

# Search: Intro

Computer Science cpsc322, Lecture 4

*(Textbook Chpt 3.0-3.4)*

Sept, 11, 2013

# Office Hours

## Instructor

- Giuseppe Carenini ( **Fri 2-3; my office CICSR 105** )



## Teaching Assistants

- Kamyar Ardekani **Mon 2 - 3** X150 (Learning Center)



- Tatsuro Oya **Thur 10 -11** **SAME**

- Xin Ru (Nancy) Wang **Tue 2 – 3** **SAME**



# Modules we'll cover in this course: R&Rsys

First part of the course

## Environment

Deterministic

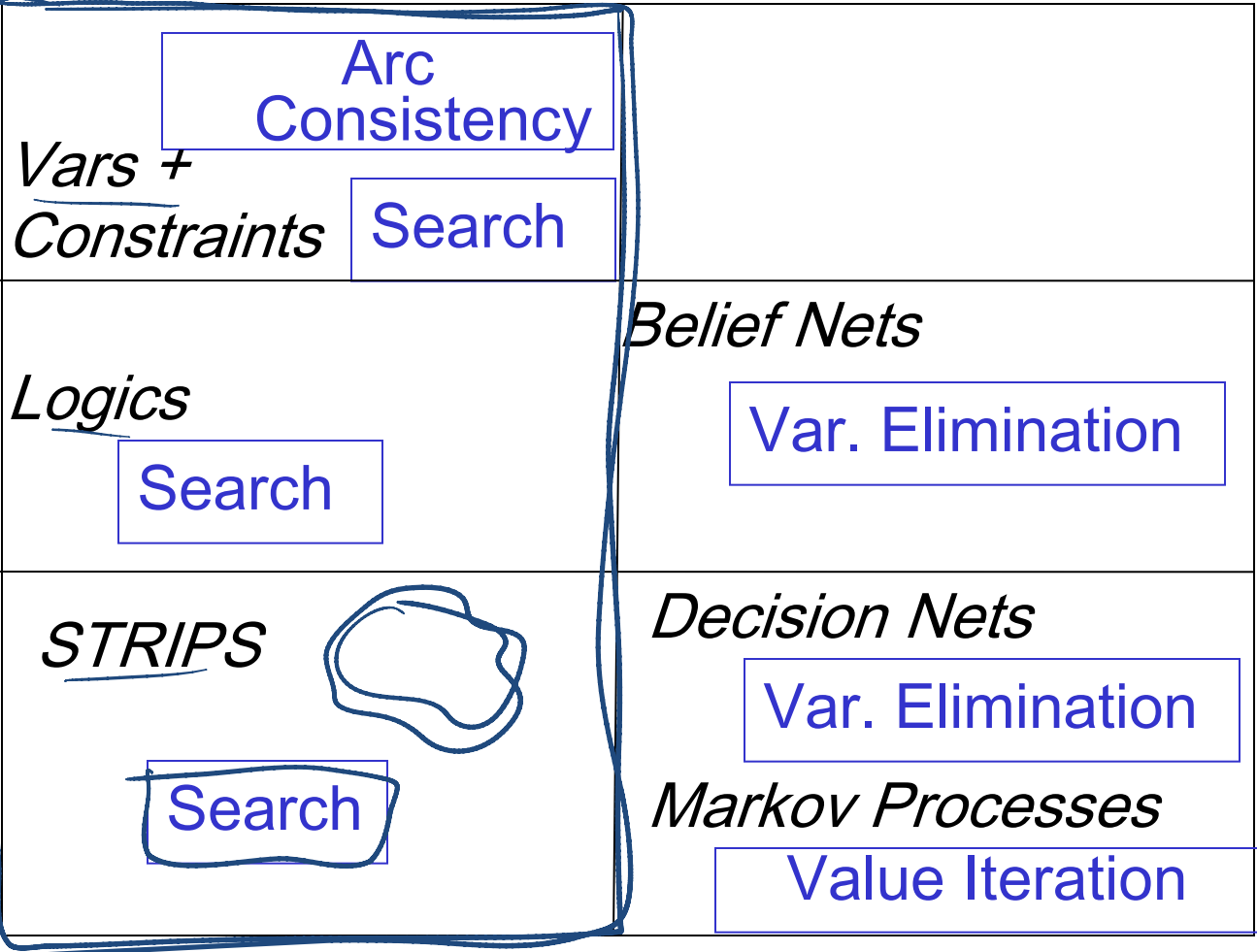
Stochastic

## Problem

Static

Constraint Satisfaction

Query



Planning

Representation

Reasoning Technique

# Lecture Overview

- **Simple Agent and Examples** 
- Search Space Graph
- Search Procedure

# Simple Planning Agent

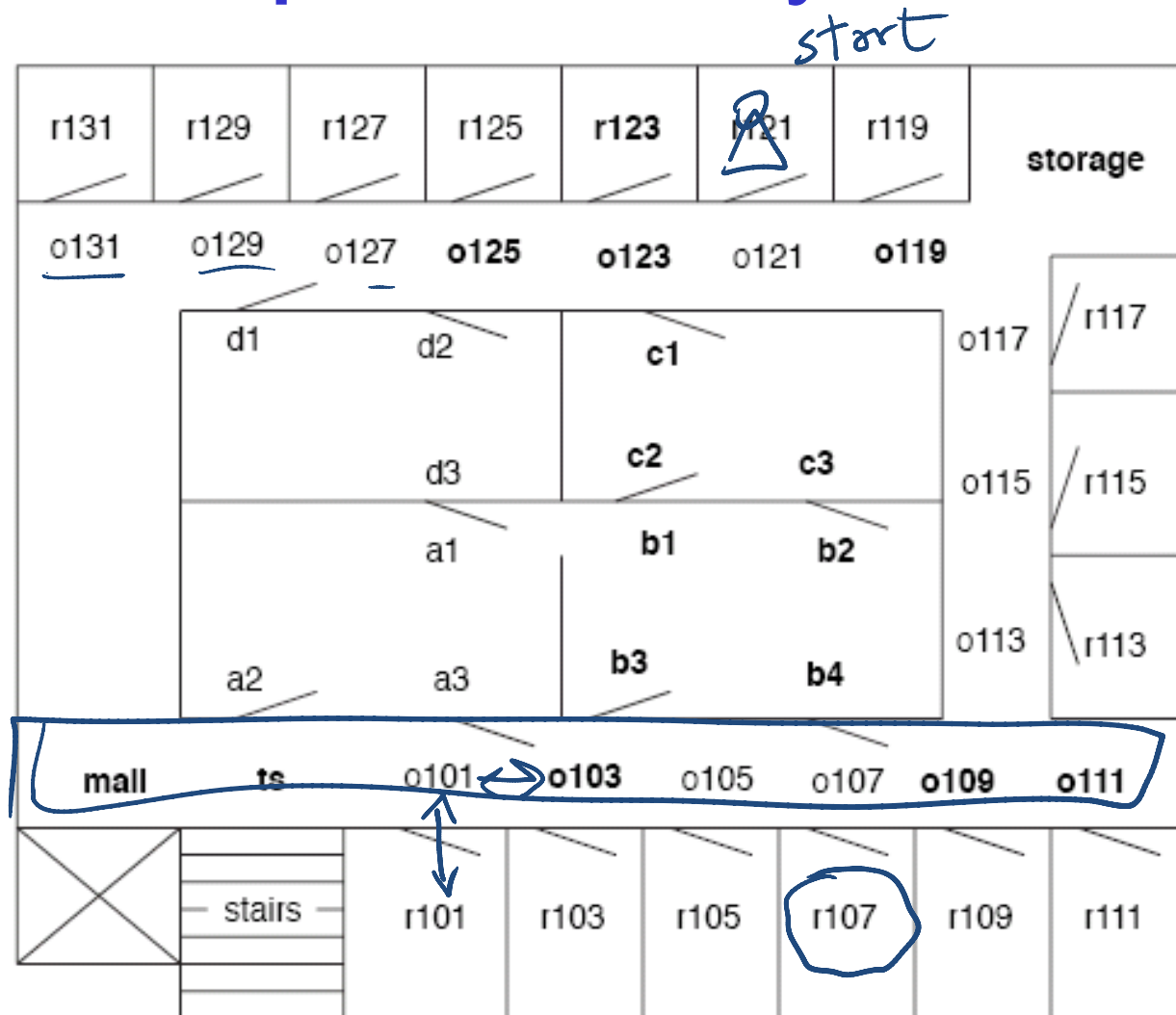
## Deterministic, goal-driven agent

- Agent is in a start state
- Agent is given a goal (subset of possible states)
- Environment changes only when the agent acts
- Agent perfectly knows:
  - what actions can be applied in any given state
  - the state it is going to end up in when an action is applied in a given state
- The sequence of actions and their appropriate ordering is the **solution**

# Three examples

1. A delivery robot planning the route it will take in a bldg. to get from one room to another
2. Solving an 8-puzzle
3. Vacuum cleaner world

# Example 1: Delivery Robot



# Eight Puzzle

5	4	
6	1	8
7	3	2

Start State

1	2	3
8		4
7	6	5

Goal State

**States:** each state specifies which number/blank occupies each of the 9 tiles

HOW MANY STATES ?

$8^9$

$2^9$

$9^9$

$9!$

**Actions:** blank moves left, right, up down

**Possible Goal:** configuration with numbers in right sequence



# of states  
9!

## Example 2: 8-Puzzle?

$\sim 360 \times 10^3$

5	4	
6	1	8
7	3	2

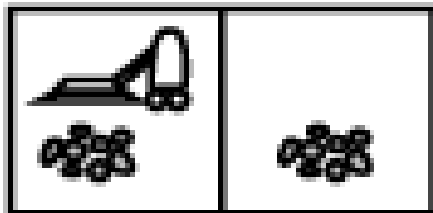
Possible start state

1	2	3
8		4
7	6	5

Goal state

# Example: vacuum world

- States
  - Two rooms: r1, r2
  - Each room can be either dirty or not
  - Vacuuming agent can be in either in r1 or r2



Possible start state



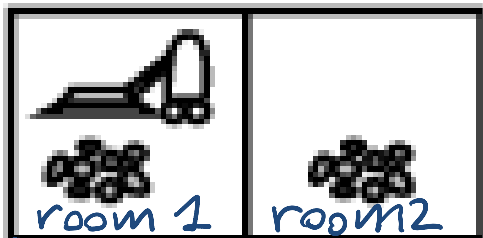
Possible goal state

# Example: vacuum world

loc 2 values  $\{r_1, r_2\}$  ~~///~~

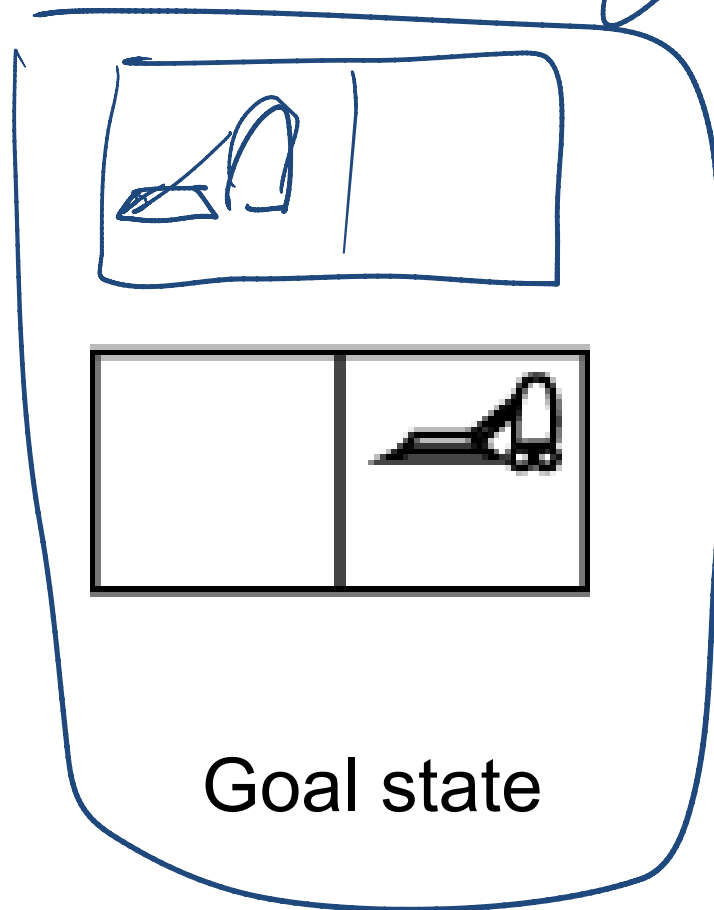
$r_1$ -clean T/F

$r_2$ -clean



Possible start state

# of states  
2 2



Goal state

can be subset of states



Suppose we have the same problem with  $k$  rooms.

The number of states is....



$$k^3$$

$$k * 2k$$

$$k * 2^k$$

$$2 * k^k$$





Suppose we have the same problem with  $k$  rooms.  
The number of states is....

$$k * 2^k$$

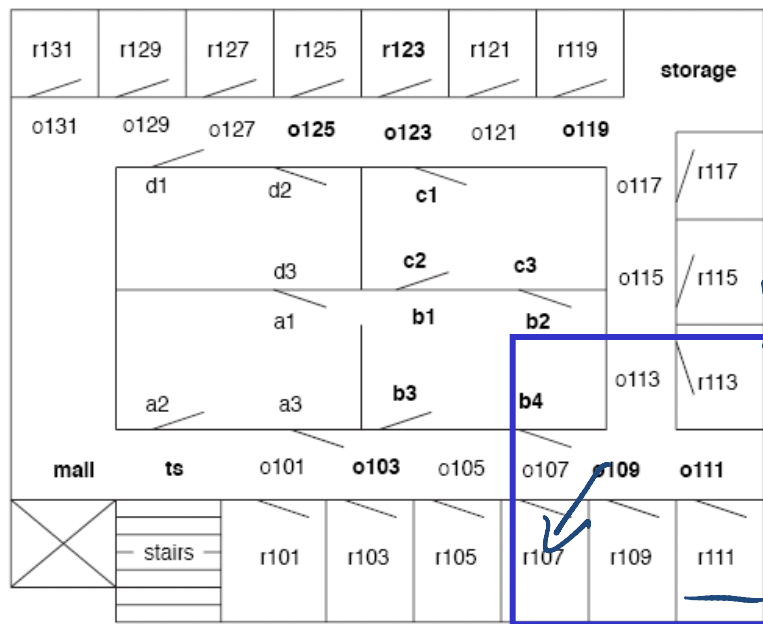


# Lecture Overview

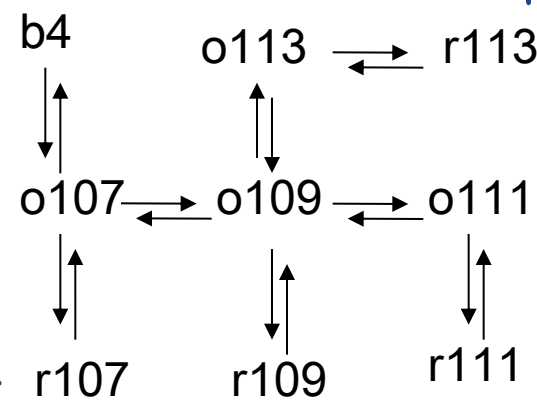
- Simple Agent and Examples
- Search Space Graph
- Search

# How can we find a solution?

- How can we find a sequence of actions and their appropriate ordering that lead to the goal?
- Define underlying search space graph where nodes are states and edges are actions.

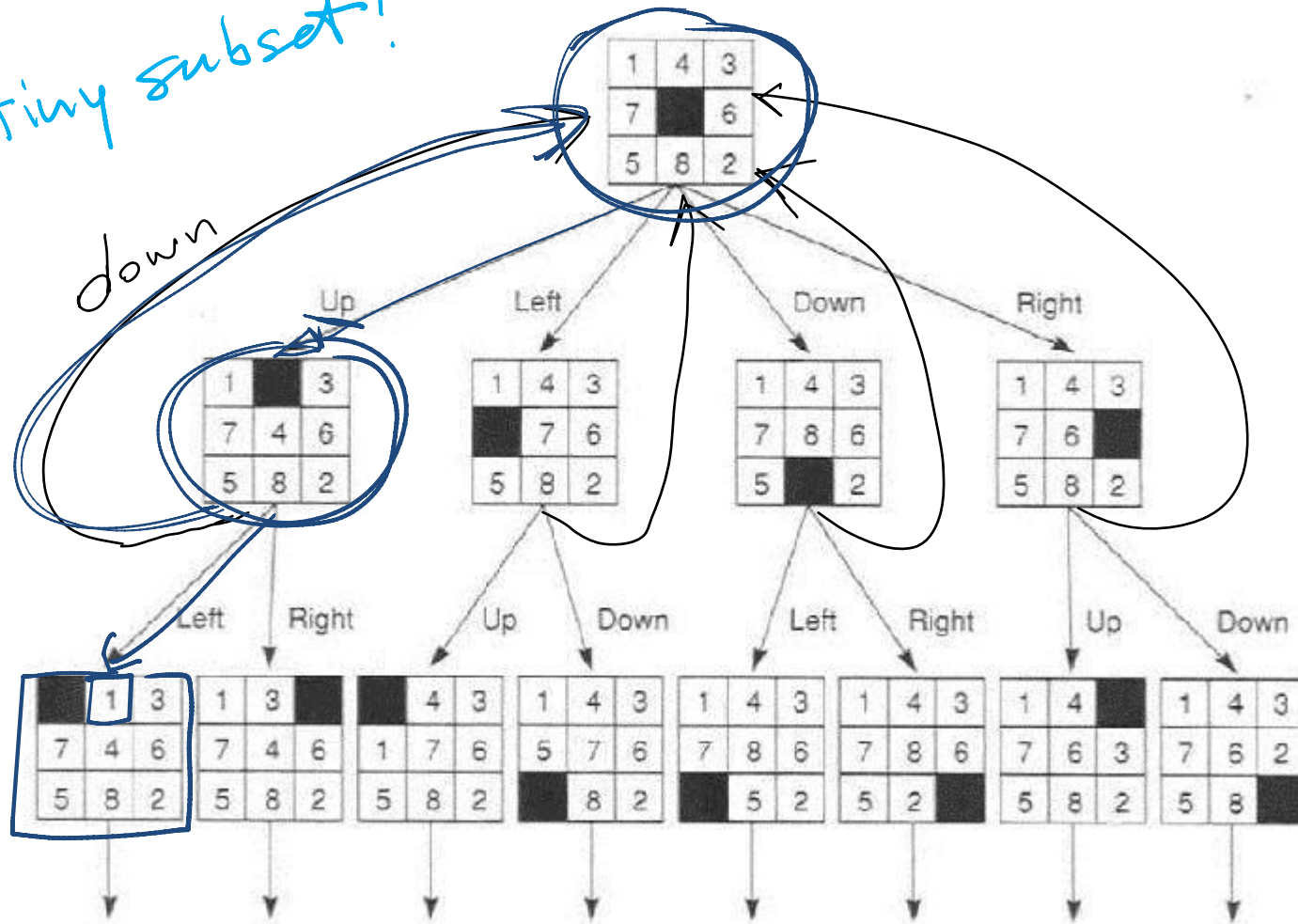


*only for this subset*



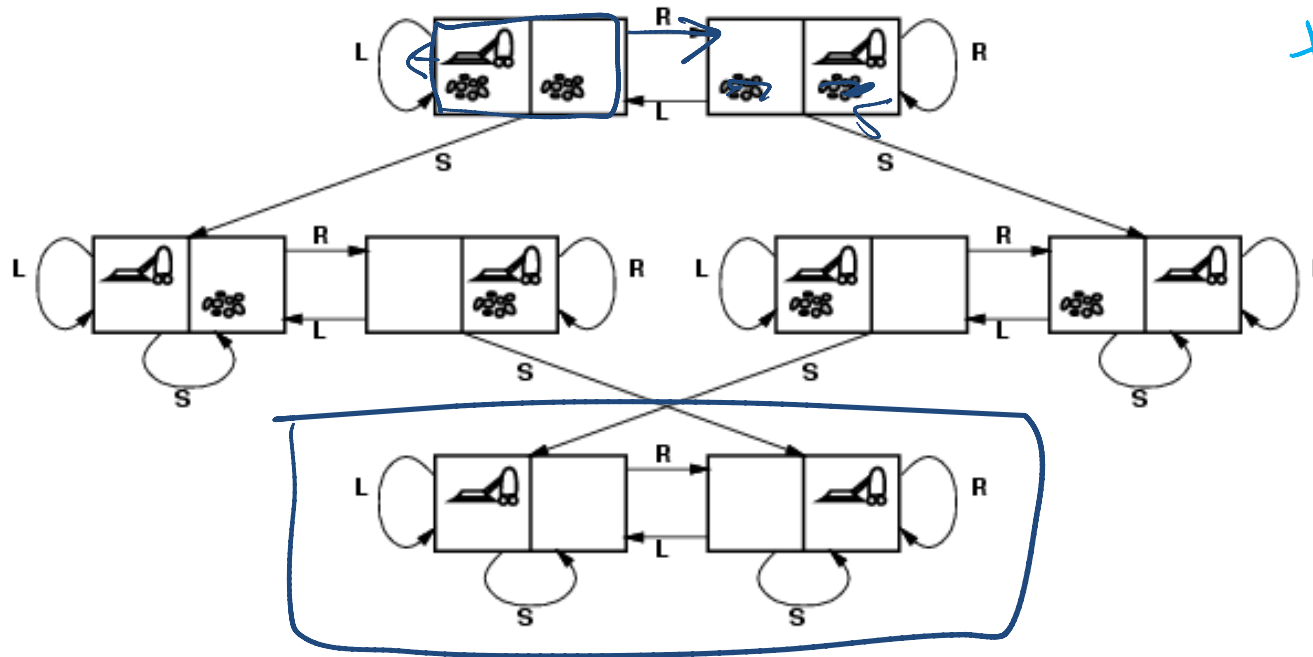
# Search space for 8puzzle

*a tiny subset!*





# Vacuum world: Search space graph



the whole space

states? Where it is dirty and robot location

actions? *Left, Right, Suck*



Possible goal test? no dirt at all locations

# Lecture Overview

- Simple Agent and Examples
- State Space Graph
- **Search Procedure**

# Search: Abstract Definition

## How to search

- Start at the start state 
- Consider the effect of taking different actions starting from states that have been encountered in the search so far 
- Stop when a goal state is encountered

To make this more formal, we'll need review the **formal definition of a graph...**

# Search Graph

A **graph** consists of a set  $N$  of **nodes** and a set  $A$  of ordered pairs of nodes, called **arcs**.

Node  $n_2$  is a **neighbor** of  $n_1$  if there is an arc from  $n_1$  to  $n_2$ . That is, if  $\langle n_1, n_2 \rangle \in A$ .

A **path** is a sequence of nodes  $n_0, n_1, n_2, \dots, n_k$  such that  $\langle n_{i-1}, n_i \rangle \in A$ .

A **cycle** is a non-empty path such that the start node is the same as the end node



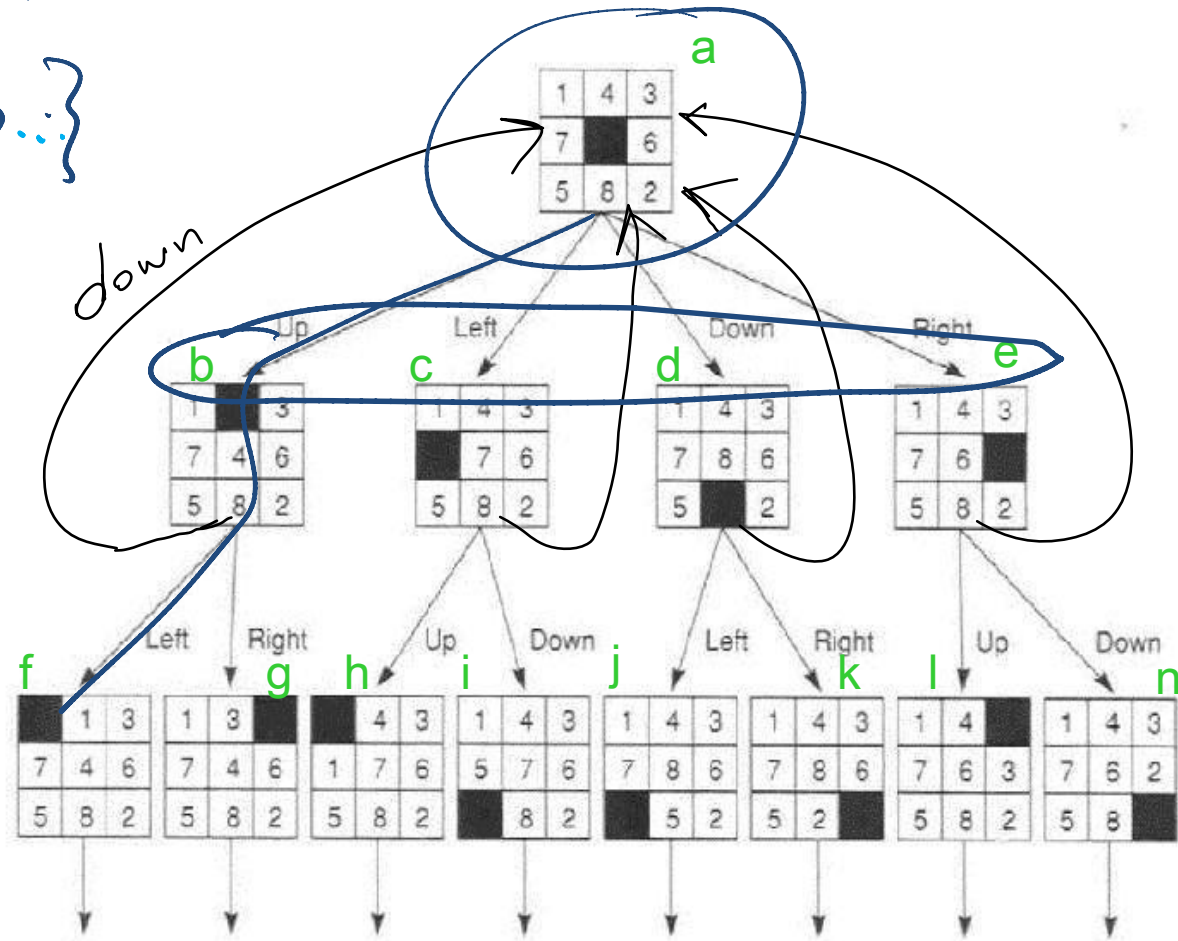
A **directed acyclic graph** (DAG) is a graph with no cycles

Given a start node and goal nodes, a **solution** is a path from a start node to a goal node.

# Examples for graph formal def.

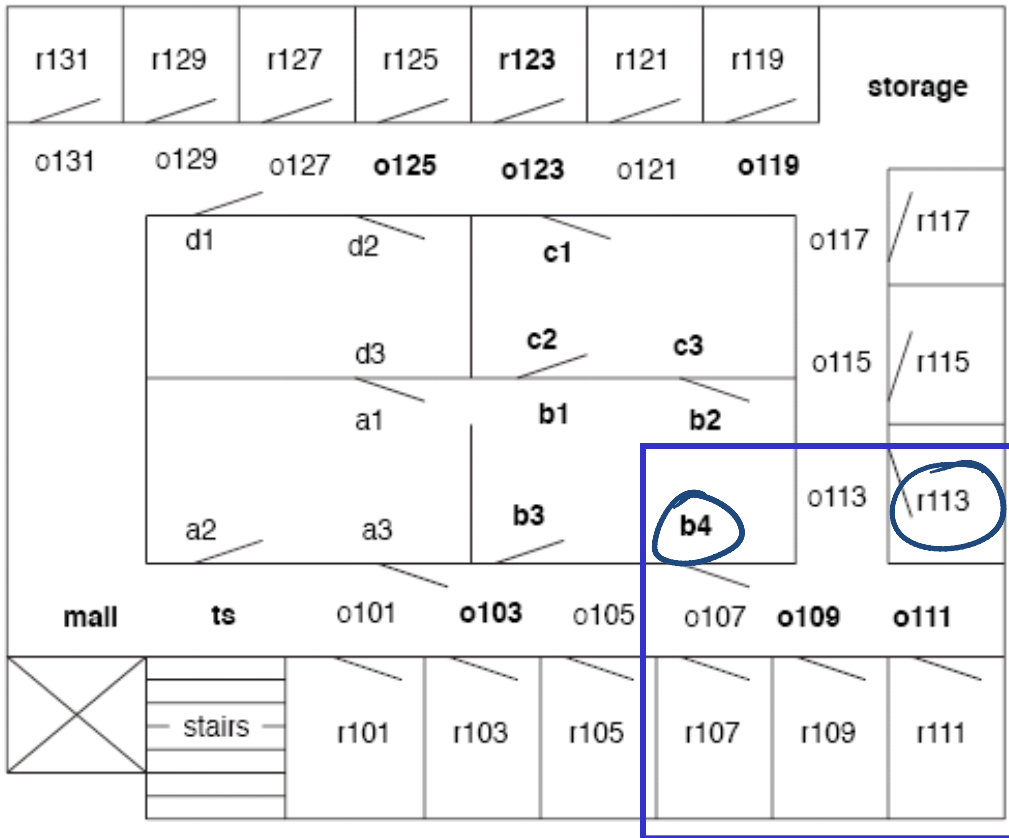
$$N = \{ a, b, \dots \}$$

$$A = \{ \langle a, b \rangle, \langle a, c \rangle, \dots \}$$

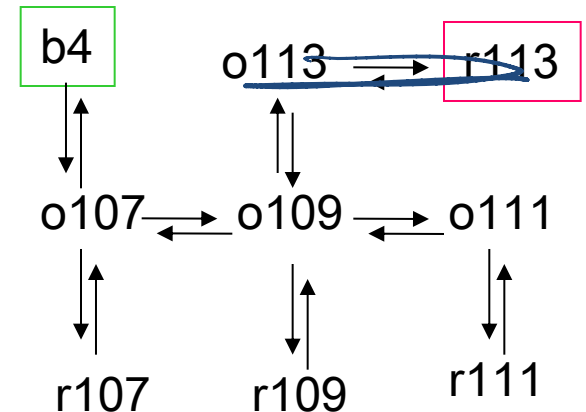


# Examples of solution

- Start state **b4**, goal **r113**
- Solution  $\langle b4, o107, o109, o113, r113 \rangle$



*but there are many others!*



# Graph Searching

**Generic search algorithm:** given a graph, start node, and goal node(s), incrementally explore paths from the start node(s).

Maintain a frontier of paths from the start node that have been explored.

As search proceeds, the frontier expands into the unexplored nodes until (hopefully!) a goal node is encountered.

The way in which the frontier is expanded defines the search strategy.



IMPLICIT IN PRACTICE

# Generic Search Algorithm

**Input:** a graph, a start node, Boolean procedure  $goal(n)$  that tests if  $n$  is a goal node

$frontier := [ \langle s \rangle : s \text{ is a start node} ]$ ;

**While**  $frontier$  is not empty:

**select and remove** path  $\langle n_0, \dots, n_k \rangle$  from  $frontier$ ;

**If**  $goal(n_k)$

**→ return**  $\langle n_0, \dots, n_k \rangle$ ;

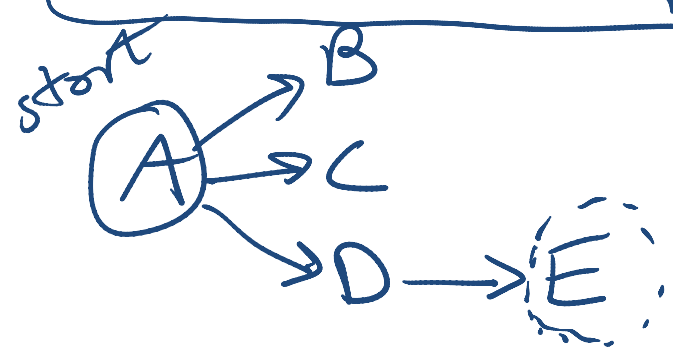
**→ For every neighbor**  $n$  of  $n_k$

**→ add**  $\langle n_0, \dots, n_k, n \rangle$  to  $frontier$ ;

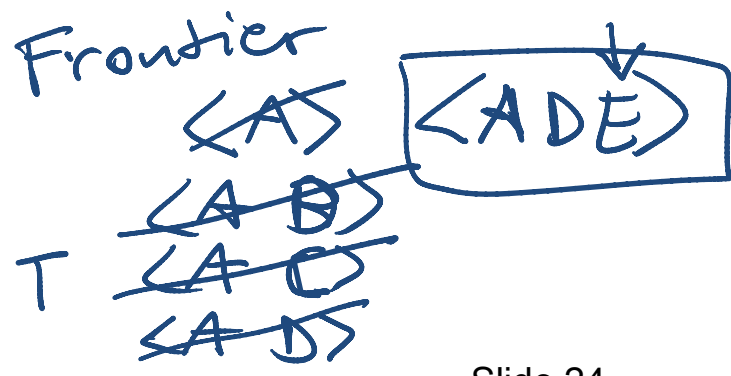
**end**

with cycles may get into infinite loop

no solution found

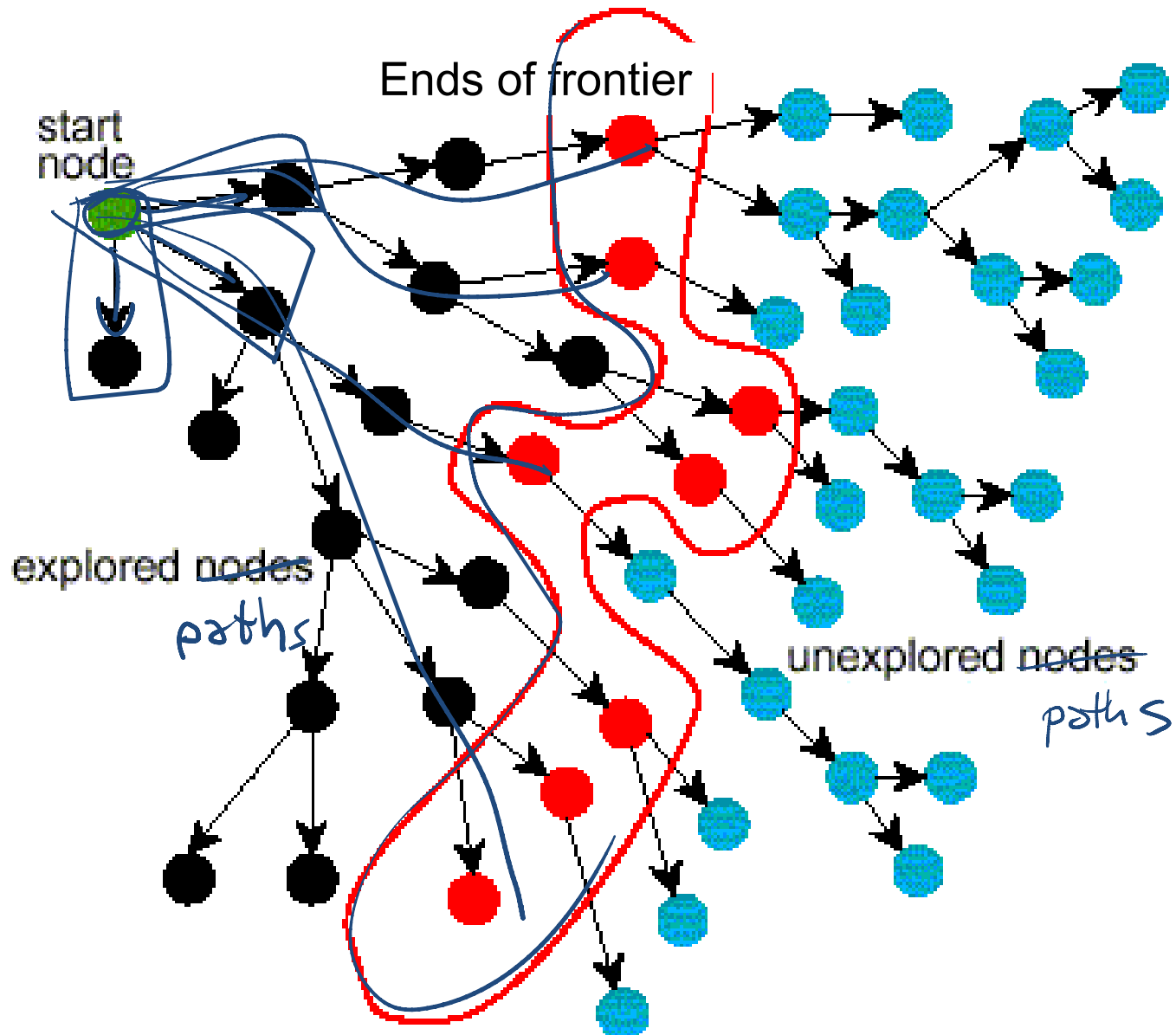


$goal(E) = T$





# Problem Solving by Graph Searching



# Branching Factor

The *forward branching factor* of a node is the number of arcs going out of the node

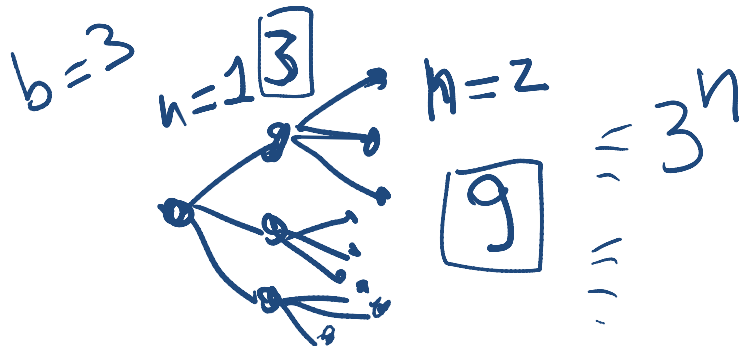


The *backward branching factor* of a node is the number of arcs going into the node



If the forward branching factor of any node is  $b$  and the graph is a tree, how many nodes are  $n$  steps away from a node?

clicker.




$nb$

$b^n$

$n^b$

$n/b$

# Lecture Summary

- Search is a key computational mechanism in many AI agents 
- We will study the basic principles of search on the simple deterministic planning agent model

## Generic search approach:

- define a search space graph,
- start from current state,
- incrementally explore paths from current state until goal state is reached.

The way in which the frontier is expanded defines the search strategy. 

# Learning Goals for today's class

- Identify real world examples that make use of deterministic, goal-driven planning agents
- **Assess** the size of the search space of a given search problem. *How many possible states*
- Implement the generic solution to a search problem. *see also Mars Explorer Lecture 2*

## Next class (Fri)

- **Uninformed search strategies**  
(read textbook Sec. 3.5)

- **First Practice Exercise 3.A**
- <http://www.aispace.org/exercises.shtml>