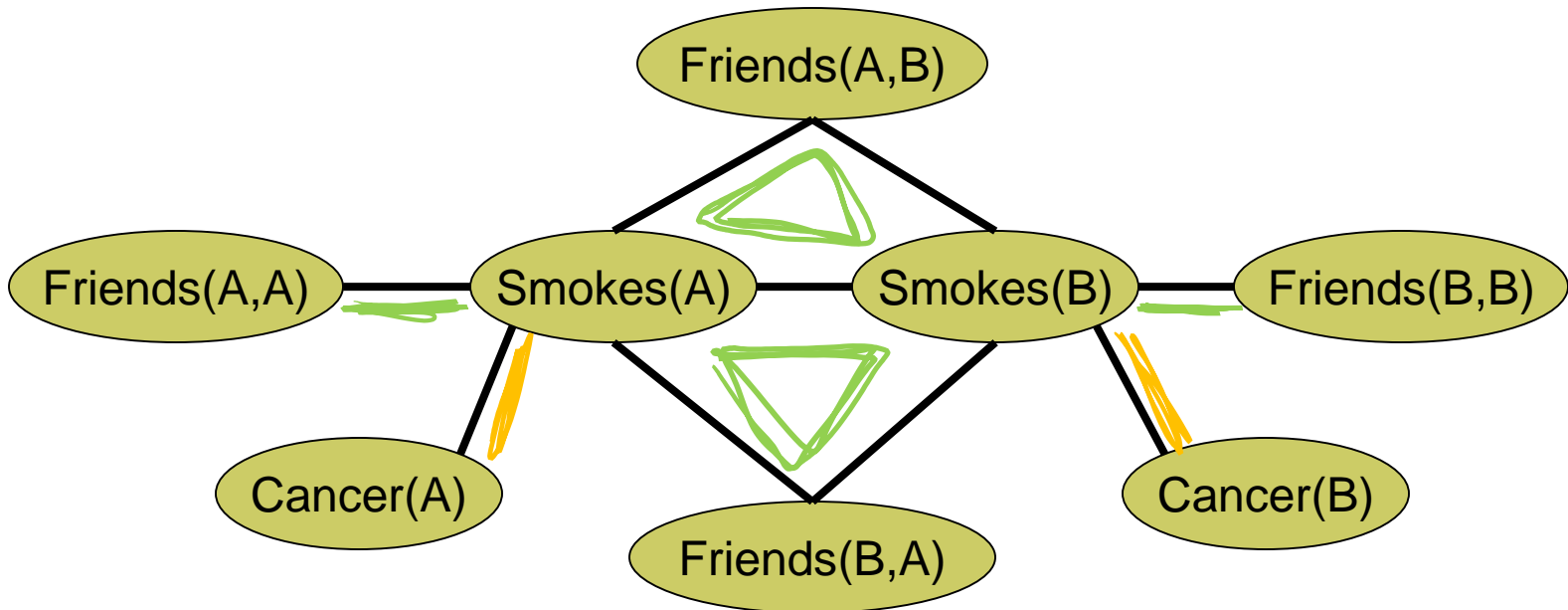
Grounding:
substituting vars
with constants

MLN features



- 1.5 $\forall x \text{Smokes}(x) \Rightarrow \text{Cancer}(x)$
- 1.1 $\forall x, y \text{Friends}(x, y) \Rightarrow (\text{Smokes}(x) \Leftrightarrow \text{Smokes}(y))$

Two constants: **Anna** (A) and **Bob** (B)



Computing Probabilities



$$P(\text{Formula}, M_{L,C}) = ?$$

- **Brute force:** Sum probs. of possible worlds where formula holds

$M_{L,C}$ Markov Logic Network

PW_F possible worlds in which F is true

$$P(F, M_{L,C}) = \sum_{pw \in PW_F} P(pw, M_{L,C})$$

- **MCMC:** Sample worlds, check formula holds

S all samples

S_F samples (i.e. possible worlds) in which F is true

$$P(F, M_{L,C}) = \frac{|S_F|}{|S|}$$

Computing Cond. Probabilities



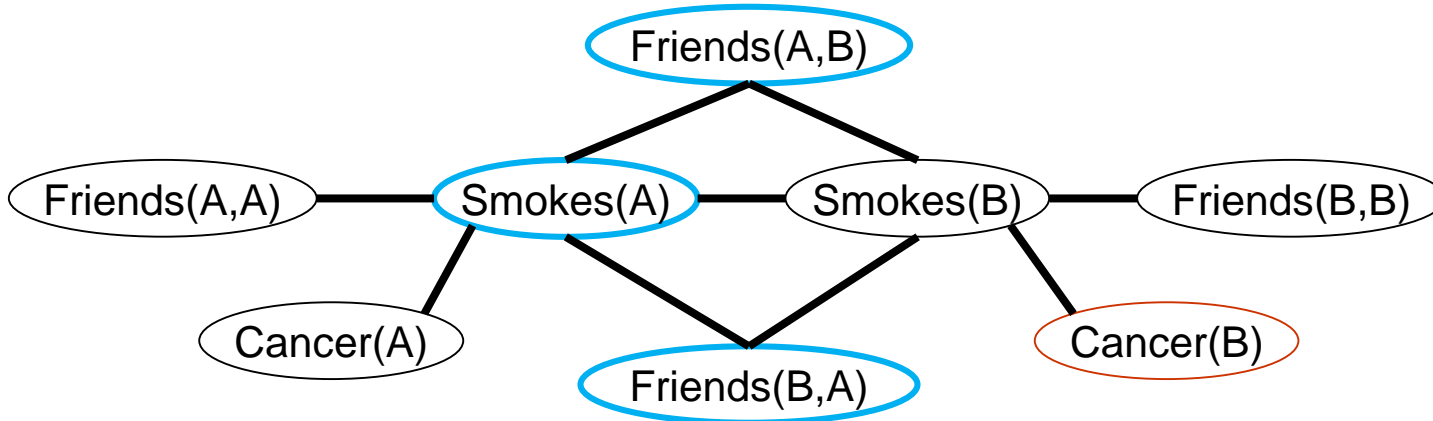
1.5 $\forall x \text{ Smokes}(x) \Rightarrow \text{Cancer}(x)$

1.1 $\forall x, y \text{ Friends}(x, y) \Rightarrow (\text{Smokes}(x) \Leftrightarrow \text{Smokes}(y))$

Let's look at the simplest case

$P(\text{ground literal} \mid \text{conjunction of ground literals}, M_{L,C})$

$P(\text{Cancer}(B) \mid \text{Smokes}(A), \text{Friends}(A, B), \text{Friends}(B, A))$



To answer this query do you need to create (ground) the whole network?

A. Yes

B. No

C. It depends ...

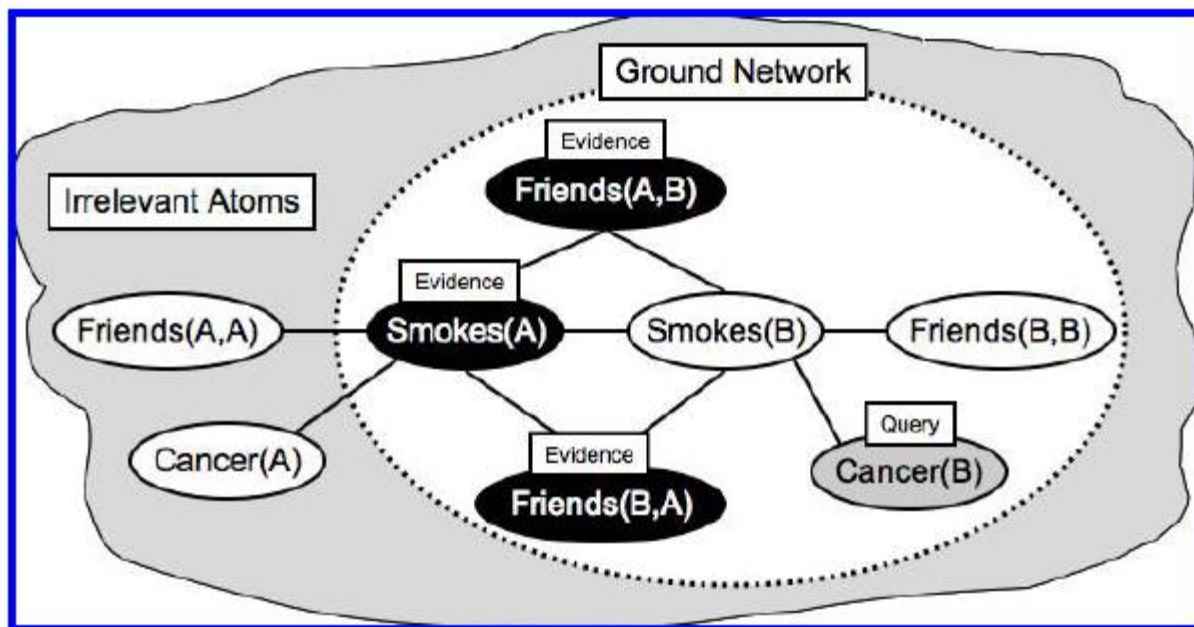
Computing Cond. Probabilities



Let's look at the simplest case

$P(\text{ground literal} \mid \text{conjunction of ground literals}, M_{L,C})$

$P(\text{Cancer}(B) \mid \text{Smokes}(A), \text{Friends}(A, B), \text{Friends}(B, A))$



You do not need to create (ground) the part of the Markov Network from which the query is independent given the evidence

Computing Cond. Probabilities

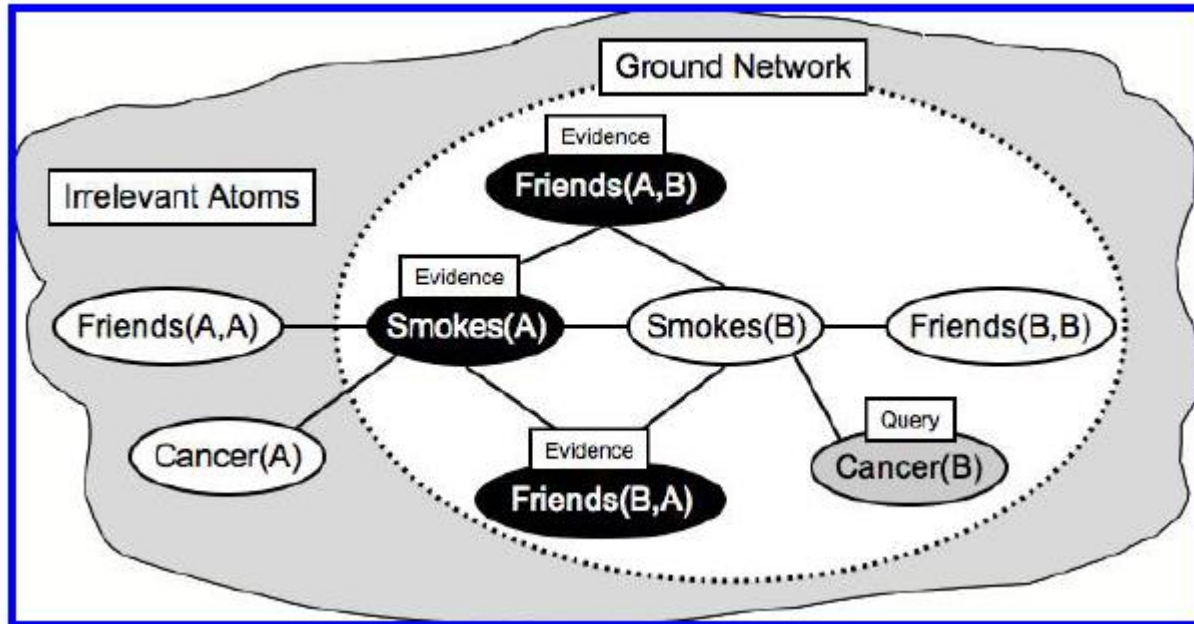


$$P(\text{Cancer}(B) \mid \text{Smokes}(A), \text{Friends}(A, B), \text{Friends}(B, A))$$

The sub network is determined by the formulas
(the logical structure of the problem)

1.5 $\forall x \text{Smokes}(x) \Rightarrow \text{Cancer}(x)$

1.1 $\forall x, y \text{Friends}(x, y) \Rightarrow (\text{Smokes}(x) \Leftrightarrow \text{Smokes}(y))$



You can then perform Gibbs Sampling in
this Sub Network

Lecture Overview

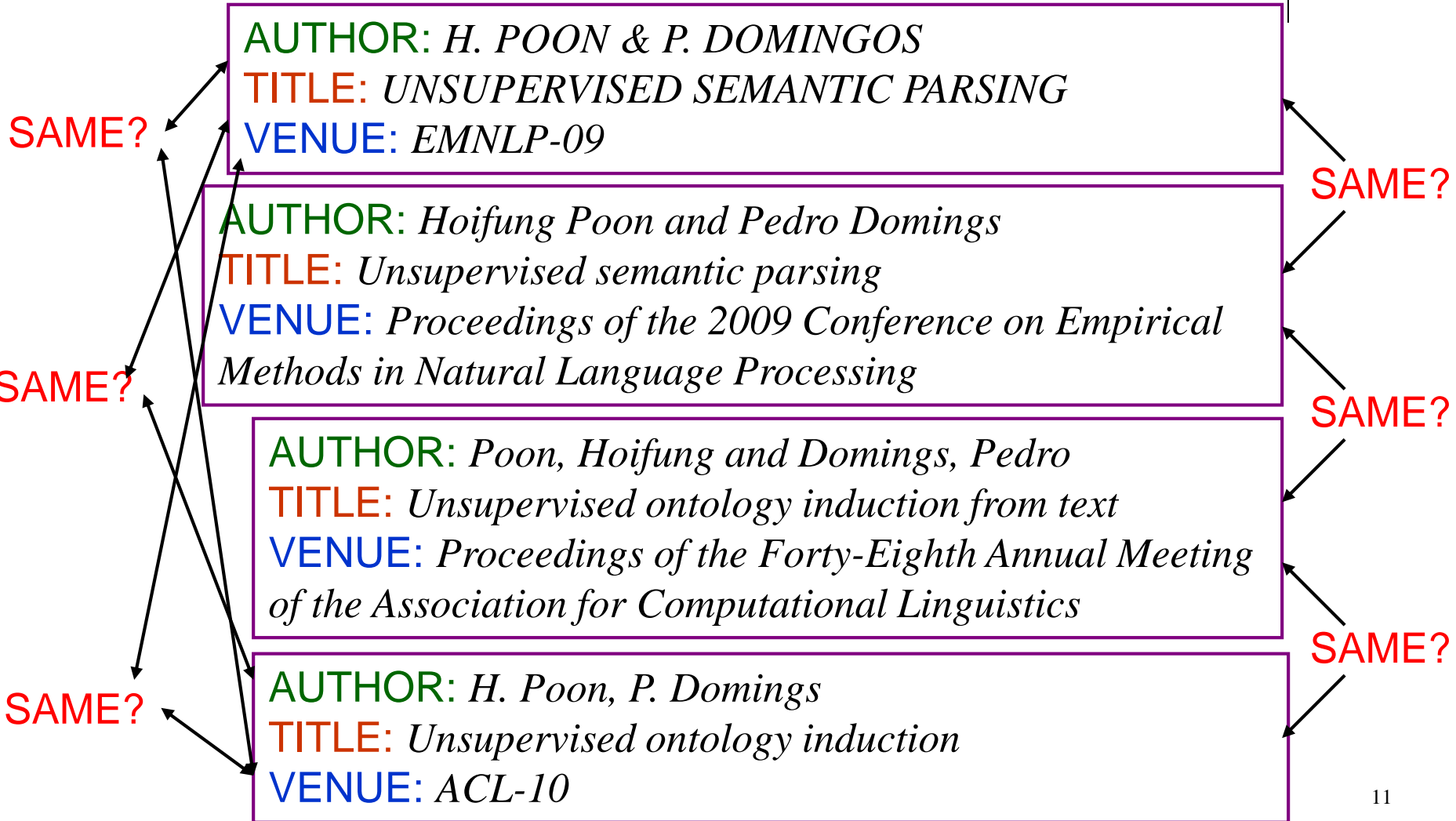
- **Finish Inference in MLN**
 - Probability of a formula, Conditional Probability
- **Markov Logic: applications**
 - **Entity resolution**
 - **Statistical Parsing!**

Entity Resolution



- Determining which observations correspond to the same real-world objects
- (e.g., database records, noun phrases, video regions, etc)
- Crucial importance in many areas (e.g., data cleaning, NLP, Vision)

Entity Resolution: Example



Entity Resolution (relations)



Problem: Given citation database, find duplicate records
Each citation has author, title, and venue fields
We have 10 relations

provided as evidence

Author(bib, author)

Title(bib, title)

Venue(bib, venue)

relate citations to their fields

HasWord(author, word)

HasWord(title, word)

HasWord(venue, word)

indicate which words are present
in each field;

SameAuthor(author, author) represent field equality;

SameTitle(title, title)

SameVenue(venue, venue)

SameBib(bib, bib) represents citation equality;

*To be
inferred*

Entity Resolution (formulas)



Predict citation equality based on words in the fields

$\text{Title}(b1, t1) \wedge \text{Title}(b2, t2) \wedge$
 $\text{HasWord}(t1, +\text{word}) \wedge \text{HasWord}(t2, +\text{word}) \Rightarrow$
 $\text{SameBib}(b1, b2)$

*1000s
of rules
one for
each word*

(NOTE: +word is a shortcut notation, you actually have a rule for each word e.g.,
 $\text{Title}(b1, t1) \wedge \text{Title}(b2, t2) \wedge$
 $\text{HasWord}(t1, \text{"bayesian"}) \wedge$
 $\text{HasWord}(t2, \text{"bayesian"}) \Rightarrow \text{SameBib}(b1, b2)$)

Same 1000s of rules for **author**

Same 1000s of rules for **venue**

Entity Resolution (formulas)



Transitive closure

$\text{SameBib}(b1, b2) \wedge \text{SameBib}(b2, b3) \Rightarrow \text{SameBib}(b1, b3)$

$\text{SameAuthor}(a1, a2) \wedge \text{SameAuthor}(a2, a3) \Rightarrow \text{SameAuthor}(a1, a3)$

Same rule for title

Same rule for venue

Link fields equivalence to citation equivalence – *e.g., if two citations are the same, their authors should be the same*

$\text{Author}(b1, a1) \wedge \text{Author}(b2, a2) \wedge \text{SameBib}(b1, b2) \Rightarrow \text{SameAuthor}(a1, a2)$

...and that citations with the same author are more likely to be the same

$\text{Author}(b1, a1) \wedge \text{Author}(b2, a2) \wedge \text{SameAuthor}(a1, a2) \Rightarrow \text{SameBib}(b1, b2)$

Same rules for title

Same rules for venue

Benefits of MLN model



Standard non-MLN approach: build a classifier that given two citations tells you if they are the same or not, and then apply transitive closure

New MLN approach:

- performs *collective* entity resolution, where resolving one pair of entities helps to resolve pairs of related entities

e.g., inferring that a pair of citations are equivalent can provide evidence that the names *AAAI-06* and *21st Natl. Conf. on AI* refer to the same venue, even though they are superficially very different. This equivalence can then aid in resolving other entities.

Other MLN applications



- **Information Extraction**
- **Co-reference Resolution Robot Mapping**
(infer the map of an indoor environment from laser range data)
- **Link-based Clustering** (uses relationships among the objects in determining similarity)
- **Ontologies extraction from Text**
-

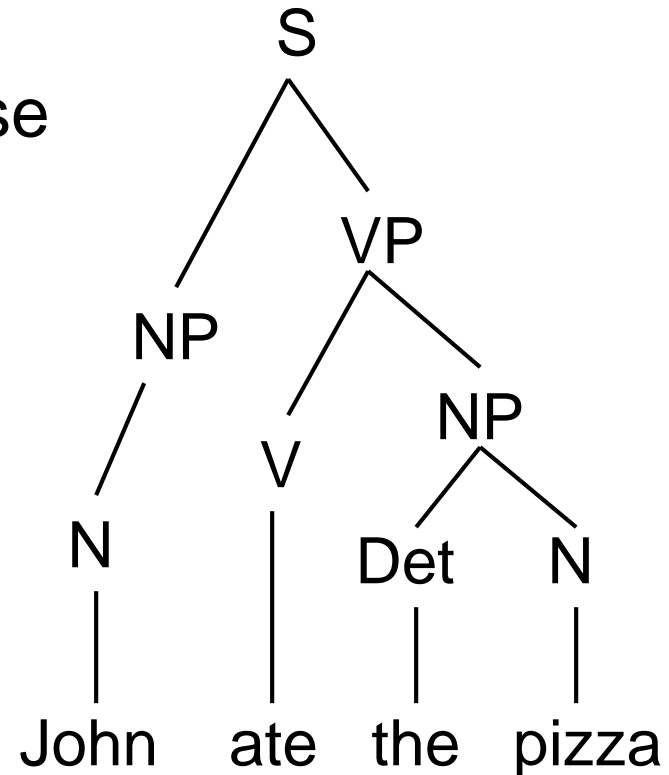
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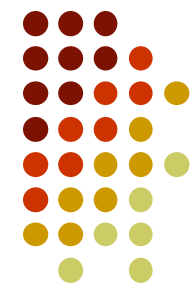
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Statistical Parsing

- **Input:** Sentence
- **Output:** Most probable parse
- **PCFG:** Production rules with probabilities
E.g.: 0.7 $NP \rightarrow N$
0.3 $NP \rightarrow Det N$
- **WCFG:** Production rules with weights (equivalent)
- Chomsky normal form:
 $A \rightarrow B C$ or $A \rightarrow a$





Logical Representation of CFG

→ rewrites as

⇒ logical implication

$S \rightarrow NP VP$ (A) $NP \wedge VP \Rightarrow S$

(B) $NP(i,j) \wedge VP(j,k) \Rightarrow S(i,k)$

(C) $S(i,k) \Rightarrow NP(i,j) \wedge VP(j,k)$

Which one would be a reasonable representation in logics?



0 the 1 dog 2 chases 3 the 4 cat 5



Logical Representation of CFG

$S \rightarrow NP VP$

$NP(i,j) \wedge VP(j,k) \Rightarrow S(i,k)$

$NP \rightarrow Adj N$

$Adj(i,j) \wedge N(j,k) \Rightarrow NP(i,k)$

$NP \rightarrow Det N$

$Det(i,j) \wedge N(j,k) \Rightarrow NP(i,k)$

$VP \rightarrow V NP$

$V(i,j) \wedge NP(j,k) \Rightarrow VP(i,k)$

Lexicon....



// Determiners

$i+1$

Token("a",i) => Det(i,i+1)

Token("the",i) => Det(i,i+1)

// Adjectives

Token("big",i) => Adj(i,i+1)

Token("small",i) => Adj(i,i+1)

// Nouns

Token("dogs",i) => N(i,i+1)

Token("dog",i) => N(i,i+1)

Token("cats",i) => N(i,i+1)

Token("cat",i) => N(i,i+1)

Token("fly",i) => N(i,i+1)

Token("flies",i) => N(i,i+1)

// Verbs

Token("chase",i) => V(i,i+1)

Token("chases",i) => V(i,i+1)

Token("eat",i) => V(i,i+1)

Token("eats",i) => V(i,i+1)

Token("fly",i) => V(i,i+1)

Token("flies",i) => V(i,i+1)

Det(0,1) N(1,2)

the cat ate the mouse
0 1 2 3 4 5
0 1 2 3 4 5

Avoid two problems (1)



- If there are two or more rules with the same left side (such as $NP \rightarrow Adj\ N$ and $NP \rightarrow Det\ N$) need to enforce the constraint that only one of them fires :

$$NP(i,k) \wedge Det(i,j) \Rightarrow \neg Adj(i,j)$$

“If a noun phrase results in a determiner and a noun, it cannot result in an adjective and a noun”.

Avoid two problems (2)



- **Ambiguities in the lexicon.**



homonyms belonging to different parts of speech,
e.g., Fly (noun or verb),
only one of these parts of speech should be assigned.

We can enforce this constraint in a general manner by making mutual exclusion rules for each part of speech pair, i.e.:

$\neg \text{Det}(i,j) \vee \neg \text{Adj}(i,j)$

$\neg \text{Det}(i,j) \vee \neg \text{N}(i,j)$

$\neg \text{Det}(i,j) \vee \neg \text{V}(i,j)$

$\neg \text{Adj}(i,j) \vee \neg \text{N}(i,j)$

$\neg \text{Adj}(i,j) \vee \neg \text{V}(i,j)$

$\neg \text{N}(i,j) \vee \neg \text{V}(i,j)$

$\neg (A \wedge B)$

Statistical Parsing

Representation: Summary



- For each rule of the form $A \rightarrow B C$:
Formula of the form $B(i, j) \wedge C(j, k) \Rightarrow A(i, k)$
E.g.: $NP(i, j) \wedge VP(j, k) \Rightarrow S(i, k)$
- For each rule of the form $A \rightarrow a$:
Formula of the form $Token(a, i) \Rightarrow A(i, i+1)$
E.g.: $Token("pizza", i) \Rightarrow N(i, i+1)$
- For each nonterminal: state that exactly one production holds (solve problem 1)
- Mutual exclusion rules for each part of speech pair (solve problem 2)



Statistical Parsing : Inference

- Evidence predicate: `Token(token, position)`
E.g.: `Token("pizza", 3)` etc.
- Query predicates:
`Constituent(position, position)`
E.g.: `S(0, 7)` "is this sequence of seven words a sentence?" but also `NP(2, 4)`
- What inference yields the most probable parse?

MAP!

Semantic Processing



Example: John ate pizza.

Grammar: $S \rightarrow NP VP$ $VP \rightarrow V NP$ $V \rightarrow \text{ate}$
 $NP \rightarrow \text{John}$ $NP \rightarrow \text{pizza}$

$\text{Token}(\text{"John"}, 0) \Rightarrow \text{Participant}(\text{John}, E, 0, 1)$

$\text{Token}(\text{"ate"}, 1) \Rightarrow \text{Event}(\text{Eating}, E, 1, 2)$

$\text{Token}(\text{"pizza"}, 2) \Rightarrow \text{Participant}(\text{pizza}, E, 2, 3)$

$\text{Event}(\text{Eating}, e, i, j) \wedge \text{Participant}(p, e, j, k)$
 $\wedge \text{VP}(i, k) \wedge \text{V}(i, j) \wedge \text{NP}(j, k) \Rightarrow \text{Eaten}(p, e)$

$\text{Event}(\text{Eating}, e, j, k) \wedge \text{Participant}(p, e, i, j)$
 $\wedge \text{S}(i, k) \wedge \text{NP}(i, j) \wedge \text{VP}(j, k) \Rightarrow \text{Eater}(p, e)$

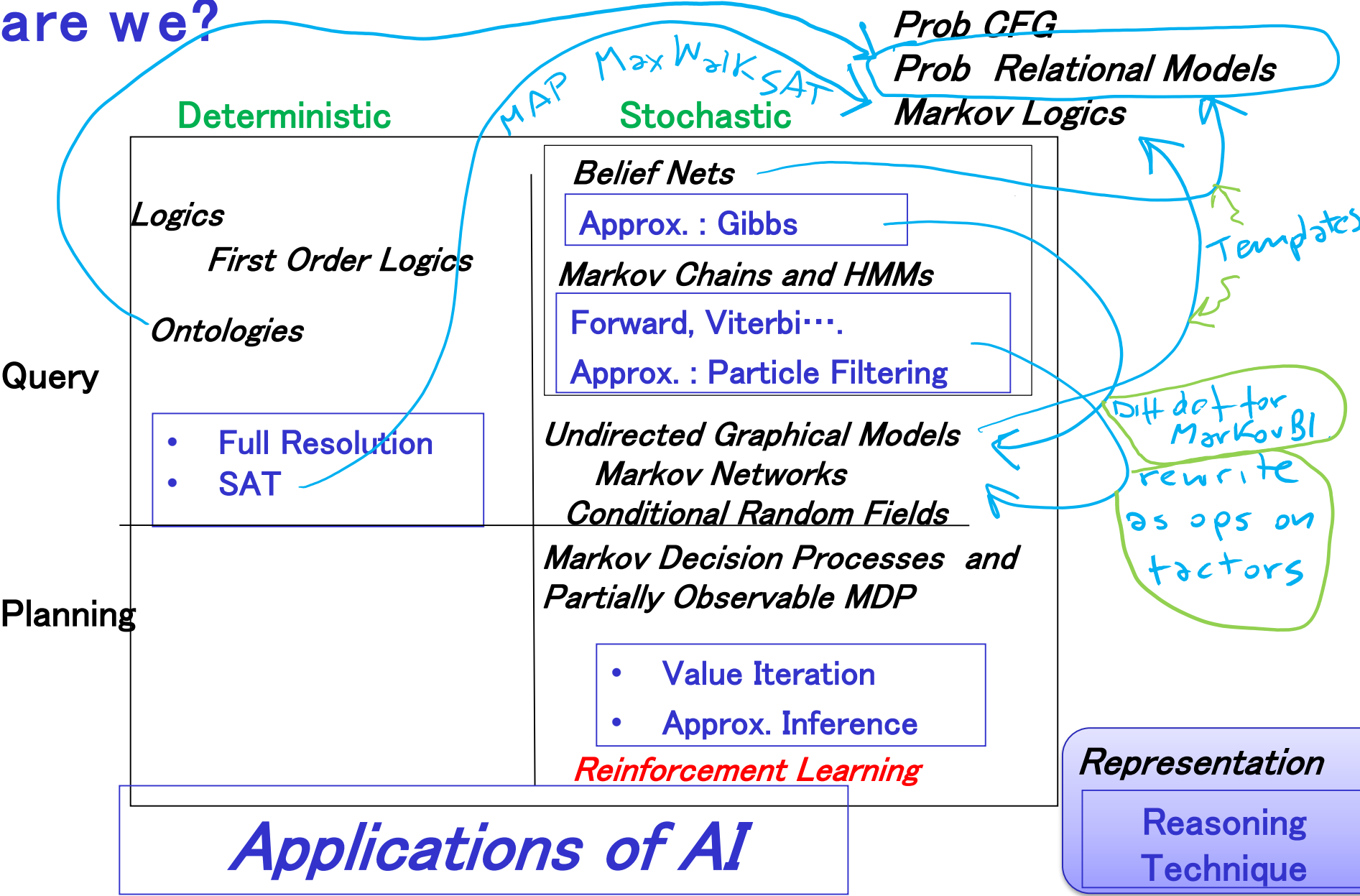
$\text{Event}(t, e, i, k) \Rightarrow \text{Isa}(e, t)$

Result: $\text{Isa}(E, \text{Eating})$, $\text{Eater}(\text{John}, E)$, $\text{Eaten}(\text{pizza}, E)$

422 big picture: Where are we?

StarAI (statistical relational AI)

Hybrid: Det +Sto



Learning Goals for today's class

You can:

- Compute Probability of a formula, Conditional Probability
- Describe the entity resolution application of ML and explain the corresponding representation

Next Class on Mon

- **Start Probabilistic Relational Models**

Keep working on **Assignment-4**

Due Dec 1

In the past, a similar hw took students between 8 - 15 hours to complete. Please start working on it as soon as possible!