

# Intelligent Systems (AI-2)

## Computer Science cpsc422, Lecture 19

Oct, 23, 2015



Slide Sources

*Raymond J. Mooney University of Texas at Austin*

*D. Koller, Stanford CS - Probabilistic Graphical Models*

*D. Page, Whitehead Institute, MIT*

Several Figures from

“Probabilistic Graphical Models: Principles and Techniques” *D. Koller, N. Friedman* 2009

CPSC 422, Lecture 19

Slide 1

# Lecture Overview

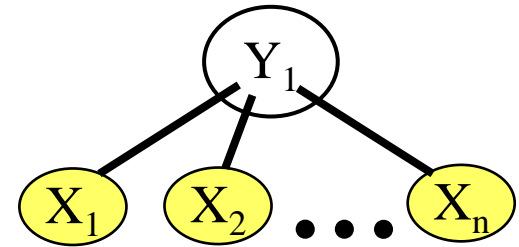
- Recap: Naïve Markov – Logistic regression (simple CRF)
- CRFs: high-level definition
- CRFs Applied to sequence labeling
- NLP Examples: Name Entity Recognition, joint POS tagging and NP segmentation

# Let's derive the probabilities we need

$$\phi_i(X_i, Y_1) = \exp\{w_i \mathbb{1}\{X_i = 1, Y_1 = 1\}\}$$

how strongly  $Y_1 = 1$  given that  $X_i = 1$

$$\phi_0(Y_1) = \exp\{w_0 \mathbb{1}\{Y_1 = 1\}\}$$



$$\tilde{P}(Y_1 = 1, X_1, X_2, \dots, X_n) = \phi_0(Y_1) * \prod_{i=1}^n \phi_i(X_i, Y_1)$$

example

$$P(Y_1 = 1, X_1 = 0, X_2 = 1, X_3 = 1)$$

$$e^{w_0 * 1} * e^{w_1 * 0} * e^{w_2 * 1} * e^{w_3 * 1}$$

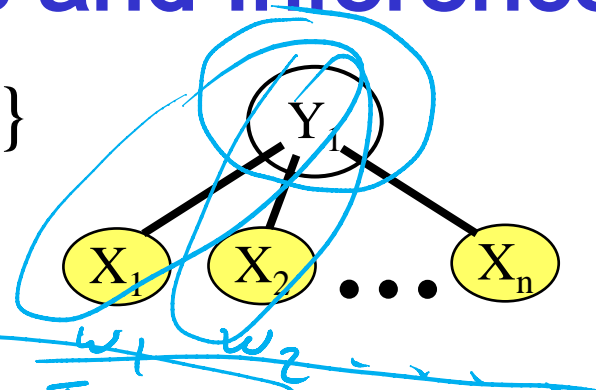
$$e^{w_0} * e^{w_1 * x_1} * e^{w_2 * x_2} * e^{w_3 * x_3} =$$

$$= e^{w_0 + \sum w_i x_i}$$

# Naïve Markov Parameters and Inference

$$\phi_i(X_i, Y_1) = \exp\{w_i \mathbb{1}\{X_i = 1, Y_1 = 1\}\}$$

$$\phi_0(Y_1) = \exp\{w_0 \mathbb{1}\{Y_1 = 1\}\}$$



$$\tilde{P}(Y_1, \underbrace{x_1, \dots, x_n}_{\text{always observed}}) = \phi_0(Y_1) \prod_{i=1}^n \phi_i(X_i | Y_1)$$

$$\tilde{P}(Y_1 = 1, x_1, \dots, x_n) = \exp(w_0 + \sum_{i=1}^n w_i x_i)$$

$$\tilde{P}(Y_1 = 0, x_1, \dots, x_n) = 1$$

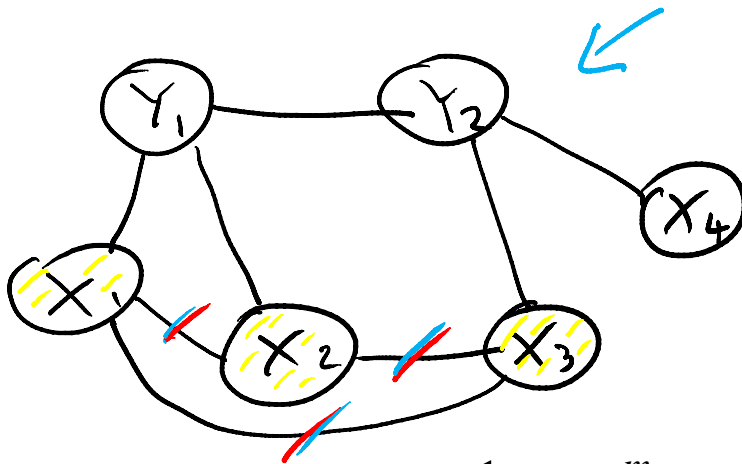
$$P(Y_1 | x_1, \dots, x_n) = \left\{ \begin{array}{l} \frac{e^z}{1 + e^z} \quad Y_1 = 1 \\ \frac{1}{1 + e^z} \quad Y_1 = 0 \end{array} \right\}$$

# Let's generalize ....

Assume that you always observe a set of variables  $X = \{X_1 \dots X_n\}$  and you want to predict one or more variables  $Y = \{Y_1 \dots Y_k\}$

A **CRF** is an undirected graphical model whose nodes corresponds to  $X \cup Y$ .

$\phi_1(D_1) \dots \phi_m(D_m)$  represent the factors which annotate the network (but we disallow factors involving only vars in  $X$  – why?)



They would be

A. too large

B. constant

C. difficult to acquire

iclicker.

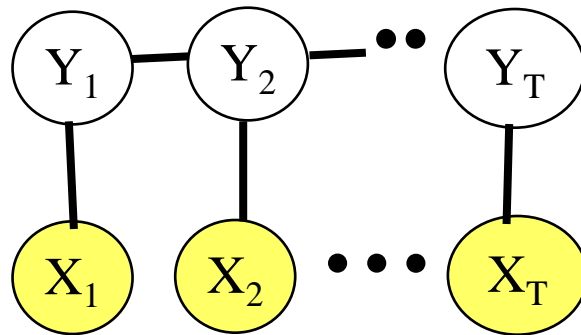
$$P(Y | X) = \frac{1}{Z(X)} \left( \prod_{i=1}^m \phi_i(D_i) \right)$$

$$Z(X) = \sum_Y \left( \prod_{i=1}^m \phi_i(D_i) \right)$$

# Lecture Overview

- Recap: Naïve Markov – Logistic regression (simple CRF)
- CRFs: high-level definition
- **CRFs Applied to sequence labeling**
- NLP Examples: Name Entity Recognition, joint POS tagging and NP segmentation

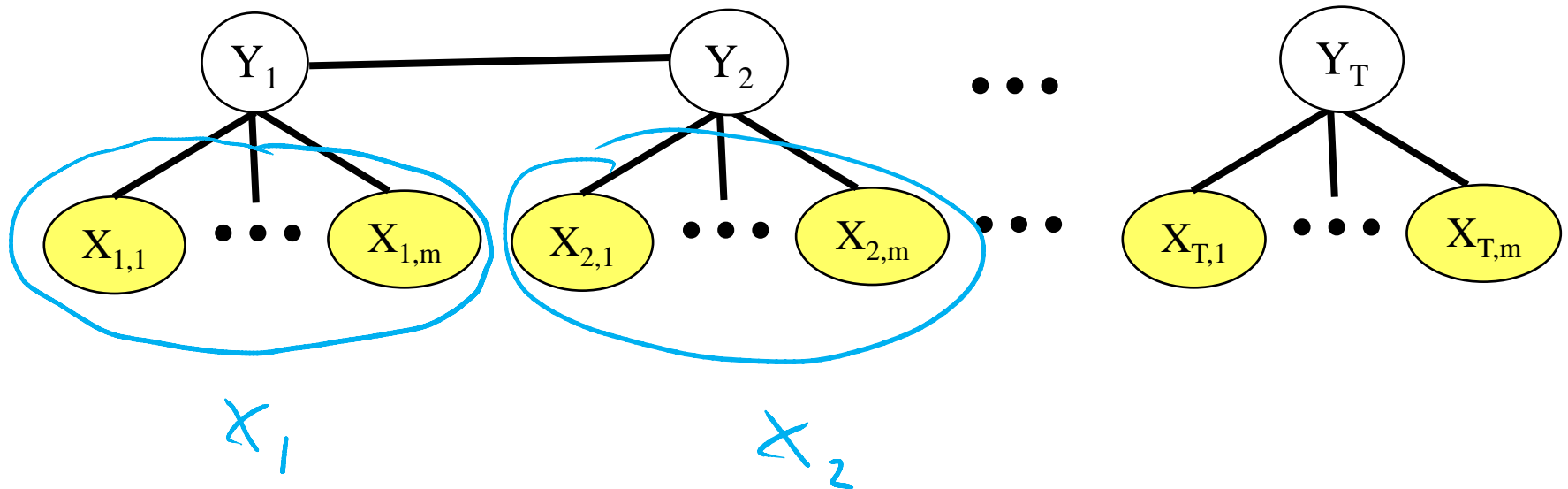
# Sequence Labeling



**Linear-chain CRF**

# Increase representational Complexity: Adding Features to a CRF

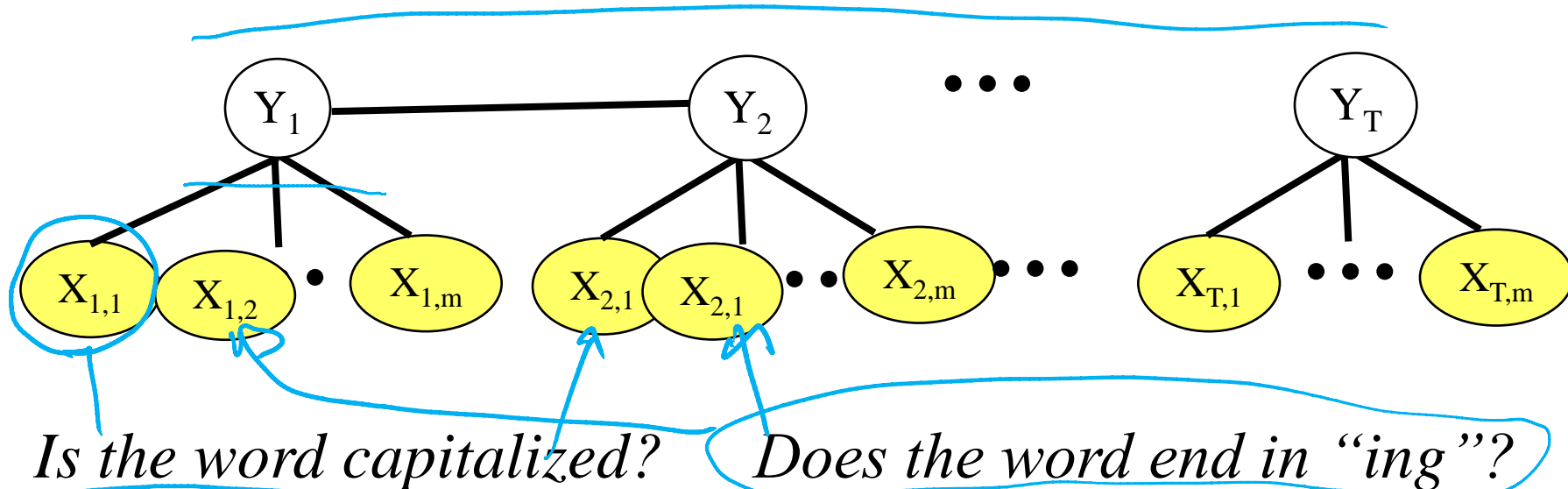
- Instead of a single observed variable  $X_i$  we can model multiple features  $X_{ij}$  of that observation.





# CRFs in Natural Language Processing

- One target variable  $Y$  for each word  $X$ , encoding the possible labels for  $X$
- Each target variable is connected to a set of feature variables that capture properties relevant to the target distinction



# Name Entity Recognition Task

- Entity often span multiple words *“British Columbia”*
- Type of an entity may not be apparent for individual words *“University of British Columbia”*
- Let’s assume three categories: *Person, Location, Organization*
- BIO notation (for sequence labeling)

possible labels    B-PER    I-PER    B-LOC    I-LOC  
                          B-ORG    I-ORG            OTHER

O            B-ORG            I-ORG    I-ORG            I-ORG  
The University of British Columbia

O    O            B-LOC                    I-LOC  
is in Vancouver B.C.

# Linear chain CRF parameters

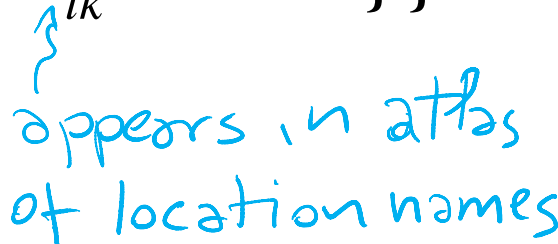
With two factors “types” for each word

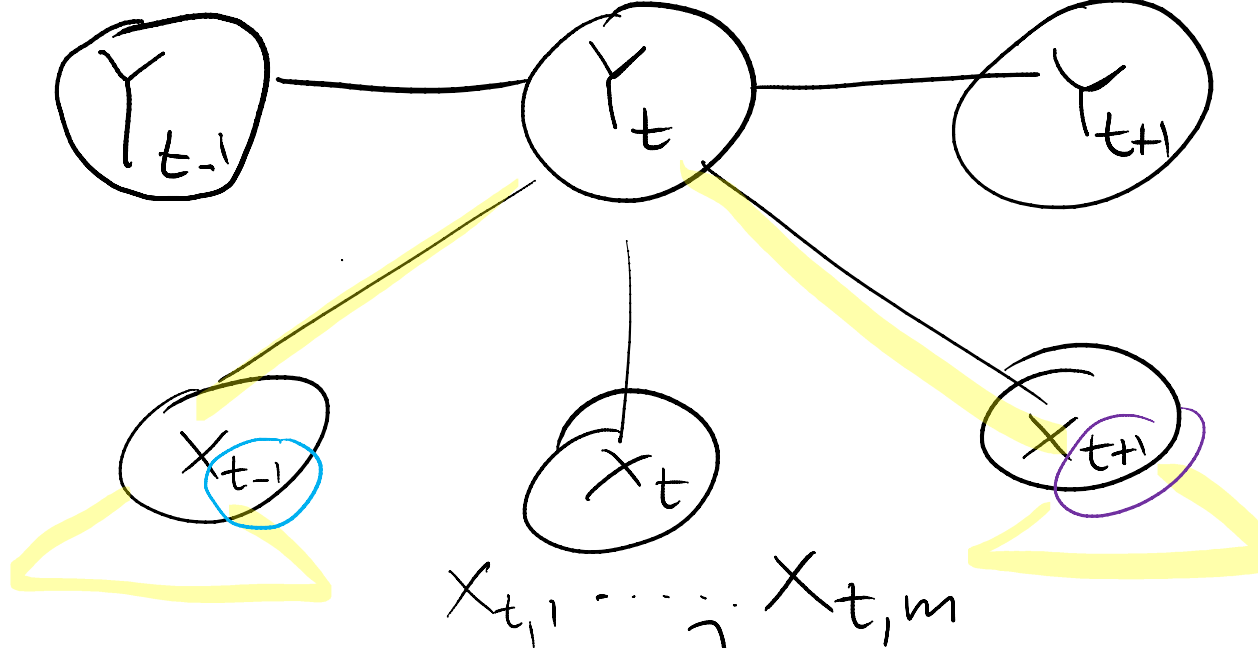
$\phi_t^1(Y_t, Y_{t-1}) \phi_t^1(Y_t, Y_{t+1})$  Dependency between neighboring target vars 

$\phi_t^2(Y_t, X_1, \dots, X_T)$  Dependency between target variable and its context in the word sequence, which can include also **features of the words** (capitalized, appear in an atlas of location names, etc.)

Factors are similar to the ones for the Naïve Markov (logistic regression)

$$\phi_t(Y_t, X_{tk}) = \exp\{w_{tk} \times \uparrow \{Y_t = \text{I-LOC}, X_{tk} = 1\}\}$$





$X_{t,1} \dots X_{t,m}$

$\uparrow \{ Y_t = I-ORG, X_{t,k} = \text{"Times"} \}$

$\uparrow \{ Y_t = I-PER, X_{t+1,k} = \text{"spoke"} \}$

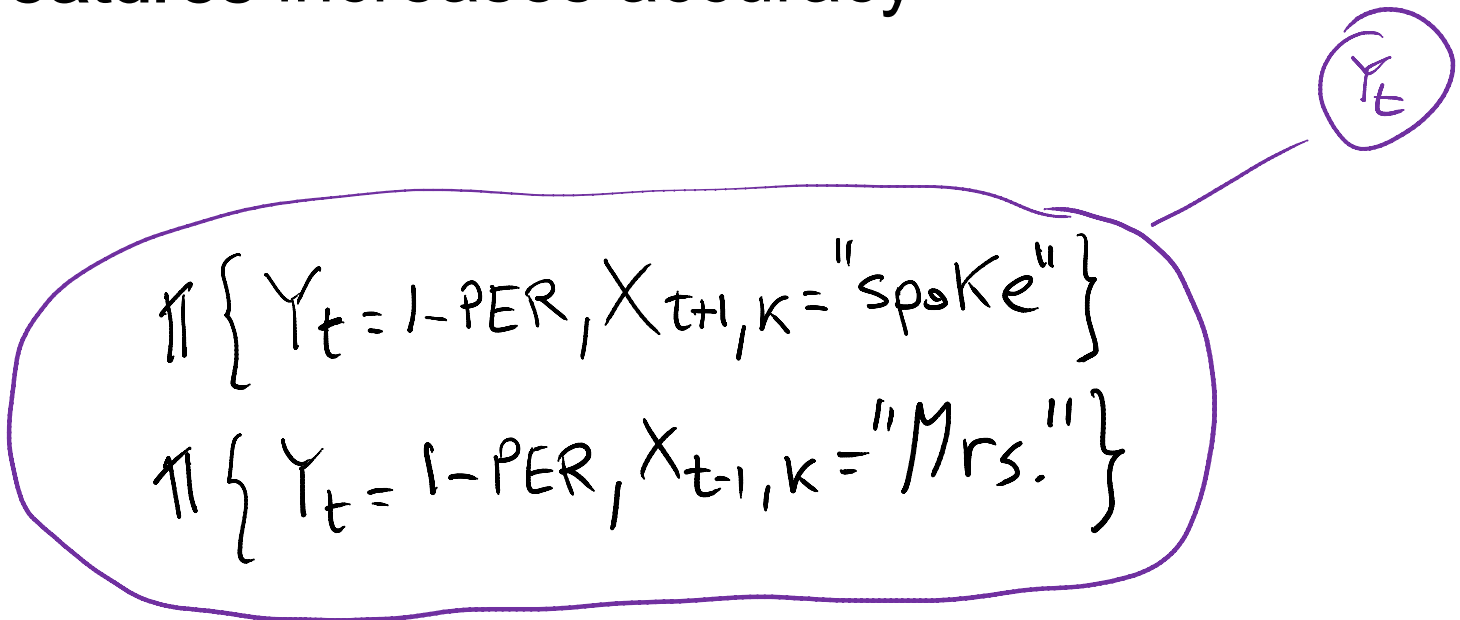
$\uparrow \{ Y_t = I-PER, X_{t-1,k} = \text{"Mrs."} \}$

**Features can also be**

- The word
- Following word
- Previous word

# More on features

Including features that are **conjunctions of simple features** increases accuracy


$$\pi \left\{ Y_t = 1\text{-PER}, X_{t+1, k} = \text{"spoke"} \right\}$$

$$\pi \left\{ Y_t = 1\text{-PER}, X_{t-1, k} = \text{"Mrs."} \right\}$$

Total number of features can be  $10^5$ - $10^6$

However features are sparse i.e. most features are 0 for most words

# Linear-Chain Performance

Per-token/word accuracy in the high 90% range for many natural datasets

Per-field precision and recall are more often around 80-95% , depending on the dataset. Entire Named Entity Phrase must be correct

O B-ORG I-ORG ~~B-LOC~~ ~~I-LOC~~  
The University of British Columbia X

O O B-LOC I-LOC  
is in Vancouver B.C. ✓

iclicker.

Per-word accuracy?

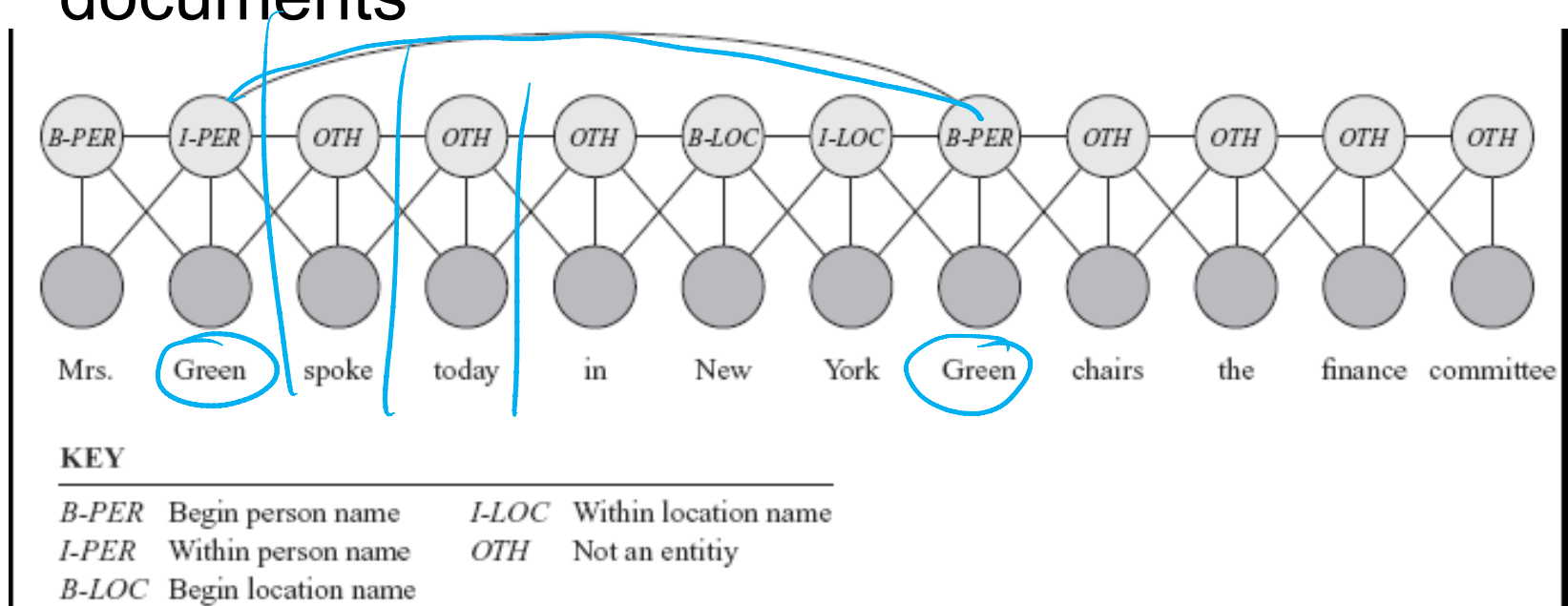
Per-field precision?

A.	B	C.
$\frac{1}{2}$	$\frac{7}{9}$	$\frac{7}{9}$
$\frac{1}{2}$	$\frac{3}{9}$	$\frac{1}{2}$

# Skip-Chain CRFs

Include additional factors that connect non-adjacent target variables

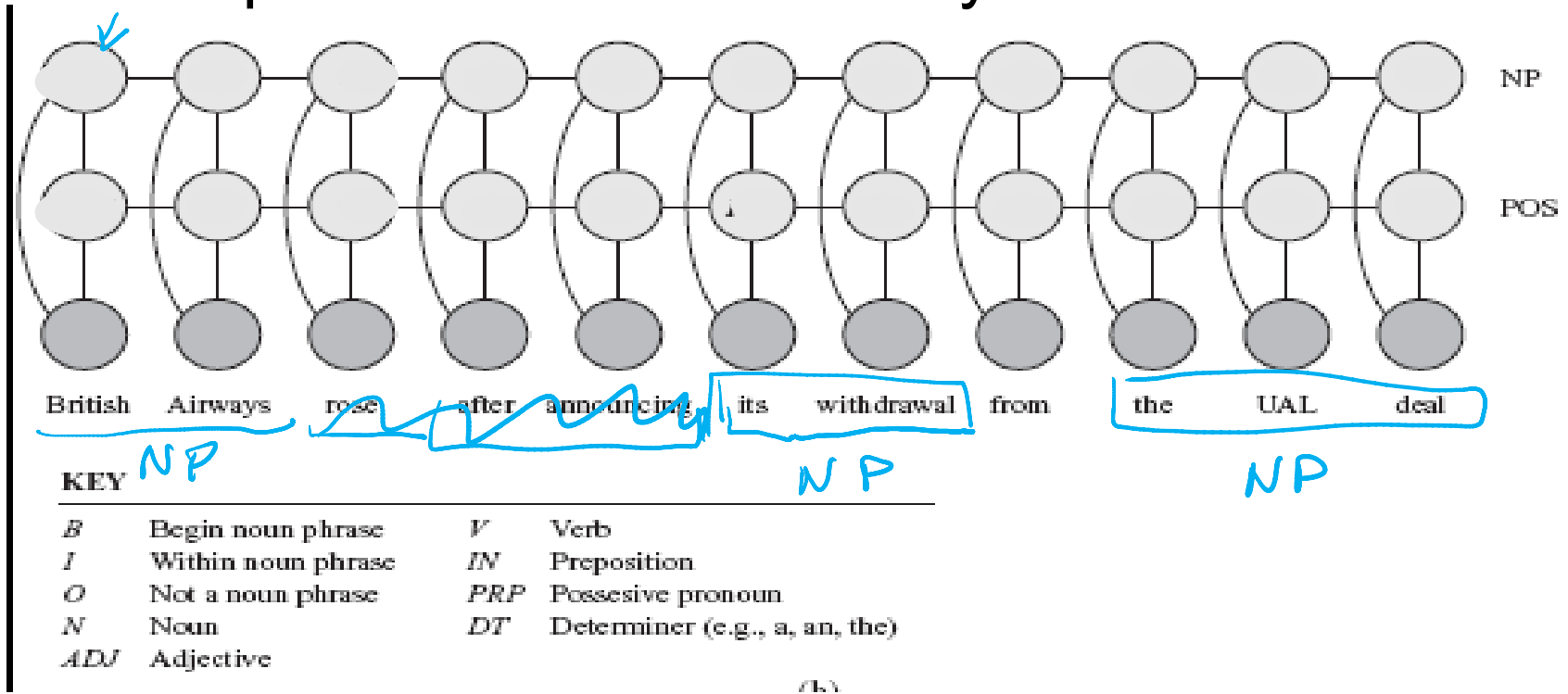
E.g., When a word occur multiple times in the same documents



Graphical structure over  $Y$  can depend on the values of the  $Xs$  ! CPSC 422, Lecture 19

# Coupled linear-chain CRFs

- Linear-chain CRFs can be combined to perform multiple tasks simultaneously

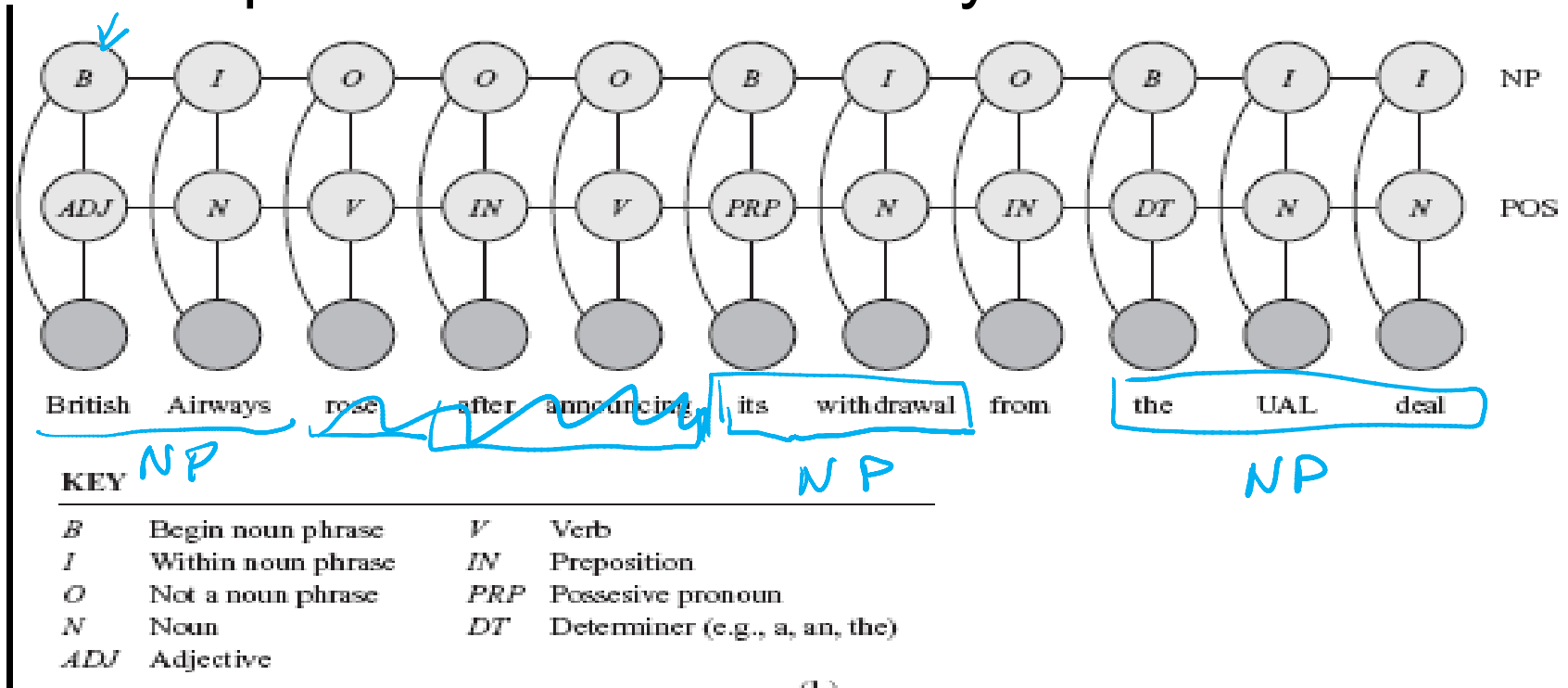


- Performs part-of-speech labeling and noun-phrase segmentation



# Coupled linear-chain CRFs

- Linear-chain CRFs can be combined to perform multiple tasks simultaneously



- Performs part-of-speech labeling and noun-phrase segmentation

# Inference in CRFs (just intuition)

An HMM can be viewed as a factor graph  
 $p(\mathbf{y}, \mathbf{x}) = \prod_t \Psi_t(y_t, y_{t-1}, x_t)$  where  $Z = 1$ , and the factors are defined as:  
$$\Psi_t(j, i, x) \stackrel{\text{def}}{=} p(y_t = j | y_{t-1} = i) p(x_t = x | y_t = j). \quad (4.1)$$

Forward / Backward / Smoothing and Viterbi can be rewritten (not trivial!) using these factors

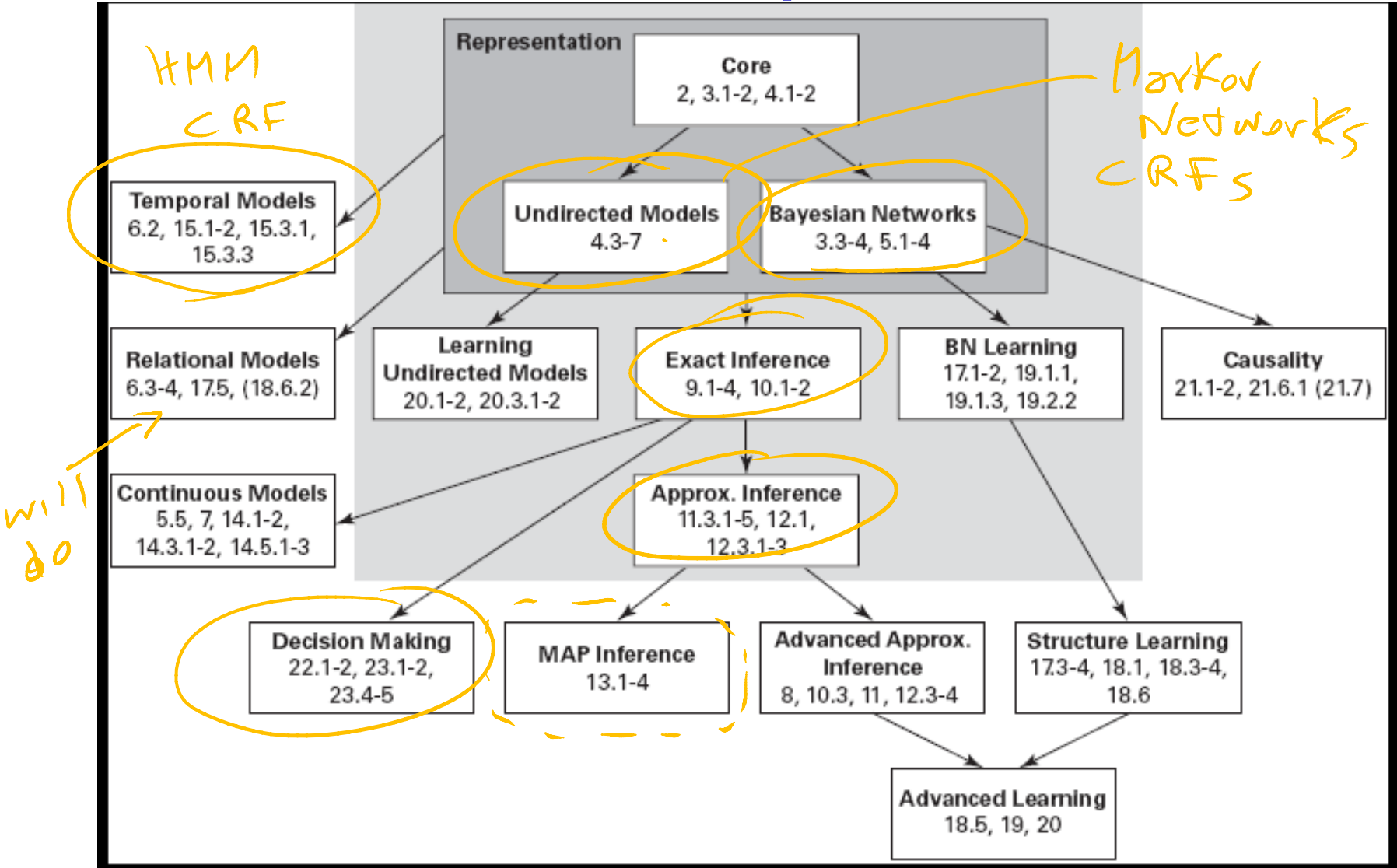
Then you plug in the factors of the CRFs and all the algorithms work fine with CRFs! 😊

# CRFs Summary

- Ability to relax strong independence assumptions
- Ability to incorporate arbitrary overlapping local and global features
- Graphical structure over  $Y$  can depend on the values of the  $X$ s
- Can perform multiple tasks simultaneously
- *Standard Inference algorithm* for HMM can be applied
- *Practical Learning algorithms exist*
- State-of-the-art on many labeling tasks (*deep learning recently shown to be often better ... ensemble them?*)

See MALLET package

# Probabilistic Graphical Models



From "Probabilistic Graphical Models: Principles and Techniques" D. Koller, N. Friedman 2009

# 422 big picture: Where are we?

Hybrid: Det +Sto

*Prob CFG*

*Prob Relational Models*

*Markov Logics*

Deterministic

Stochastic

Query	<i>Logics</i> <i>First Order Logics</i>	<i>Belief Nets</i> Approx. : Gibbs
	<i>Ontologies</i> <i>Temporal rep.</i>	<i>Markov Chains and HMMs</i> Forward, Viterbi.... Approx. : Particle Filtering
Planning	<ul style="list-style-type: none"><li>• Full Resolution</li><li>• SAT</li></ul>	<i>Undirected Graphical Models</i> <i>Markov Networks</i> <i>Conditional Random Fields</i> <i>Markov Decision Processes and Partially Observable MDP</i> <ul style="list-style-type: none"><li>• Value Iteration</li><li>• Approx. Inference</li></ul> <i>Reinforcement Learning</i>

*Applications of AI*

*Representation*

Reasoning  
Technique

# Learning Goals for today's class

## **You can:**

- Provide general definition for CRF
- Apply CRFs to sequence labeling
- Describe and justify features for CRFs applied to Natural Language processing tasks
- Explain benefits of CRFs

**Midterm, Mon, Oct 26,  
we will start at 9am sharp**

## **How to prepare....**

- Work on **practice material** posted on Connect
- **Learning Goals** (look at the end of the slides for each lecture – or complete list on Connect)
- Revise all the **clicker questions** and **practice exercises**

**Extra Office Hours TODAY 11:00am - 12:30pm in the DLC**

## **Next class Wed**

- Start Logics
- Revise Logics from 322!

# Announcements

## Midterm

- Avg 73.5 Max 105 Min 30
- If score below 70 need to very seriously revise all the material covered so far
- You can pick up a printout of the solutions along with your midterm.



# Generative vs. Discriminative Models

**Generative models (like Naïve Bayes):** *not* directly designed to maximize performance on classification. They model the *joint distribution*  $P(X, Y)$ .

Classification is then done using Bayesian inference

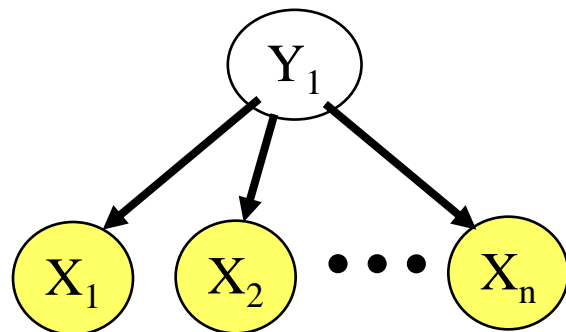
But a generative model can also be used to perform any other inference task, e.g.  $P(X_1 | X_2, \dots, X_n)$

- “Jack of all trades, master of none.”

**Discriminative models (like CRFs):** specifically designed and trained to maximize performance of classification. They only model the *conditional distribution*  $P(Y | X)$ .

By focusing on modeling the conditional distribution, they generally perform better on classification than generative models when given a reasonable amount of training data.

# Naïve Bayes vs. Logistic Regression

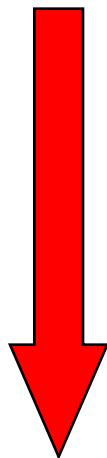


Naïve  
Bayes

$$P(Y_1, X_1, \dots, X_n)$$

**Generative**

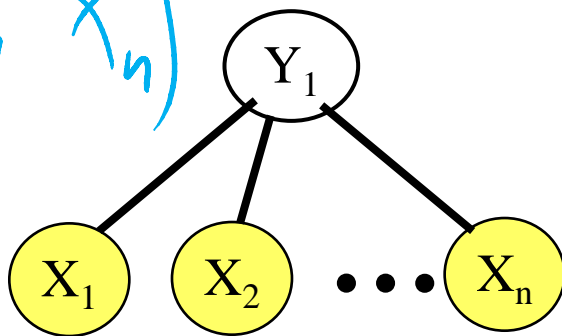
Conditional



**Discriminative**

**Logistic  
Regression (Naïve Markov)**

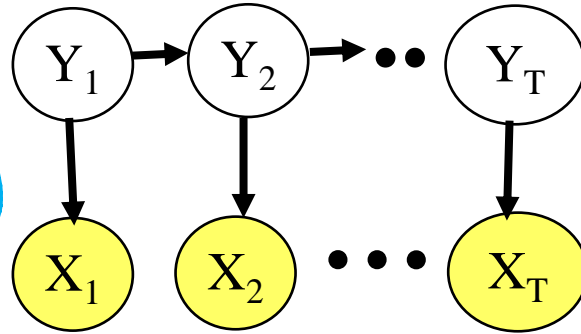
$$P(Y_1 | X_1, X_n)$$



# Sequence Labeling

models

$$P(Y_1 \dots Y_T, X_1 \dots X_T)$$



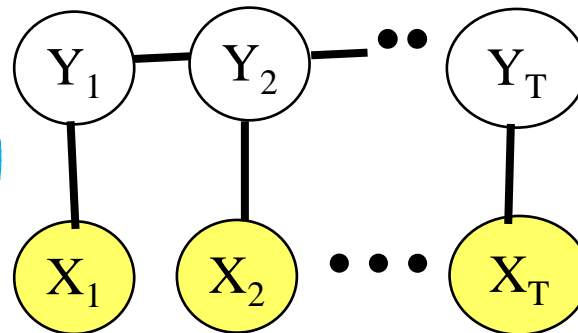
**HMM**

**Generative**

**Conditional**

models

$$P(Y_1 \dots Y_T | X_1 \dots X_T)$$



**Discriminative**

**Linear-chain CRF**