## Reasoning Under Uncertainty: More on BNets structure and construction

#### Computer Science cpsc322, Lecture 28

(Textbook Chpt 6.3)

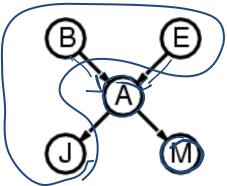


#### March, 18, 2009

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## **Belief networks Recap**

- By considering causal dependencies, we order variables in the joint.
- Apply. choin rule and simplify



- P(B, E, A, J, M) = P(B) P(E) P(A|B,E) P(J|A) P(M|A) why M indep(B, E, J) given A P(M, B, E, J, A)
- Build a directed acyclic graph (DAG) in which the parents of each var X are those vars on which X directly depends.
- By construction, a var is independent form it nondescendant given its parents. why?

## **Belief Networks: open issues**

- Independencies: Does a BNet encode more  $\swarrow$  independencies than the ones specified by construction?  $\gamma_{es}$
- **Compactness**: We reduce the number of  $\frac{K parents}{too(N 2^{K})}$

In some domains we need to do better than that!

• Still too many and often there are no data/experts for accurate assessment

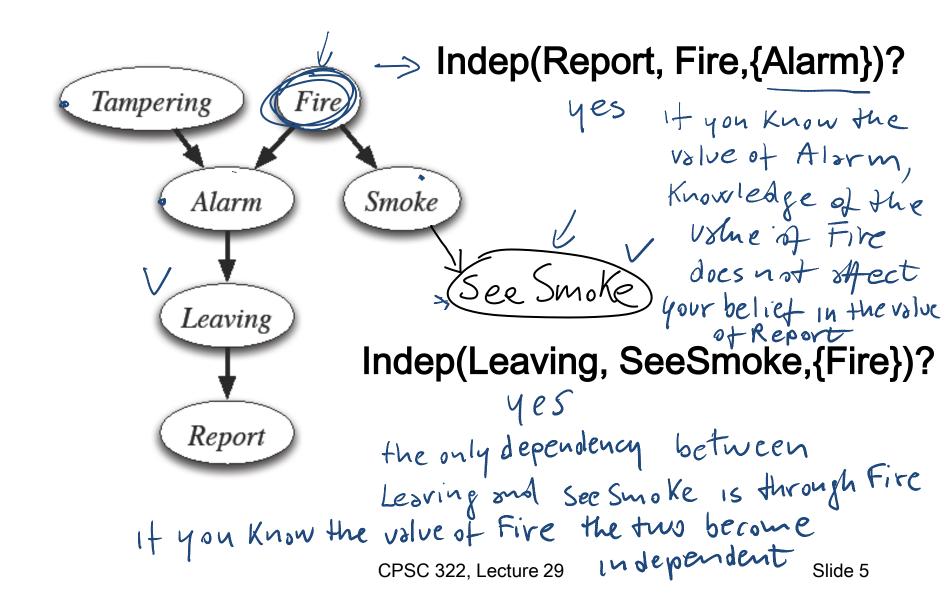
Solution: Make stronger (approximate)

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## **Lecture Overview**

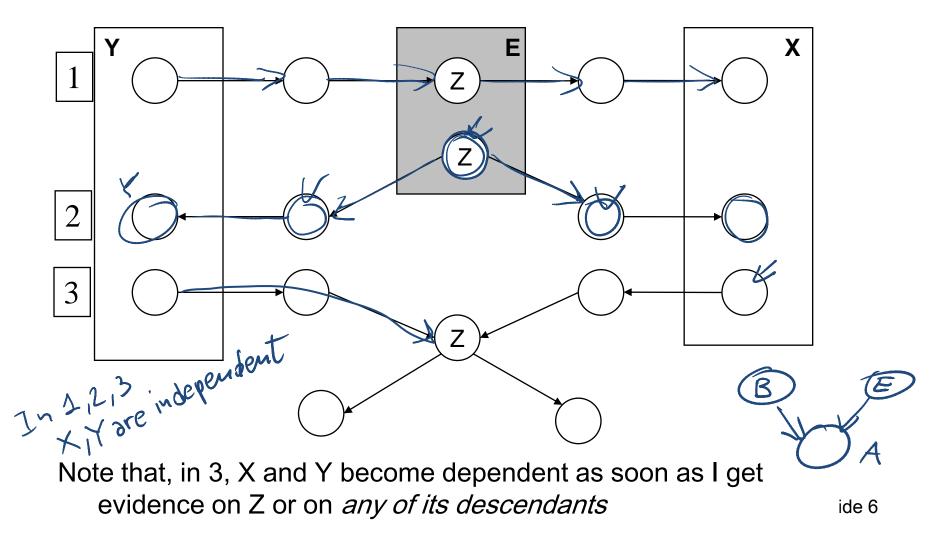
- Implied Conditional Independence relations in a Bnet
- Compactness: Making stronger
   Independence assumptions
  - Representation of Compact Conditional Distributions
  - Network structure( Naïve Bayesian Classifier)

## **Bnets: Entailed (in)dependencies**

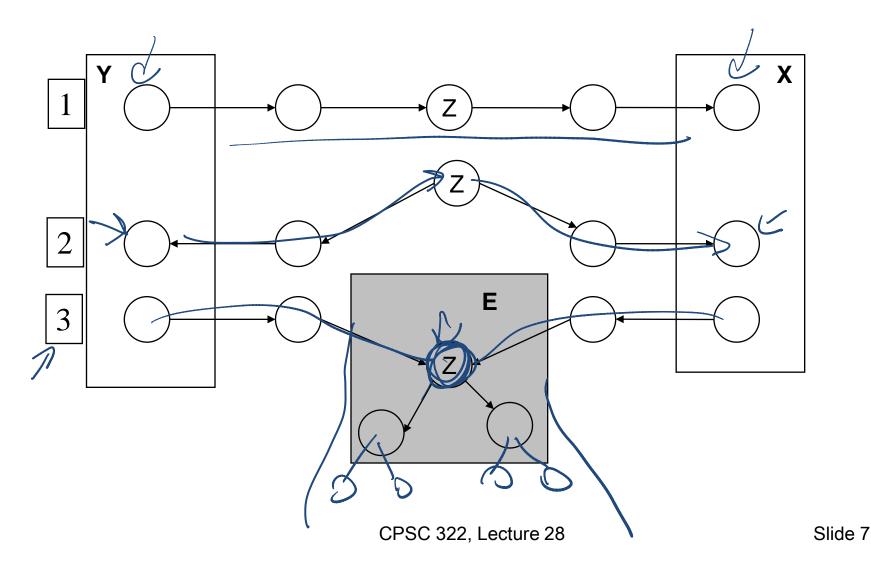


## **Conditional Independencies**

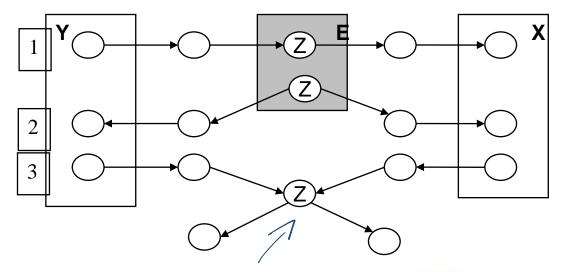
Or, blocking paths for probability propagation. Three ways in which a path between X to Y can be blocked, given evidence E

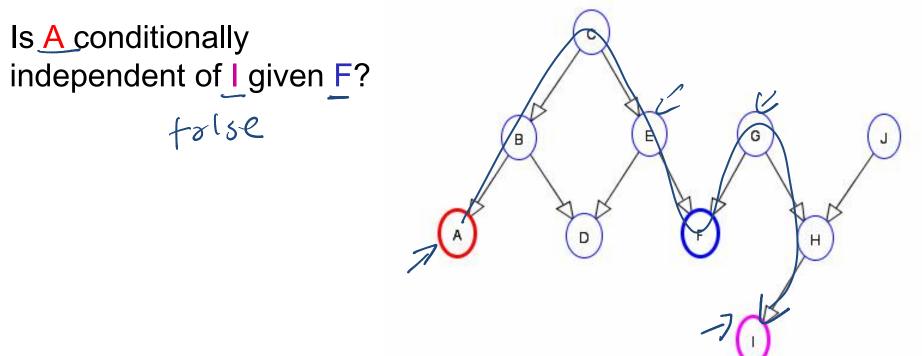


## Or .... Conditional Dependencies In 1,2,3 X Y are dependent

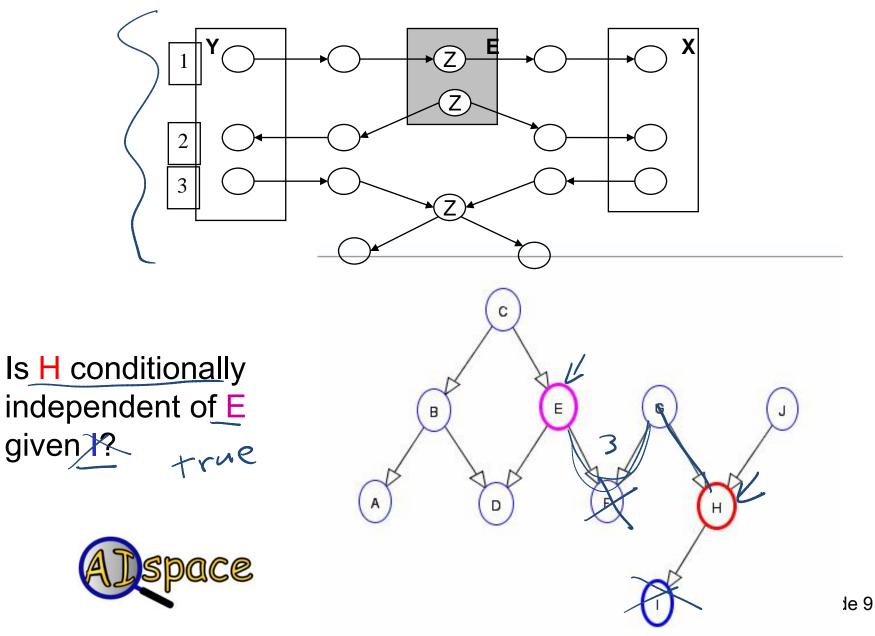


In/Dependencies in a Bnet : Example 1





In/Dependencies in a Bnet : Example 2



## **Lecture Overview**

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#### More on Construction and Compactness: Compact Conditional Distributions

Once we have established the topology of a Bnet, we still need to specify the conditional probabilities How?

- From Data
- From Experts
- To facilitate acquisition, we aim for compact representations for which data/experts can provide accurate assessments

## More on Construction and Compactness: **Compact Conditional Distributions** 47.K

to

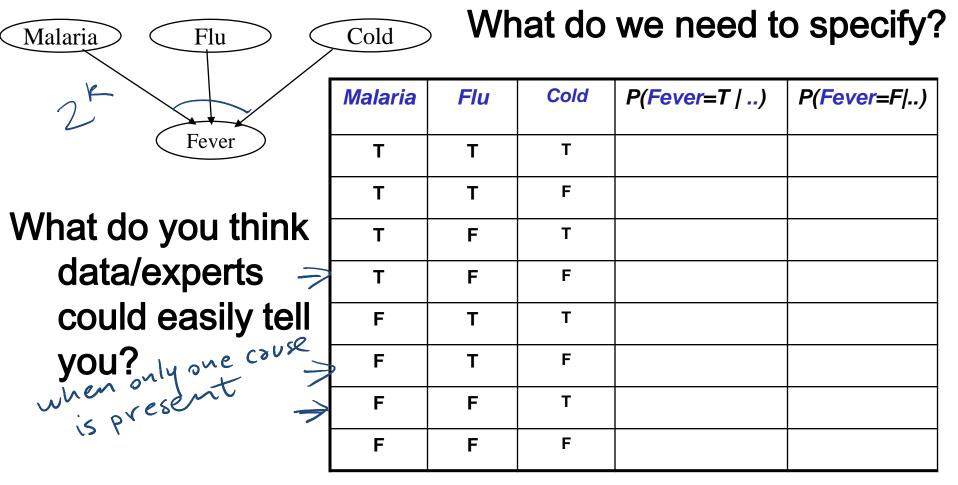
But still, CPT grows exponentially with number of parents

From JointPD

In realistic model of internal medicine with 448 nodes and 906 links 133,931,430 values are required!

And often there are no data/experts for accurate assessment

#### Effect with multiple non-interacting causes



More difficult to get info to assess more complex conditioning....

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#### **Solution: Noisy-OR Distributions**

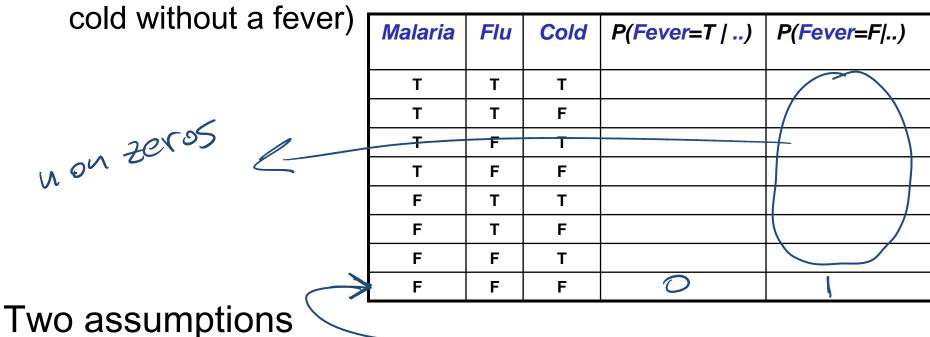
- Models multiple non interacting causes
- Logic OR with a probabilistic twist.
  - Logic OR Conditional Prob. Table.

Malaria	Flu	Cold	P(Fever=T  )	P(Fever=F )
Т	Т	т	l	0
Т	Т	F	l	0
Т	F	т	1	0
Т	F	F	)	0
F	т	т	(	0
F	т	F	)	0
F	F	Т	l	0
F	F	F	0	

## **Solution: Noisy-OR Distributions**

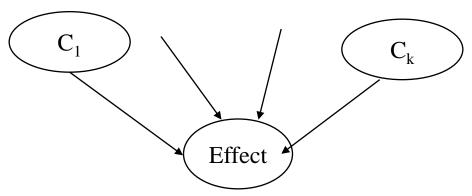
The Noisy-OR model allows for uncertainty in the ability of

each cause to generate the effect (e.g., one may have a

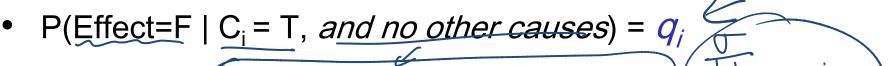


- 1. All possible causes a listed
- 2. For each of the causes, whatever inhibits it to generate the target effect is independent from the inhibitors of the other causes

#### **Noisy-OR: Derivations**



- For each of the causes, whatever inhibits it to generate the target effect is independent from the inhibitors of the other causes
- Independent Probability of failure  $q_i$  for each cause alone:



- P(Effect=F  $(C_1 = T, ..., C_j = T, C_{j+1} = F, ..., C_k = F) = 1$ P(Effect=T  $(C_1 = T, ..., C_j = T, C_{j+1} = F, ..., C_k = F) = 1$

#### **Noisy-OR: Example**

P(Fever=F|Cold=T) Flu=F, Malaria=F) = 0.6 P(Fever=F|Cold=F, Flu=T, Malaria=F) = 0.2 P(Fever=F|Cold=F, Flu=F, Malaria=T) = 0.1 P(Fever=F|Cold=F, Flu=F, Malaria=T) = 0.1

• P(Effect=F |  $C_1 = T, ..., C_j = T, C_{j+1} = F, .., C_k = F) = \prod_{i=1}^{j} q_i$ 

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Malaria	Flu	Cold	P(Fever=T  )	P(Fever=F )		
≫ T	Т	Т	. 988	<u>0.1 x 0.2 x 0.6 = 0.012</u>		
$\rightarrow$ (T)	T	F	-> .98	$0.2 \times 0.1 = 0.02$		
) T	F	Т	. 94	0.6 × 0.1 <b>=0.06</b>		
✓	F	F	0.9	0.1 🧲		
F	Т	Т	. 88	0.2 × 0.6 <b>= 0.12</b>		
F	Т	F	0.8	0.2 ←		
F	F	Т	0.4	0.6		
F	F	F	O requ	nived 1.0		
<ul> <li>Number of probabilities linear in K 3 in this example</li> </ul>						

## **Lecture Overview**

- Implied Conditional Independence relations in a Bnet
- Compactness: Making stronger Independence assumptions
  - Representation of Compact Conditional Distributions
  - Network structure (Naïve Bayesian Classifier)

## Naïve Bayesian Classifier

A very simple and successful Bnets that allow to classify entities in a set of classes C, given a set of attributes

#### Example:

- Determine whether an email is spam (only two classes spam=T and spam=F)

words contained in the email

#### Assumptions

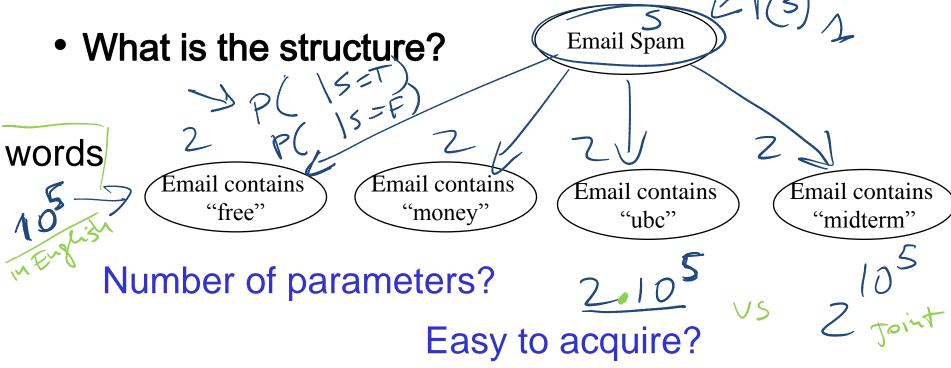
- The value of each attribute depends on the classification
- (Naïve) The attributes are independent of each other given the classification

P("bank" | "account", spam=T) = P("bank" | spam=T)

# Naïve Bayesian Classifier for Email Spam

#### Assumptions

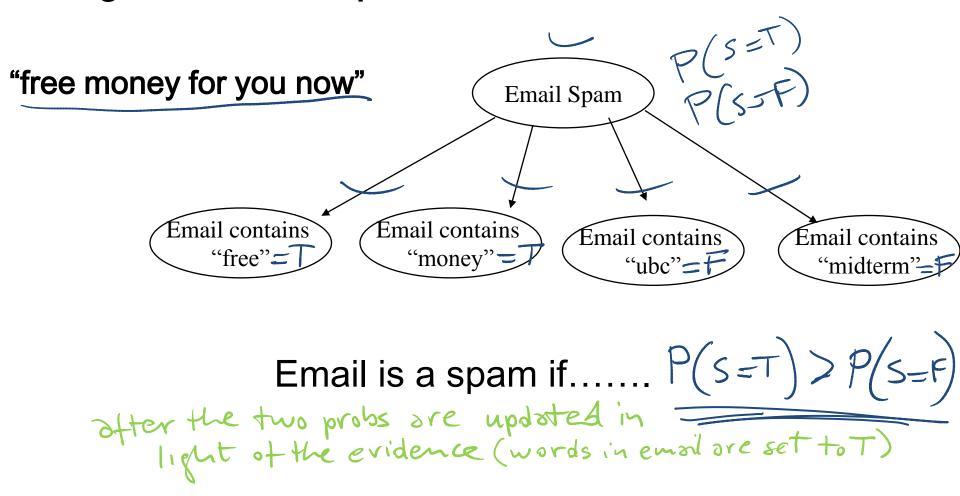
- The value of each attribute depends on the classification
- (Naïve) The attributes are independent of each other given the classification



If you have a large collection of emails for which you know if they are spam or not.....

## NB Classifier for Email Spam: Usage

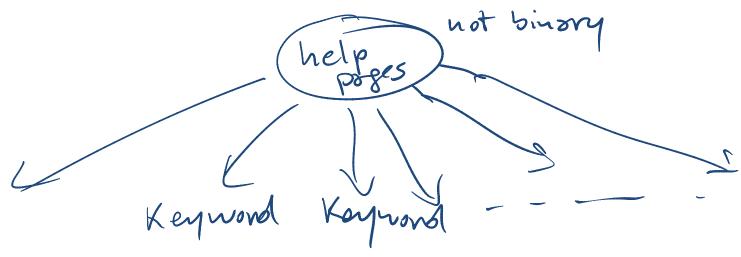
## Most likely class given set of observations Is a given Email *E* spam?



## For another example of naïve Bayesian Classifier

See textbook ex. 6.11

help system to determine what help page a user is interested in based on the keywords they give in a query to a help system.



## Learning Goals for today's class

## You can:

- Given a Belief Net, determine whether one variable is conditionally independent of another variable, given a set of observations.
- Define and use Noisy-OR distributions.
   Explain assumptions and benefit.

 Implement and use a naïve Bayesian classifier. Explain assumptions and benefit.

## **Next Class**

Bayesian Networks Inference: Variable Elimination

## Course Elements

- Practice Exercise on Bnet posted (a second one will follow on Fri)
- Assignment 3 is due on Monday!
- Assignment 4 will be available on Wednesday and due on Apr the 8<sup>th</sup> (last class).