Heuristic Search

Computer Science cpsc322, Lecture 7

(Textbook Chpt 3.5)

January, 19, 2009

Dept. Announcements

• Event: Weekly ELM Lunches

- **Description:** Whimsical discussion of CS topics over brown bag lunch. This term's theme is human distributed games.
- Date and Time: Every Tuesday, 12:30 2 pm
- Place: ICICS/CS Rm 206
- Event: IBM Information Session
 - Date and Time: Tuesday, Jan 20, 5:30 7:30 pm
 - Place: Wesbrook 100

Event: Resume and Cover Letter Writing Workshop

- Date and Time: Wednesday, Jan 21, 12 1 pm
- Place: DMP 201
- Event: How to Prepare for Career Fair Workshop
 - Date and Time: Thursday, Jan 29, 1 2 pm
 - Place: DMP 110

Course Announcements

Posted on WebCT

- Marks for assignment0
- Second Practice Exercise (uninformed Search)

If you are confused on basic search algorithm, different search strategies..... Check learning goals at the end of lectures. Please come to office hours

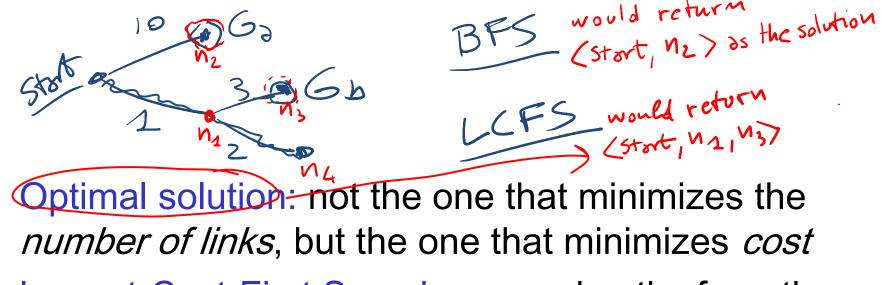
Assignment1 will be posted on Wed

Lecture Overview

- Recap
 - Search with Costs
 - Summary Uninformed Search
- Heuristic Search

Recap: Search with Costs

- Sometimes there are costs associated with arcs.
 - The cost of a path is the sum of the costs of its arcs.



• Lowest-Cost-First Search: expand paths from the frontier in order of their costs.

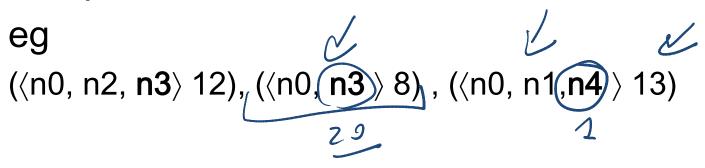
Recap Uninformed Search

	Complete	Optimal	Time	Space
DFS	$\left(\mathbf{N}^{\prime} \right)$	Ν	$O(b^m)$	O(mb)
	Yit no cycles and finite search space			
BFS	Y	Y	$O(b^m)$	$O(b^m)$
IDS	Y	Y	$O(b^m)$	O(mb)
			~~~	
LCFS	Y	Y	$O(b^m)$	$O(b^m)$
	Costs > 0	Costs >=0	)	

#### **Recap Uninformed Search**

• Why are all these strategies called uninformed?

Because they do not consider any information about the states (end nodes) to decide which path to expand first on the frontier



In other words, they are general they do not take into account the specific nature of the problem.

#### **Lecture Overview**

- Recap
  - Search with Costs
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- Heuristic Search
- Best-First Search

#### **Heuristic Search**

Uninformed/Blind search algorithms do not take into account the goal until they are at a goal node.

Often there is extra knowledge that can be used to guide the search: an *estimate* of the distance from node *n* to a goal node.

#### This is called a *heuristic*

## **More formally**

Definition (search heuristic)

A search heuristic h(n) is an estimate of the cost of the shortest path from node n to a goal node.

- *h* can be extended to paths:  $h(\langle n_0, \dots, n_k \rangle) = h(n_k)$
- *h(n)* uses only readily obtainable information (that is easy to compute) about a node.

CPSC 322, Lecture 7

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## More formally (cont.)

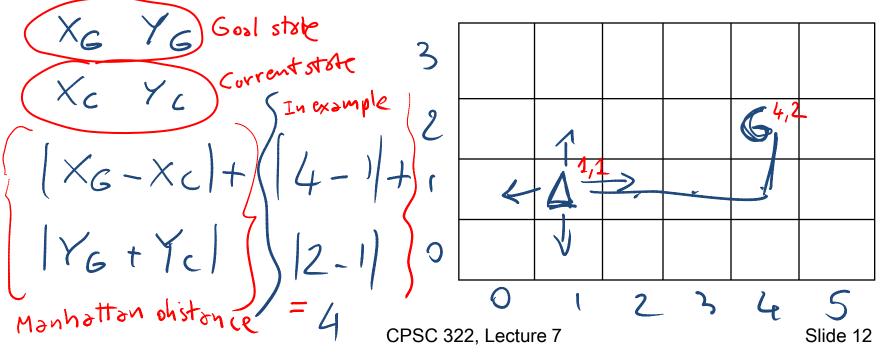
Definition (admissible heuristic)A search heuristic *h(n)* is admissible if it is never an overestimate of the cost from *n* to a goal.

- There is never a path from *n* to a goal that has path length less than *h(n)*.
- another way of saying this: h(n) is a lower bound on the cost of getting from n to the nearest goal.



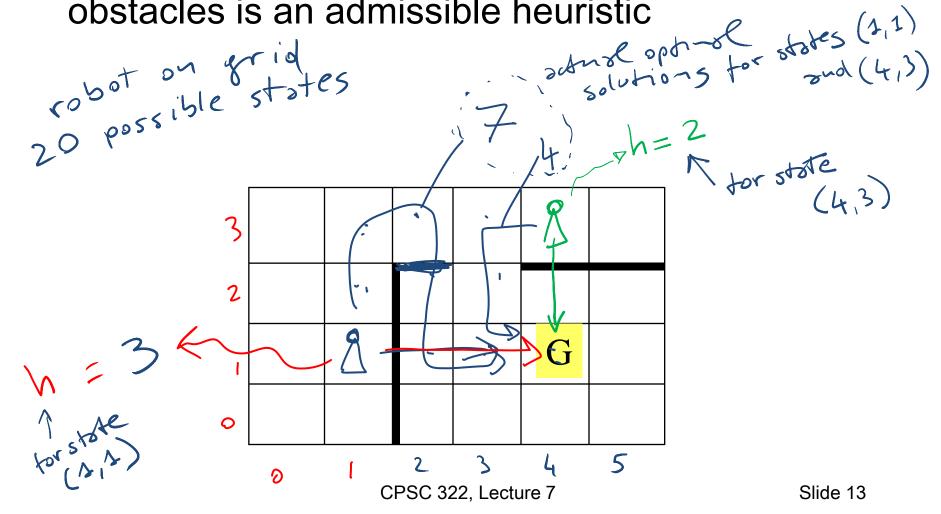
#### **Example Admissible Heuristic Functions**

- Search problem: robot has to find a route from start location to goal location on a grid (discrete space with obstacles)
- Final cost (quality of the solution) is the number of steps
- If no obstacles, cost of optimal solution is...



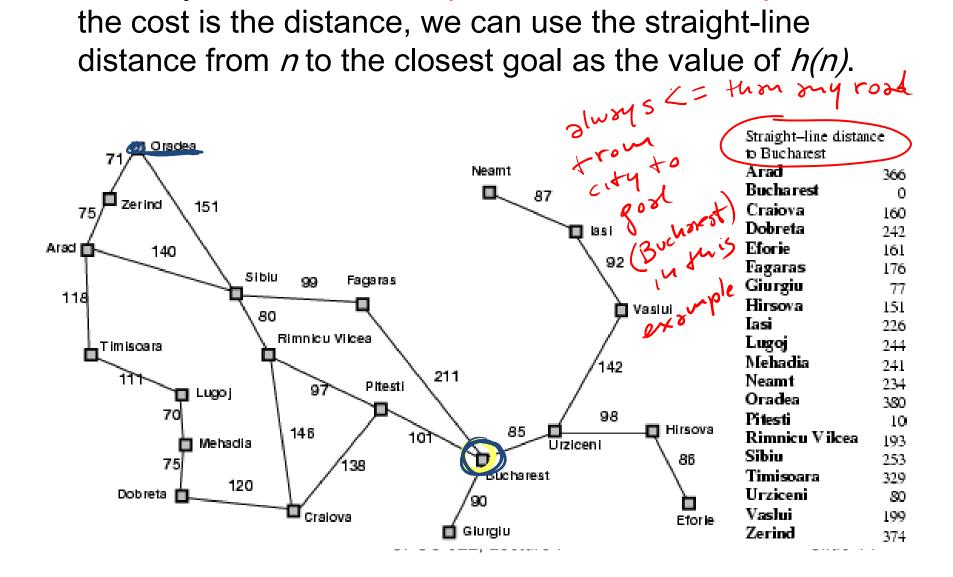
#### **Example Admissible Heuristic Functions**

If there are obstacle, the optimal solution without obstacles is an admissible heuristic



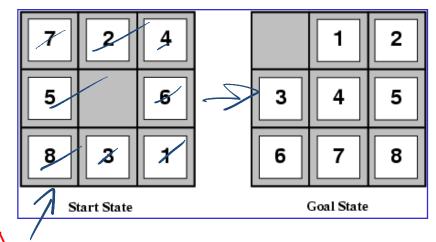
#### **Example Admissible Heuristic Functions**

Similarly, If the nodes are points on a Euclidean plane and • the cost is the distance, we can use the straight-line distance from *n* to the closest goal as the value of h(n).

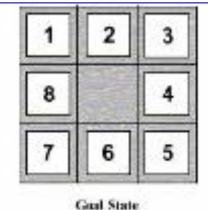


## Example Heuristic Functions

• In the 8-puzzle, we can use the number of misplaced tiles





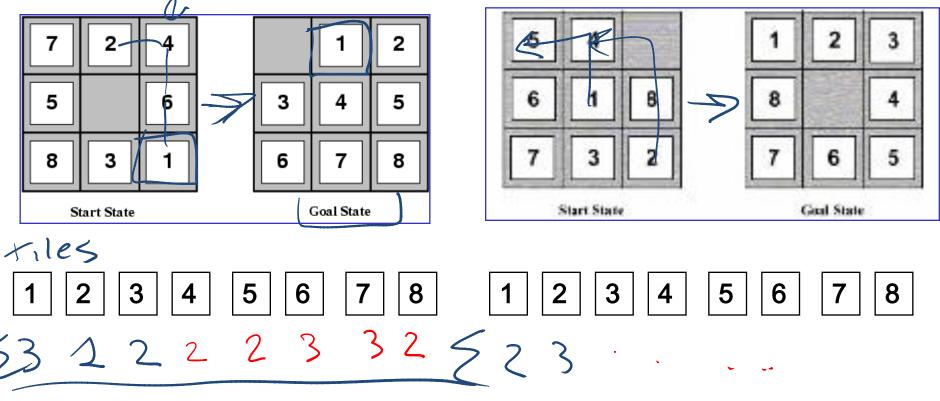


Start State

N 7

## Example Heuristic Functions (2)

 Another one we can use the number of moves between each tile's current position and its position in the solution



= 18

#### How to Construct a Heuristic

You identify relaxed version of the problem:

- where one or more constraints have been dropped
- problem with fewer restrictions on the actions
  Robot: the agent can move through walls 
  Driver: the agent can move straight <</li>
  8puzzle: (1) tiles can move anywhere 
  (2) tiles can move to any adjacent square

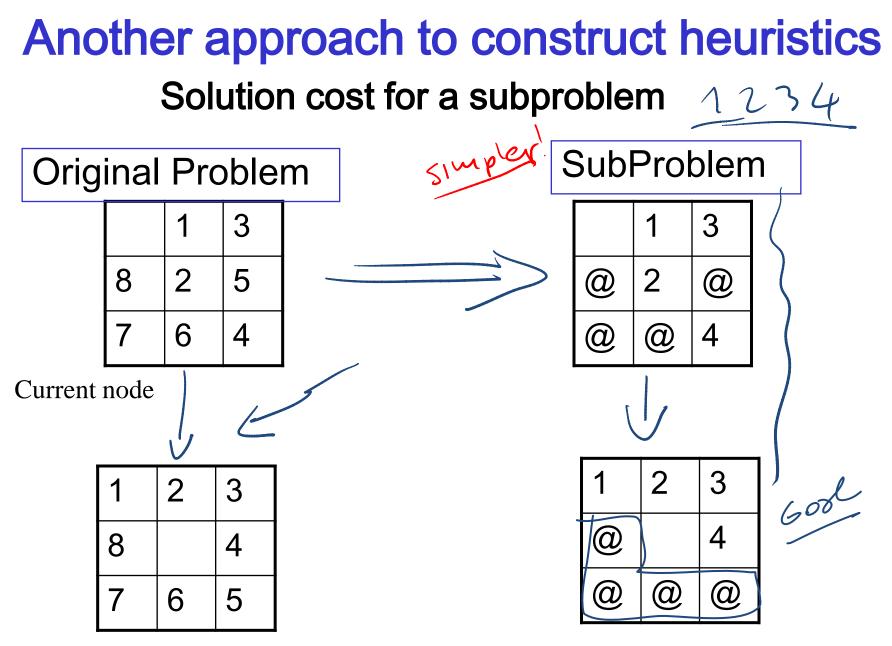
**Result:** The cost of an optimal solution to the relaxed problem is an admissible heuristic for the original problem (because it is always weakly less costly to solve a less constrained problem!)

## How to Construct a Heuristic (cont.)

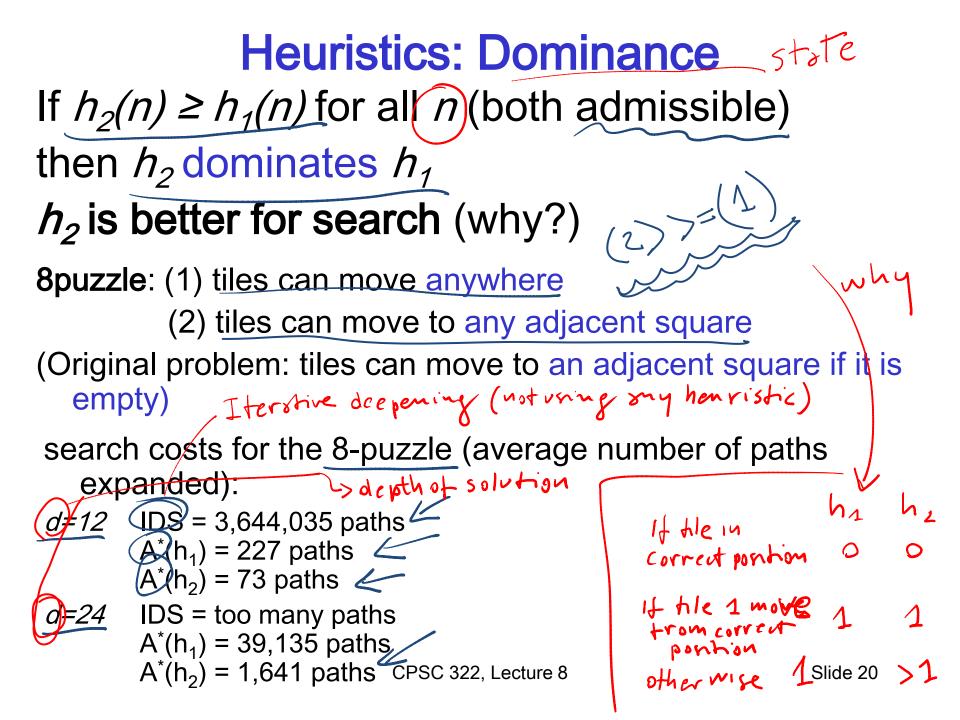
- You should identify constraints which, when dropped, make the problem extremely easy to solve
  - this is important because heuristics are not useful if they're as hard to solve as the original problem!

#### This was the case in our examples

- Robot: *allowing* the agent to move through walls. Optimal solution to this relaxed problem is Manhattan distance
- Driver: *allowing* the agent to move straight. Optimal solution to this relaxed problem is straight-line distance
- 8puzzle: (1) tiles can move anywhere Optimal solution to this relaxed problem is number of misplaced tiles
- (2) tiles can move to any adjacent square....



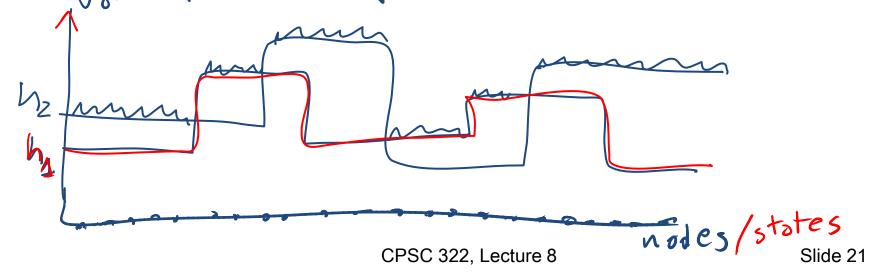
Goal node



## **Combining Heuristics**

# How to combine heuristics when there is no dominance?

- If  $h_1(n)$  is admissible and  $h_2(n)$  is also admissible then
- $h(n) = \frac{m \delta x}{(h_1, h_2)}$  is also admissible
- ... and dominates all its components



### **Combining Heuristics: Example**

In 8-puzzle, solution cost for the 1,2,3,4 subproblem is substantially more accurate than Manhattan distance in some cases som of of each the non So....tromits portion WZX retter henrigh'?

#### **Lecture Overview**

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## Learning Goals for today's class

- Construct admissible heuristics for appropriate problems. Verify Heuristic Dominance. Combine admissible heuristics
- Define/read/write/trace/debug different search algorithms
  - •With / Without cost

Informed / Uninformed

#### **Next class**

Combining LCFS and BFS: A* (finish 3.5)

- A* Optimality
- A* is optimal efficient