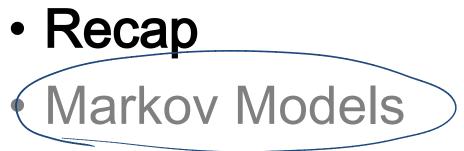
Probability and Time: Hidden Markov Models (HMMs)

Computer Science cpsc322, Lecture 32

(Textbook Chpt 6.5.2)

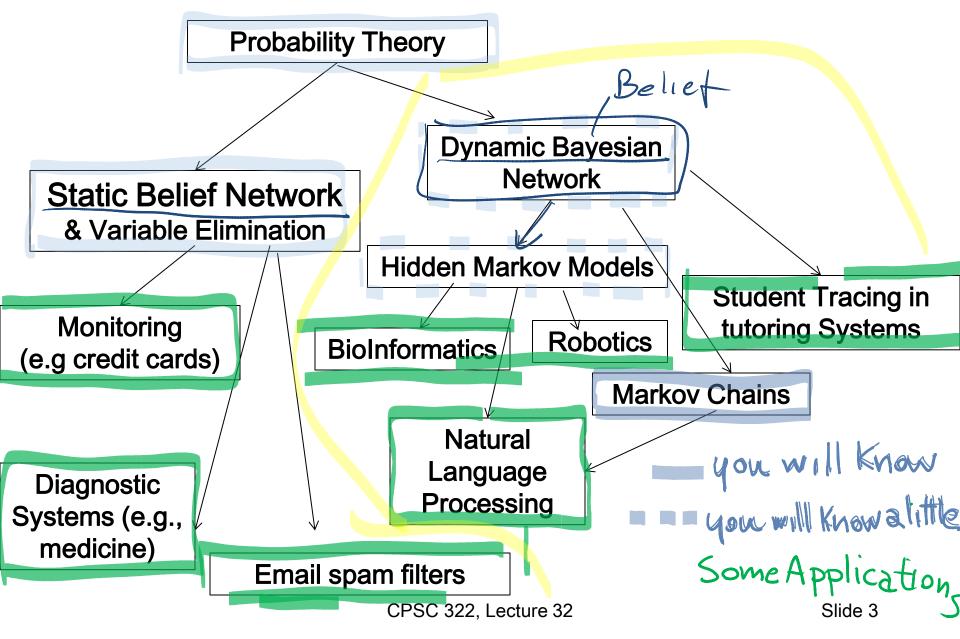
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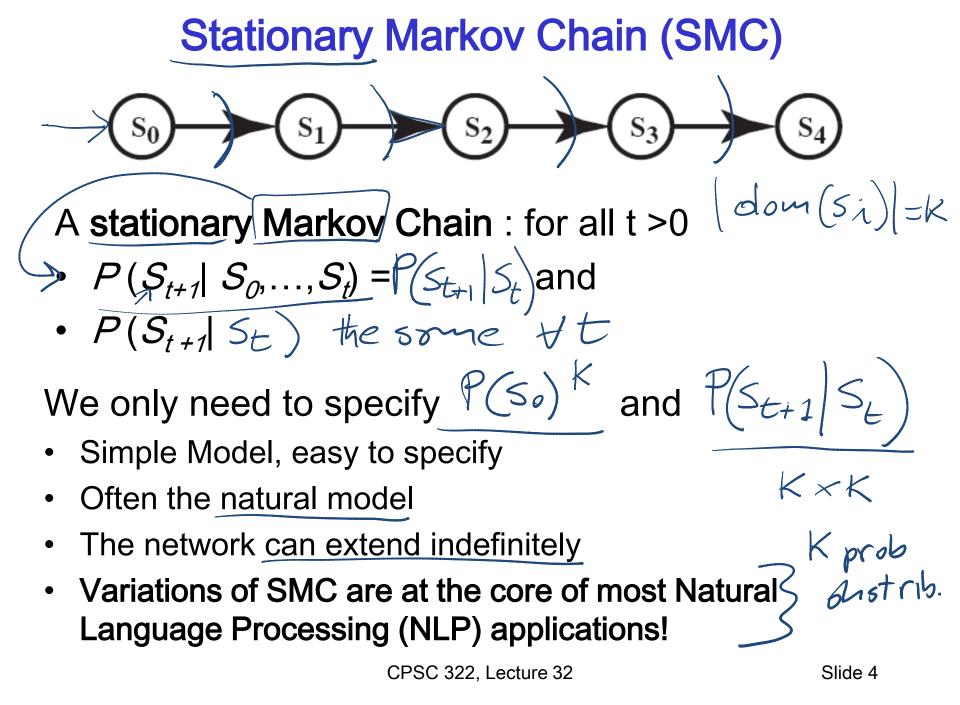
Lecture Overview



- Markov Chain
- Hidden Markov Models

Answering Queries under Uncertainty

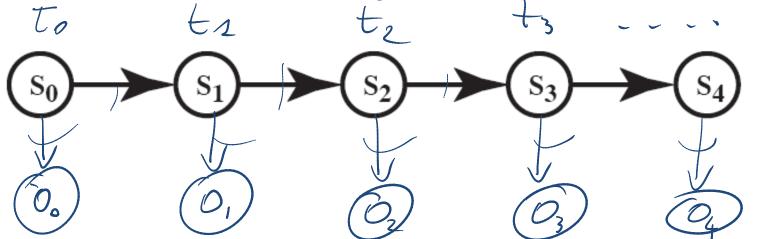




Lecture Overview

- Recap
- Markov Models
 - Markov Chain
 - Hidden Markov Models

How can we minimally extend Markov Chains?



• Maintaining the Markov and stationary assumptions?

A useful situation to model is the one in which:

- the reasoning system does not have access to the states
- but can make observations that give some information about the current state

i⊧clicker.

A. *2* × *h*

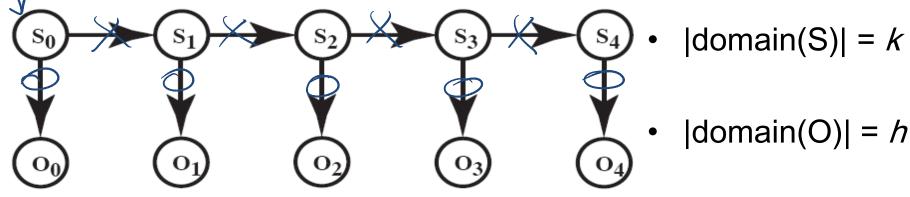
B. *h* × *h*

C . *k* × *h*

D. *k* × *k*

Hidden Markov Model

 A Hidden Markov Model (HMM) starts with a Markov chain, and adds a noisy observation about the state at each time step:



• $P(S_0)$ specifies initial conditions

$$P(S_{t+1}|S_t)$$
 specifies the dynamics

 $O_P(O_t | S_t)$ specifies the sensor model

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i**⊳**clicker.

A. 2 × h

B. hxh

 \mathbf{C} . $k \times h$

 \mathbf{D} . $k \times k$

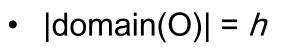
Hidden Markov Model

 $\mathbf{S}_{\mathbf{3}}$

0

 A Hidden Markov Model (HMM) starts with a Markov chain, and adds a noisy observation about the state at each time step:

|domain(S)| = k



Kxh {Kprob.bist.}

 $P(S_{0})$ specifies initial conditions

 S_4

 O_4

KXK

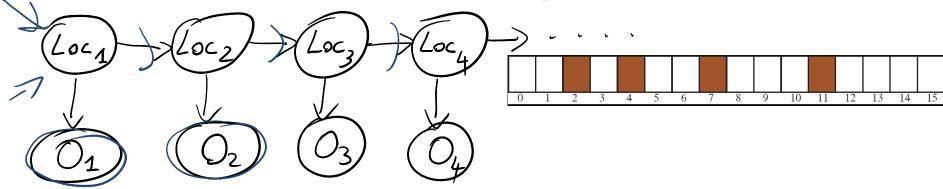
 $P(S_{t+1}|S_t)$ specifies the dynamics

 $O_{f}(O_{f}|S_{f})$ specifies the sensor model

Example: Localization for "Pushed around" Robot

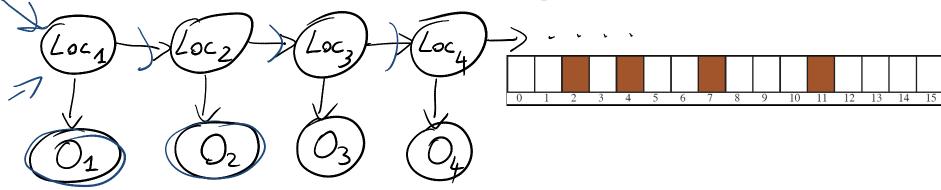
- Localization (where am I?) is a fundamental problem in robotics
- Suppose a robot is in a circular corridor with 16 locations 2 9 10 12 13 2 3 5 6 8 11 14 15 0 4
 - There are four doors at positions: 2, 4, 7, 11
 - The Robot initially doesn't know where it is
 - The Robot is pushed around. After a push it can stay in the same location, move left or right.
 - The Robot has a Noisy sensor telling whether it is in front of a door

This scenario can be represented as...



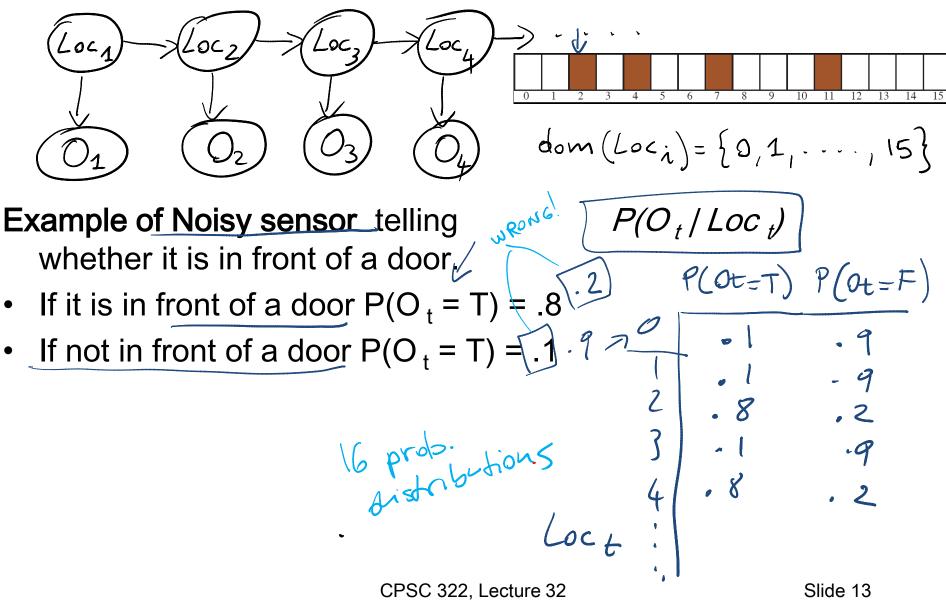
 Example Stochastic Dynamics: when pushed, it stays in the same location p=0.2, moves one step left or right with equal probability

This scenario can be represented as...



Example Stochastic Dynamics: when pushed, it stays in the same location p=0.2, moves left or right with equal probability

This scenario can be represented as...



Useful inference in HMMs

 Localization: Robot starts at an unknown location and it is pushed around *t* times. It wants to determine where it is

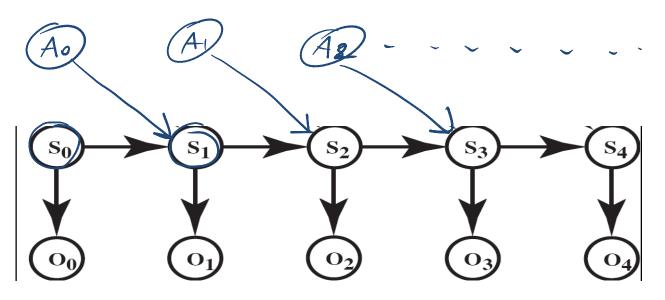
$$P(Loc_t | o_1 \dots o_t)$$

 In general: compute the posterior distribution over the current state given all evidence to date

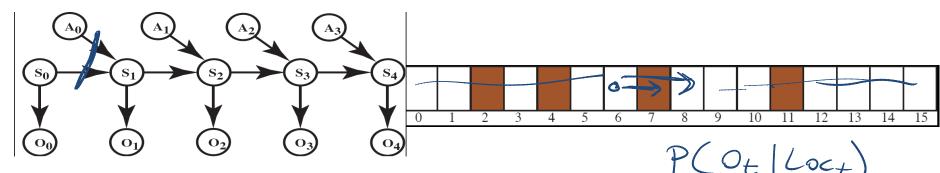
 \mathbf{N}

Example : Robot Localization

- Suppose a robot wants to determine its location based on its actions and its sensor readings
- Three actions: *goRight, goLeft, Stay*
- This can be represented by an augmented HMM



Robot Localization Sensor and Dynamics Model



- Sample Sensor Model (assume same as for pushed around)
- Sample Stochastic Dynamics: P(Loc_{t + 1} / Action_t, Loc t)

$$P(Loc_{t+1} = L) | Action_{t} = goRight, Loc_{t} = L) = 0.1$$

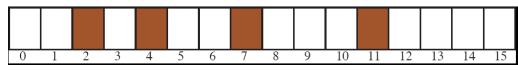
$$P(Loc_{t+1} = L+1 | Action_{t} = goRight, Loc_{t} = L) \neq 0.8$$

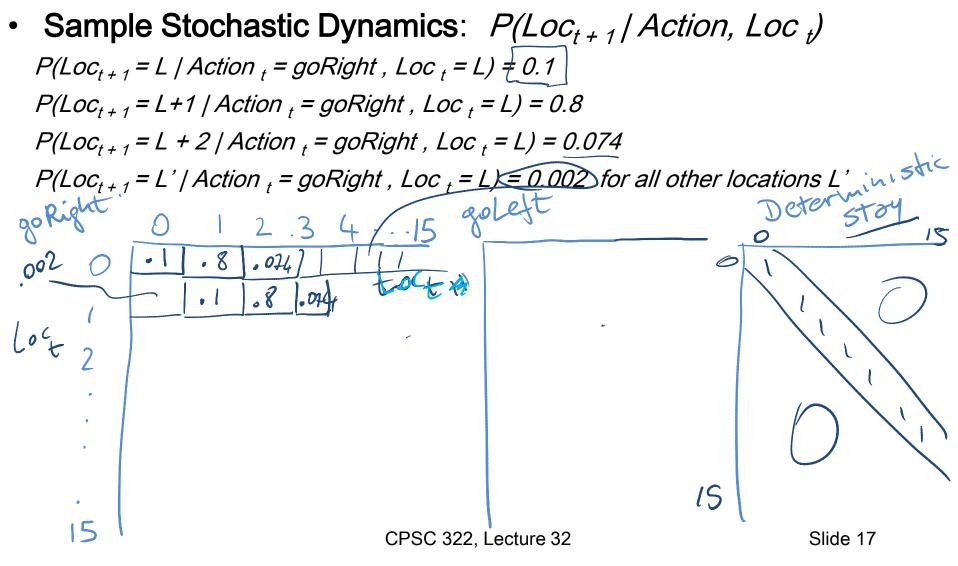
$$P(Loc_{t+1} = L + 2 | Action_{t} = goRight, Loc_{t} = L) = 0.074$$

$$P(Loc_{t+1} = L' | Action_{t} = goRight, Loc_{t} = L) = 0.002 \text{ for all other locations L'}$$

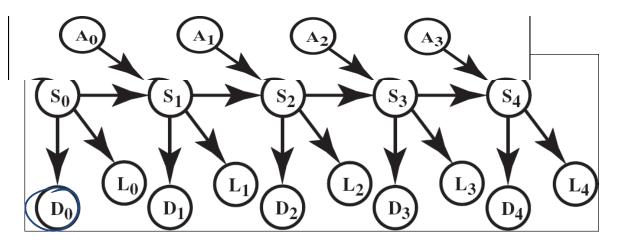
- All location arithmetic is modulo 16
- The action goLeft works the same but to the left

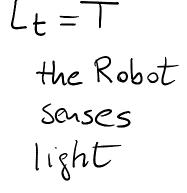
Dynamics Model More Details



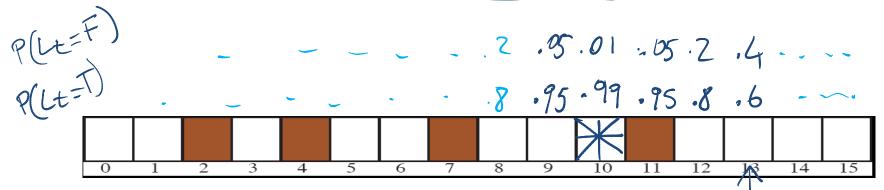


Robot Localization additional sensor





• Additional Light Sensor: there is light coming through an opening at location 10 $P(L_t | Loc_t)$



Info from the two sensors is combined :"Sensor Fusion"

The Robot starts at an unknown location and must determine where it is

The model appears to be too ambiguous

- Sensors are too noisy
- Dynamics are too stochastic to infer anything

But inference actually works pretty well. Let's check:

http://www.cs.ubc.ca/spider/poole/demos/localization
 /localization.html

You can use standard Bnet inference. However you typically take advantage of the fact that time moves forward (not in 322)

Sample scenario to explore in demo

- Keep making observations without moving. What happens?
- Then keep moving without making observations. What happens?
- Assume you are at a certain position alternate moves and observations

HMMs have many other applications....

- Natural Language Processing: e.g., Speech Recognition
- - Observations: DNA Sequences
 ATCGGAA

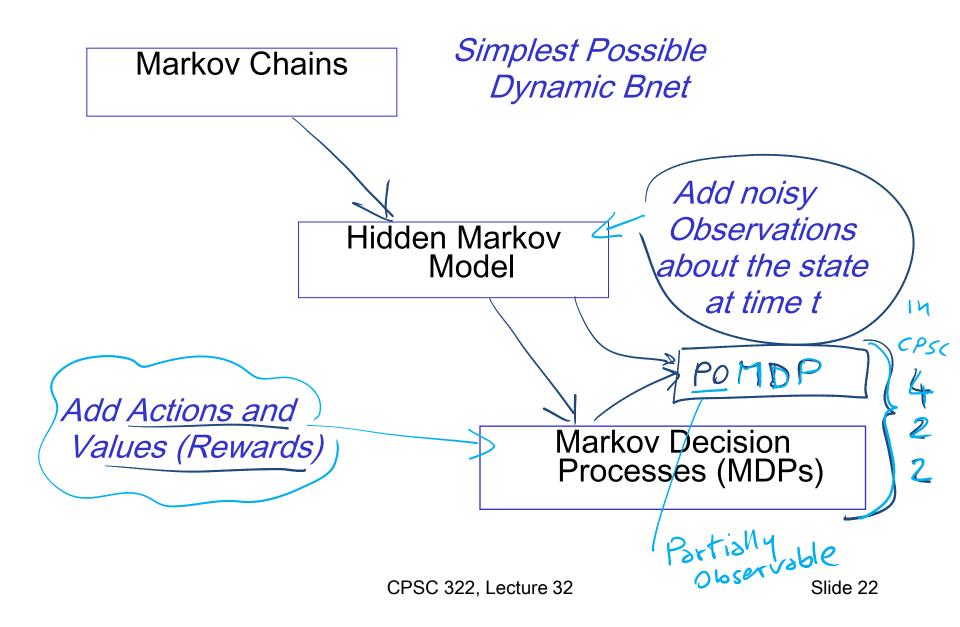
For these problems the critical inference is:

find the most likely sequence of states given a sequence of observations

Viterbi Algo

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Markov Models



Learning Goals for today's class

You can:

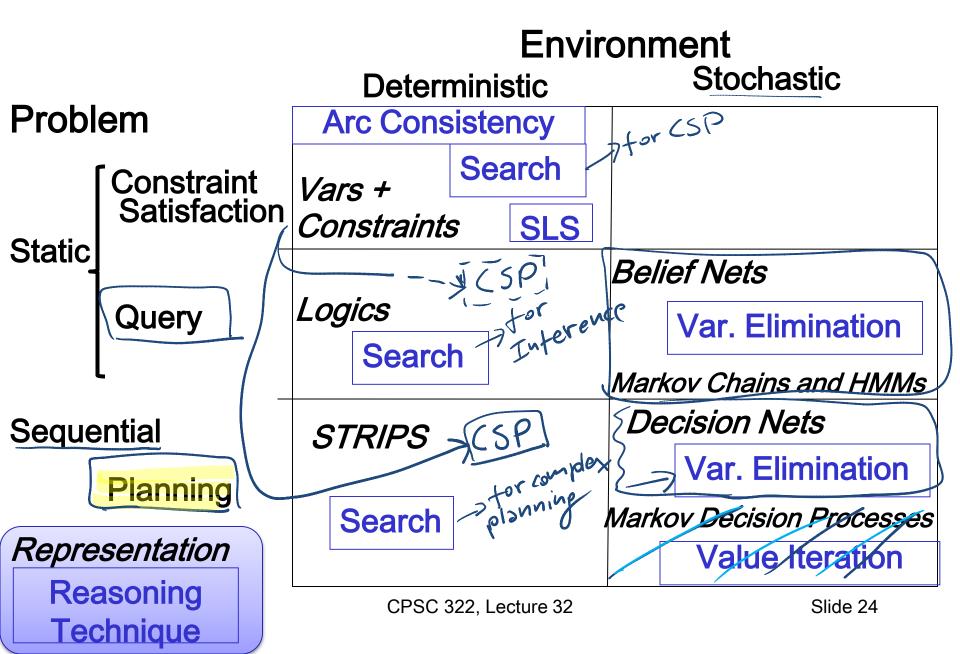
- Specify the components of an Hidden Markov Model (HMM)
- Justify and apply HMMs to Robot Localization

Clarification on second LG for last class

You can:

Justify and apply Markov Chains to compute the probability of a Natural Language sentence (NOT to estimate the conditional probs- slide 18)

Next week



Next Class

- One-off decisions (TextBook 9.2)
- Single Stage Decision networks (9.2.1)

Instructor

• Giuseppe Carenini (carenini@cs.ubc.ca; office CICSR 105)

People

Teaching Assistants

- Kamyar Ardekani kamyar.ardekany@gmail.com
- Tatsuro Oya toya@cs.ubc.ca
- Xin Ru (Nancy) Wang nancywang1991@yahoo.ca







Slide 26