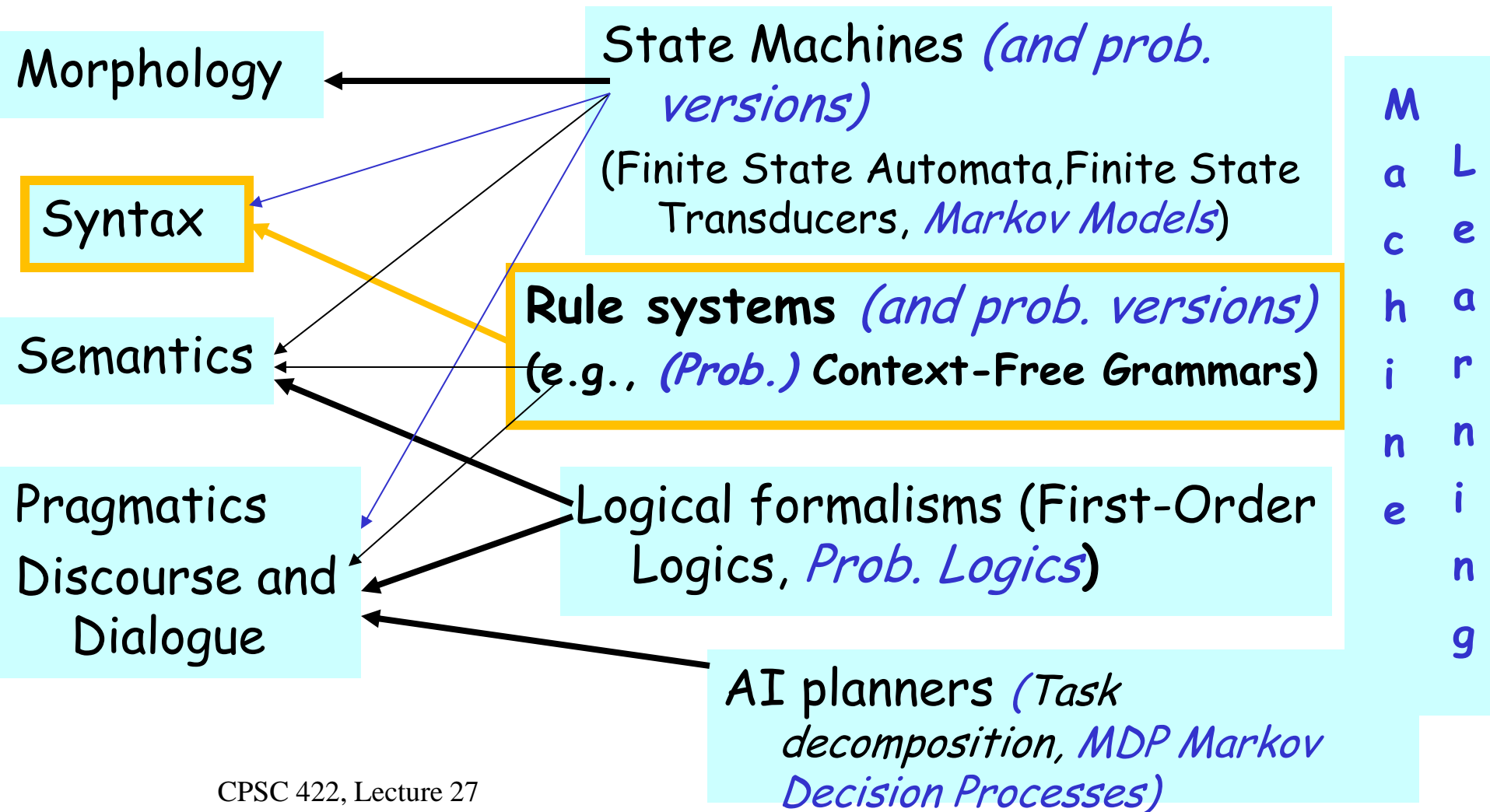


# Intelligent Systems (AI-2)

Computer Science cpsc422, Lecture 27

Nov, 16, 2015

# NLP: Knowledge-Formalisms Map (including probabilistic formalisms)



# Lecture Overview

- Recap English Syntax and Parsing
- Key Problem with parsing: Ambiguity
- Probabilistic Context Free Grammars (PCFG)
- Treebanks and Grammar Learning

# Key Constituents: Examples <sup>Head</sup>

$NP \rightarrow N$   
 $NP \rightarrow Det X$

(Specifier) **X** (Complement)

• Noun phrases (NP)

• (Det)      **N**      (PP)

the      **cat**      on the table

---

• Verb phrases (VP)

• (Qual)      **V**      (NP)

never      **eat**      a cat

---

• Prepositional phrases (PP)

• (Deg)      **P**      (NP)

almost      **in**      the net

---

• Adjective phrases (AP)

• (Deg)      **A**      (PP)

very      **happy**      about it

---

• Sentences (S)

• (NP)      (-)      (VP)

a mouse      --      ate it

# Context Free Grammar (CFG)

- 4-tuple (non-term., term., productions, start)
- $(N, \Sigma, P, S)$
- $P$  is a set of rules  $A \rightarrow \alpha$ ;  $A \in N$ ,  $\alpha \in (\Sigma \cup N)^*$

$N = \{X, Y\}$     $\Sigma = \{a, b, c\}$     $P =$

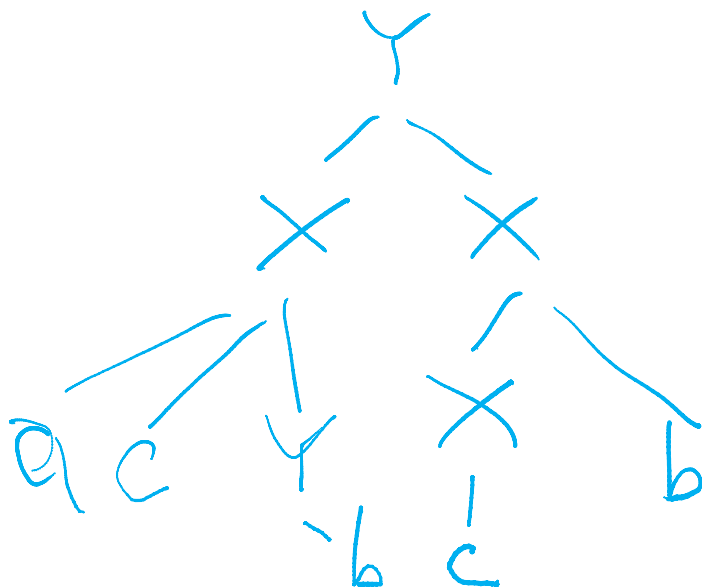
$X \rightarrow Xb$

$Y \rightarrow XX$

$X \rightarrow acY$

$X \rightarrow c$

$Y \rightarrow b$



# CFG Example

## Grammar with example phrases

## Lexicon

$S \rightarrow NP VP$

I + want a morning flight

$NP \rightarrow Pronoun$

I

$NP \rightarrow Proper-Noun$

Los Angeles

$\rightarrow NP \rightarrow Det Nominal$

a + flight

$Nominal \rightarrow Noun Nominal$   
|  $Noun$

morning + flight  
flights

$VP \rightarrow Verb$

do

$VP \rightarrow Verb NP$

want + a flight

$VP \rightarrow Verb NP PP$

leave + Boston + in the morning

$VP \rightarrow Verb PP$

leaving + on Thursday

$PP \rightarrow Preposition NP$

from + Los Angeles

$Noun \rightarrow flights | breeze | trip | morning | \dots$

$Verb \rightarrow is | prefer | like | need | want | fly$

$Adjective \rightarrow cheapest | non-stop | first | latest | other | direct | \dots$

$Pronoun \rightarrow me | I | you | it | \dots$

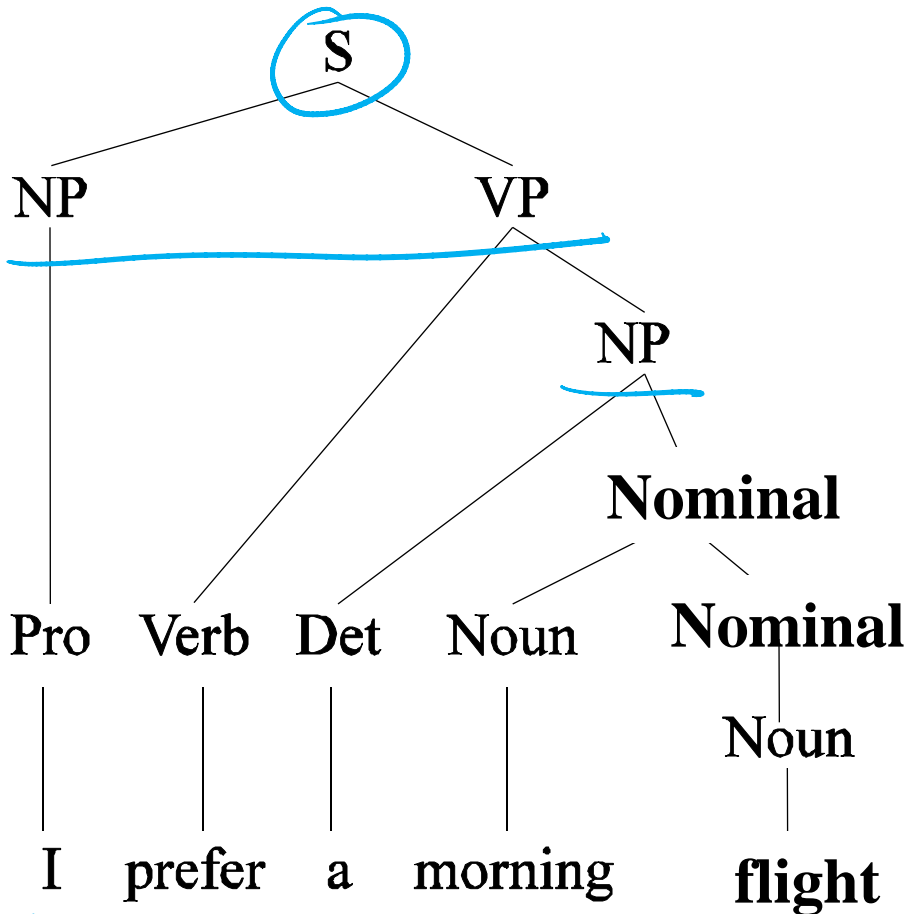
$Proper-Noun \rightarrow Alaska | Baltimore | Los Angeles | Chicago | United | American | \dots$

$Determiner \rightarrow the | a | an | this | these | that | \dots$

$Preposition \rightarrow from | to | on | near | \dots$

$Conjunction \rightarrow and | or | but | \dots$

# Derivations as Trees



$S \rightarrow NP VP$

$NP' \rightarrow Pronoun$

$NP \rightarrow Proper-Noun$

$NP \rightarrow Det Nominal$

$Nominal \rightarrow Noun Nominal$

$Nominal \rightarrow Noun$

$VP \rightarrow Verb$

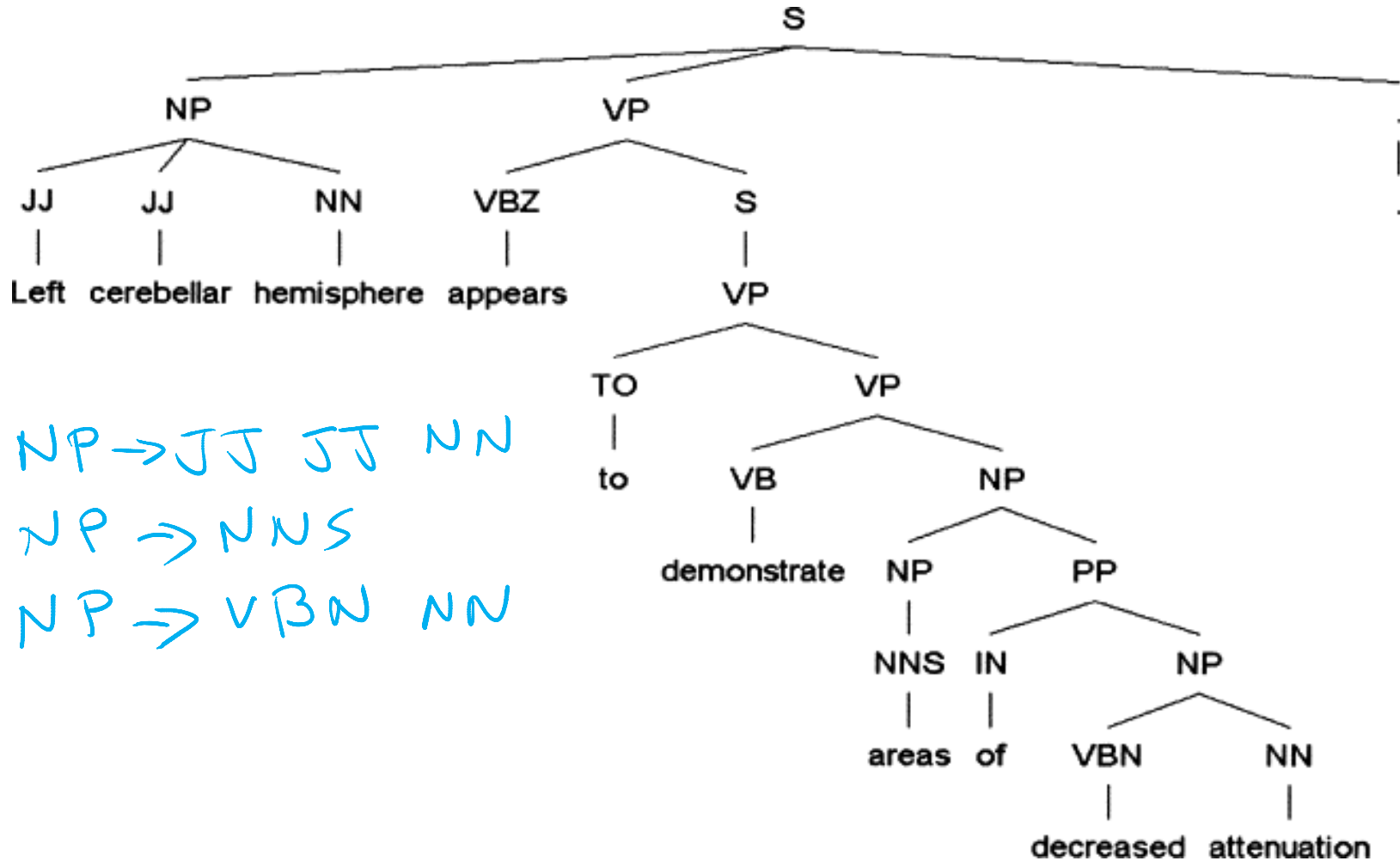
$VP \rightarrow Verb NP$

$VP \rightarrow Verb NP PP$

$VP \rightarrow Verb PP$

$PP \rightarrow Preposition NP$

# Example of relatively complex parse tree



Journal of the American Medical Informatics Association, 2005,  
Improved Identification of Noun Phrases in Clinical Radiology  
Reports Using a High-Performance **Statistical Natural Language  
Parser** Augmented with the **UMLS Specialist Lexicon**



# Lecture Overview

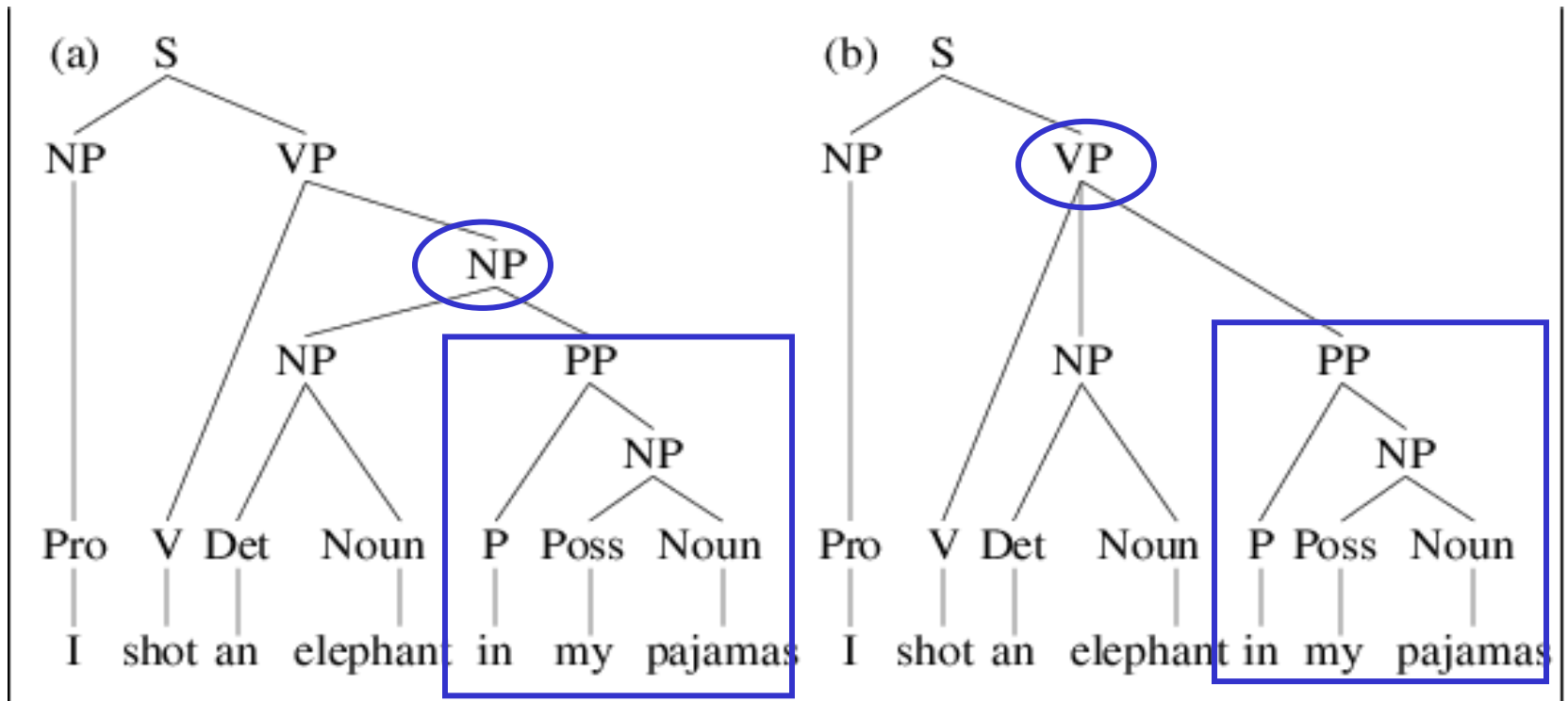
- Recap English Syntax and Parsing
- **Key Problem with parsing: Ambiguity**
- Probabilistic Context Free Grammars (PCFG)
- Treebanks and Grammar Learning

# Structural Ambiguity (Ex. 1)

VP  $\rightarrow$  V NP ; NP  $\rightarrow$  NP PP

VP  $\rightarrow$  V NP PP

*"I shot an elephant in my pajamas"*



# Structural Ambiguity (Ex.2)

"I saw **Mary passing by cs2**"

(ROOT  
(S  
(NP (PRP I))  
(VP (VBD saw)  
(S  
(NP (NNP Mary))  
(VP (VBG passing)  
(PP (IN by)  
(NP (NNP cs2))))))))

"I saw **Mary passing by cs2**"

(ROOT  
(S  
(NP (PRP I))  
(VP (VBD saw)  
(NP (NNP Mary))  
(S  
(VP (VBG passing)  
(PP (IN by)  
(NP (NNP cs2))))))))

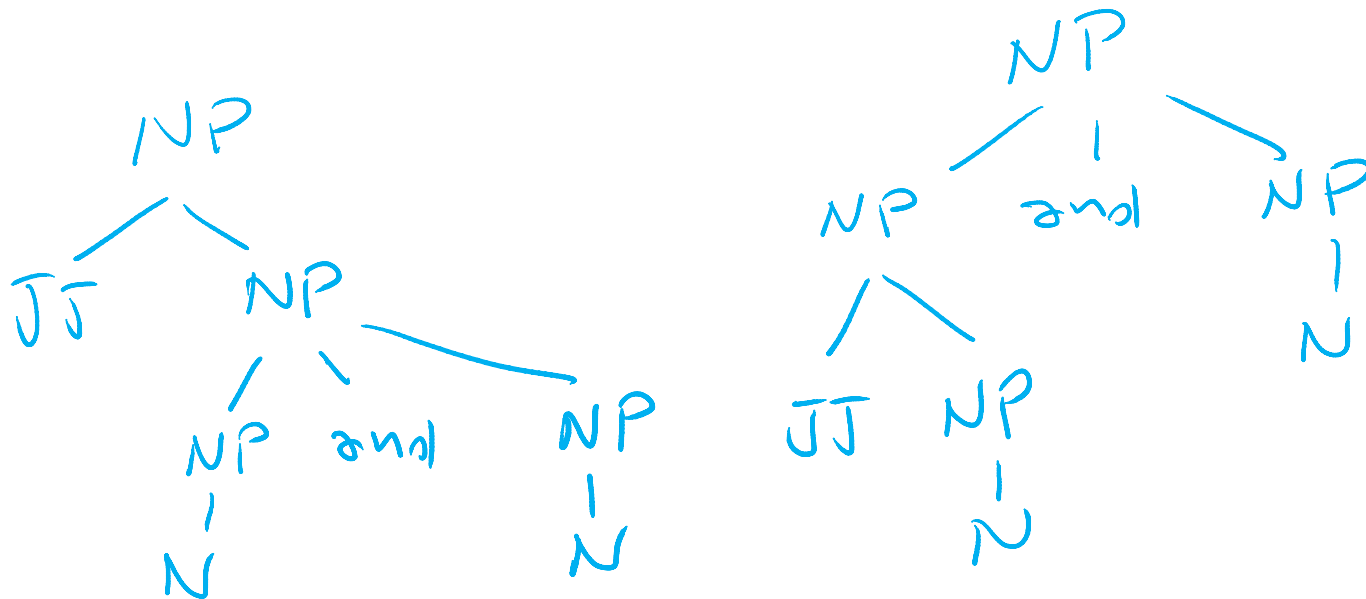
# Structural Ambiguity (Ex. 3)

- Coordination "new student and profs"  
JJ      N                      N

NP → NP and NP

NP → JJ NP

NP → N



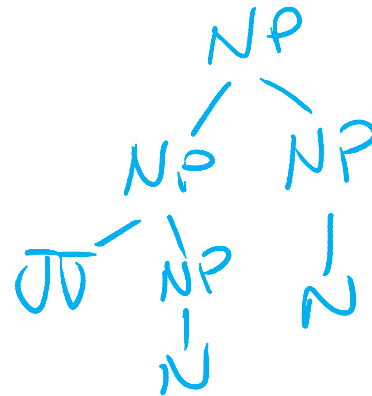
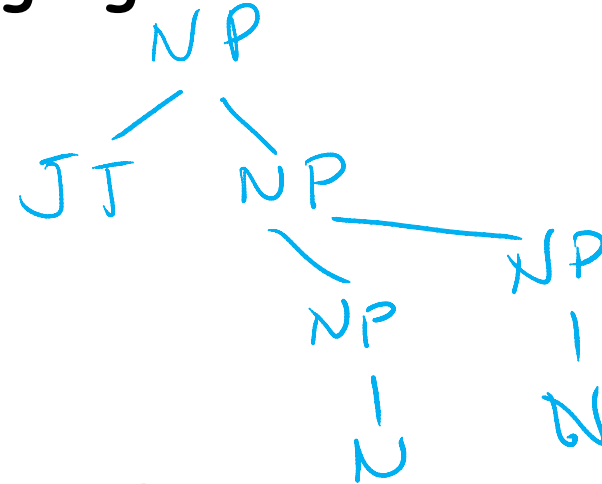
# Structural Ambiguity (Ex. 4)

- NP-bracketing "French language teacher"

NP  $\rightarrow$  JJ NP

NP  $\rightarrow$  N

NP  $\rightarrow$  NP NP



# Lecture Overview

- Recap English Syntax and Parsing
- Key Problem with parsing: Ambiguity
- **Probabilistic Context Free Grammars (PCFG)**
- Treebanks and Grammar Learning (acquiring the probabilities)
- Intro to Parsing PCFG

# Probabilistic CFGs (PCFGs)

- **GOAL:** assign a probability to parse trees and to sentences
- Each grammar rule is augmented with a conditional probability

- If these are all the rules for VP and .55 is the  $P(\text{VP} \rightarrow \text{Verb} \mid \text{VP})$

VP  $\rightarrow$  Verb .55

VP  $\rightarrow$  Verb NP .40

VP  $\rightarrow$  Verb NP NP ??

- What ?? should be ?

A. 1

B. 0

C. .05

D. None of the above

iclicker.

# Probabilistic CFGs (PCFGs)

- **GOAL:** assign a probability to parse trees and to sentences
- Each grammar rule is augmented with a conditional probability
- The expansions for a given non-terminal sum to 1

VP  $\rightarrow$  Verb

VP  $\rightarrow$  Verb NP

VP  $\rightarrow$  Verb NP NP

.55

.40

.05

$P(\text{VP} \rightarrow \text{Verb} \mid \text{VP})$

$P(\text{VP} \rightarrow \text{Verb NP} \mid \text{VP})$

$P(\text{VP} \rightarrow \text{Verb NP NP} \mid \text{VP})$

**Formal Def:** 5-tuple  $(N, \Sigma, P, S, D)$



# Sample PCFG

$S \rightarrow NP VP$	[.80]	$Det \rightarrow that$	[.05]	$the$	[.80]	$a$	[.15]
$S \rightarrow Aux NP VP$	[.15]	$Noun \rightarrow book$	[.10]				
$S \rightarrow VP$	[.05]	$Noun \rightarrow flights$	[.50]				
$NP \rightarrow Det Nom$	[.20]	$Noun \rightarrow meal$	[.40]				
$NP \rightarrow Proper-Noun$	[.35]	$Verb \rightarrow book$	[.30]				
$NP \rightarrow Nom$	[.05]	$Verb \rightarrow include$	[.30]				
$NP \rightarrow Pronoun$	[.40]	$Verb \rightarrow want$	[.40]				
$Nom \rightarrow Noun$	[.75]	$Aux \rightarrow can$	[.40]				
$Nom \rightarrow Noun Nom$	[.20]	$Aux \rightarrow does$	[.30]				
$Nom \rightarrow Proper-Noun Nom$	[.05]	$Aux \rightarrow do$	[.30]				
$VP \rightarrow Verb$	[.55]	$Proper-Noun \rightarrow TWA$	[.40]				
$VP \rightarrow Verb NP$	[.40]	$Proper-Noun \rightarrow Denver$	[.40]				
$VP \rightarrow Verb NP NP$	[.05]	$Pronoun \rightarrow you$	[.40]	$I$	[.60]		

# PCFGs are used to....

- Estimate Prob. of parse tree

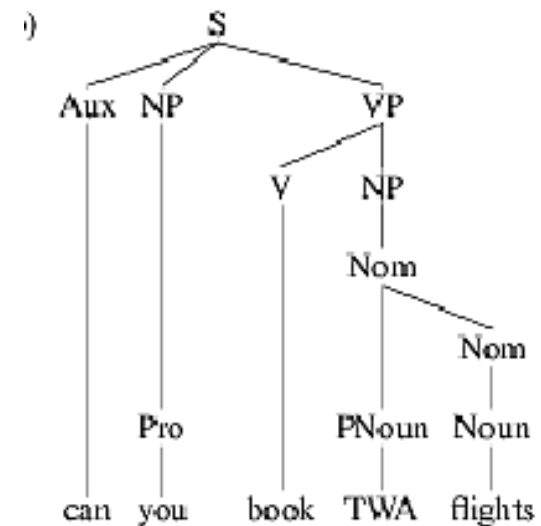
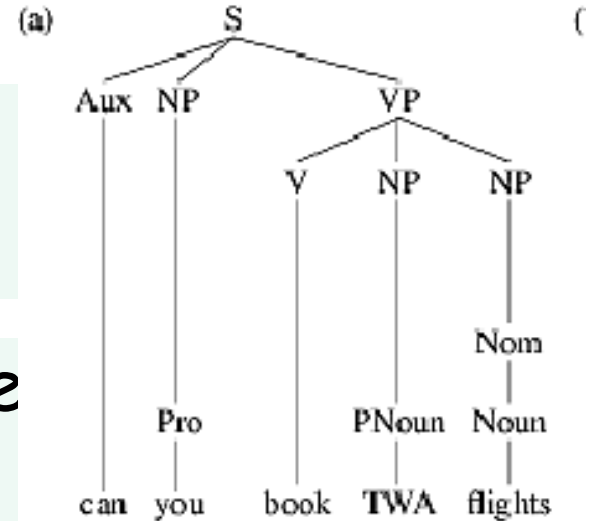
A. Sum of the probs of all the rules applied

B. Product of the probs of all the rules applied

- Estimate Prob. of a sentence

A. Sum of the probs of all the parse trees

B. Product of the probs of all the parse trees



# PCFGs are used to....

- Estimate Prob. of parse tree

$$P(\text{Tree}) = \prod_{\text{node} \in \text{Tree}} P(\text{expansion for node})$$

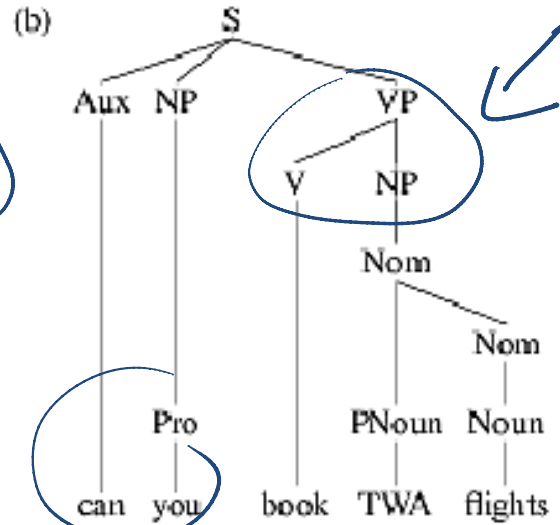
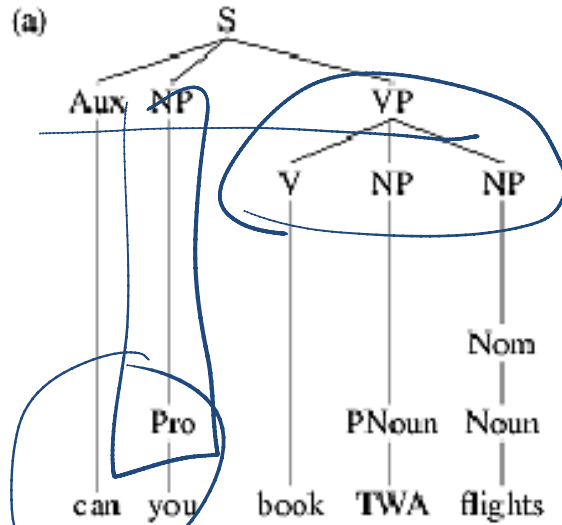
- Estimate Prob. to sentences

$$P(\text{Sentence}) = \sum_{\text{Tree} \in \text{Sentence parses}} P(\text{Tree})$$

# Example

$$P(\text{Tree}^a) = .15 * .4 * \dots = 1.5 \times 10^{-6}$$

$$P(\text{Tree}^b) = .15 * .4 * \dots = 1.7 \times 10^{-6}$$



$$P(\text{"Can you...."}) = 1.7 \times 10^{-6} + 1.5 \times 10^{-6} = 3.2 \times 10^{-6}$$

Rules	P	Rules	P
S → Aux NP VP	.15	S → Aux NP VP	.15
NP → Pro	.40	NP → Pro	.40
VP → V NP NP	.05	VP → V NP	.40
NP → Nom	.05	NP → Nom	.05
NP → PNoun	.35	Nom → PNoun Nom	.05
Nom → Noun	.75	Nom → Noun	.75
Aux → Can	.40	Aux → Can	.40
NP → Pro	.40	NP → Pro	.40
Pro → you	.40	Pro → you	.40
Verb → book	.30	Verb → book	.30
PNoun → TWA	.40	PNoun → TWA	.40
Noun → flights	.50	Noun → flights	.50

# Lecture Overview

- Recap English Syntax and Parsing
- Key Problem with parsing: Ambiguity
- Probabilistic Context Free Grammars (PCFG)
- **Treebanks and Grammar Learning (acquiring the probabilities)**

# Treebanks

- DEF. corpora in which each sentence has been paired with a parse tree
- These are generally created
  - Parse collection with parser
  - human annotators revise each parse
- Requires detailed annotation guidelines
  - POS tagset
  - Grammar
  - instructions for how to deal with particular grammatical constructions.



# Treebank Grammars

- Such grammars tend to contain lots of rules....
- For example, the Penn Treebank has 4500 different rules for VPs! Among them...

VP → VBD PP

VP → VBD PP PP

VP → VBD PP PP PP

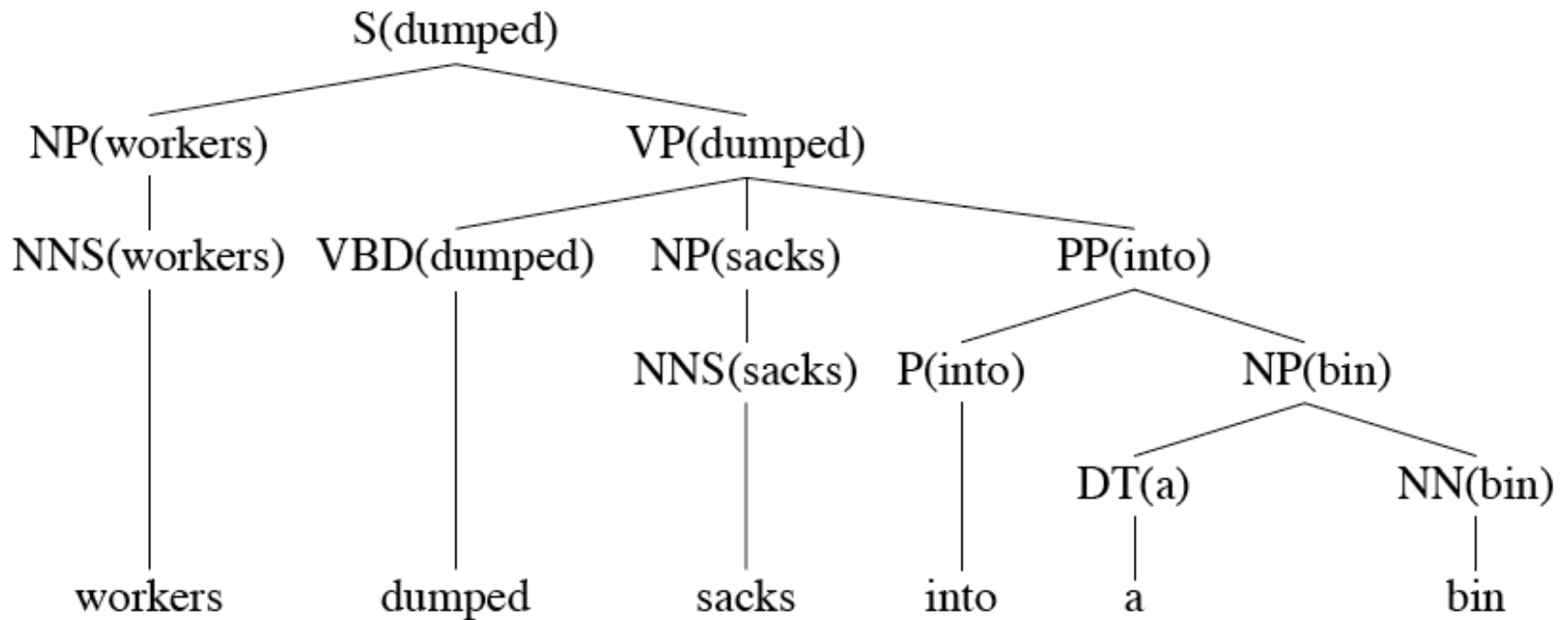
VP → VBD PP PP PP PP



# Heads in Trees

- Finding heads in treebank trees is a task that arises frequently in many applications.
  - Particularly important in **statistical parsing**
- We can visualize this task by annotating the nodes of a parse tree with the heads of each corresponding node.

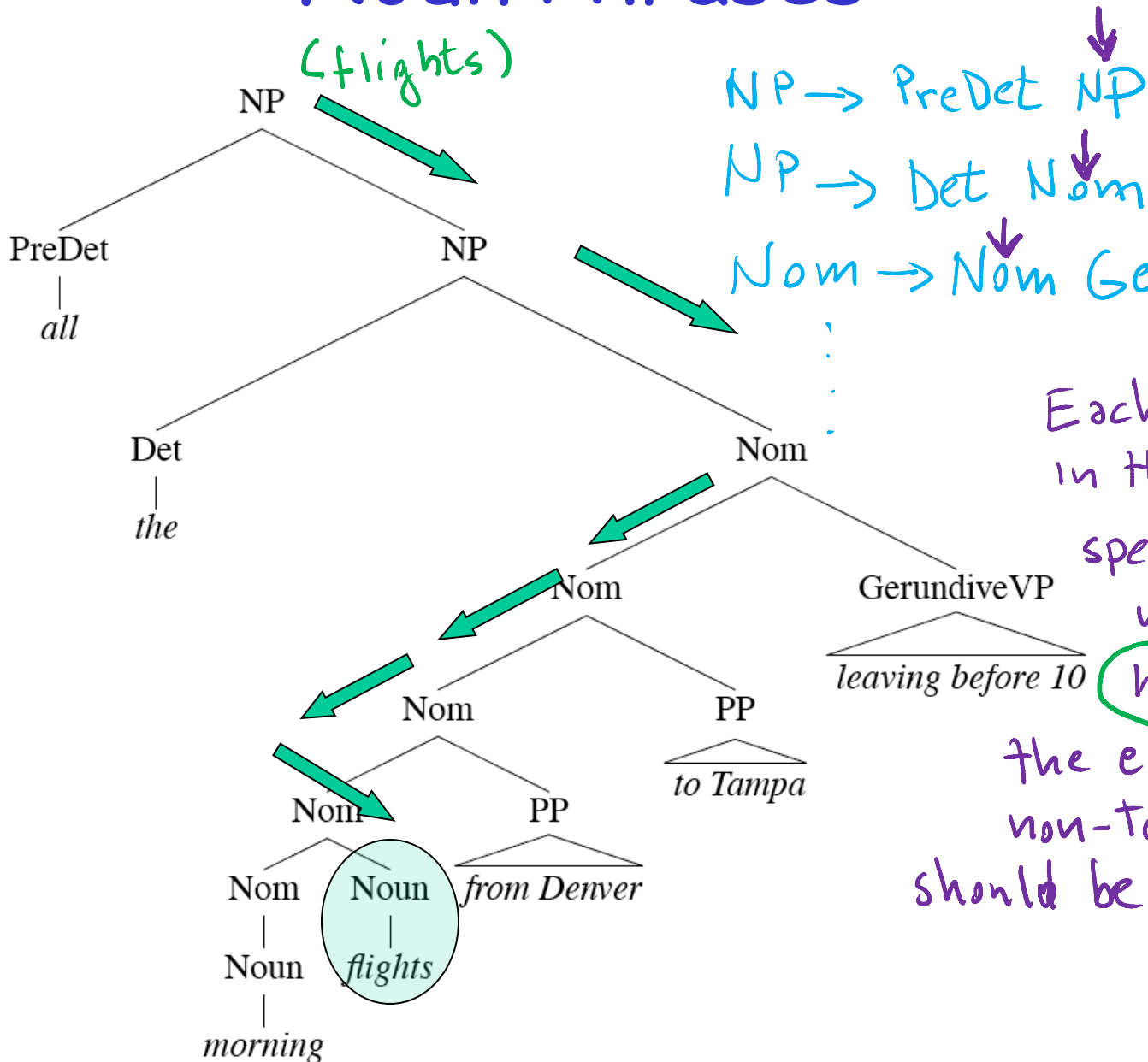
# Lexically Decorated Tree



# Head Finding

- The standard way to do head finding is to use a simple set of tree traversal rules specific to each non-terminal in the grammar.
- Each rule in the PCFG specifies where the head of the expanded non-terminal should be found

# Noun Phrases



# Acquiring Grammars and Probabilities

Manually parsed text corpora (e.g., PennTreebank)

- **Grammar:** read it off the parse trees

Ex: if an NP contains an ART, ADJ, and NOUN then we create the rule  $NP \rightarrow ART ADJ NOUN$ .

- **Probabilities:**

$$P(A \rightarrow \alpha | A) = \frac{\overset{NP \rightarrow Pro}{\text{count}(A \rightarrow \alpha)}}{\sum_{\forall \beta} \text{count}(A \rightarrow \beta)} = \frac{\text{count}(A \rightarrow \alpha)}{\text{count}(A)}$$

Ex: if the  $NP \rightarrow ART ADJ NOUN$  rule is used 50 times and all NP rules are used 5000 times, then the rule's probability is ...  $.01$

# Example

if you look at all the parse trees in the bank you find three rules for NP

① NP → ART ADJ NOUN

How many times

50

② NP → NOUN

4000

③ NP → PRONOUN

950

5000

total #  
of NP  
expansions

$$P(\textcircled{1} | \text{NP}) = 50/5000 = .01$$

$$P(\textcircled{2} | \text{NP}) = 4000/5000 = .8$$

$$P(\textcircled{3} | \text{NP}) = 950/5000 = .19$$

$$\boxed{\text{also} = 1 - (.01 + .8)}$$

# Learning Goals for today's class

## You can:

- Provide a formal definition of a PCFG
- Apply a PCFG to compute the probability of a parse tree of a sentence as well as the probability of a sentence
- Describe the content of a treebank
- Describe the process to identify a head of a syntactic constituent
- Compute the probability distribution of a PCFG from a treebank

# Next class on Wed

- Parsing Probabilistic CFG: CKY parsing
- PCFG in practice: Modeling Structural and Lexical Dependencies

Assignment-3 due on Fri  
Assignment-4 out same day