

Uninformed Search

Computer Science cpsc322, Lecture 5

(Textbook Chpt 3.5)

May 18, 2017

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Recap

- **Search** is a key computational mechanism in many **AI agents**
- We will study the basic principles of search on the simple **deterministic planning agent model**

Generic search approach:

- define a search space graph,
- start from current state,
- incrementally explore paths from current state until goal state is reached.

Searching: Graph Search Algorithm with three bugs ☹️

Input: a graph,

a start node,

Boolean procedure $goal(n)$ that tests if n is a goal node.

~~$frontier := \{ \langle g \rangle : g \text{ is a goal node} \}$~~ ← should be initiated with start node

while $frontier$ is not empty:

select and **remove** path $\langle n_0, n_1, \dots, n_k \rangle$ from $frontier$,

if $goal(n_k)$ ←

~~**return** $\langle n_k \rangle$;~~ ← should return the path

for every neighbor n of n_k

~~**add** $\langle n_0, n_1, \dots, n_k, n \rangle$ to $frontier$,~~

end while

No solution found

- The *goal* function defines what is a solution.
- The *neighbor* relationship defines the graph.
- Which path is selected from the frontier defines the search strategy

Lecture Overview

- Recap
- Criteria to compare Search Strategies
- Simple (Uninformed) Search Strategies
 - Depth First
 - Breadth First



Comparing Searching Algorithms: will it find a solution? the best one?

Def. (complete): A search algorithm is **complete** if, whenever at least one solution exists, the algorithm is **guaranteed to find a solution** within a finite amount of time.

Def. (optimal): A search algorithm is **optimal** if, when it finds a solution, it is the best solution

Comparing Searching Algorithms: Complexity

Def. (time complexity)

The **time complexity** of a search algorithm is an expression for the **worst-case** amount of time it will take to run,

- expressed in terms of the **maximum path length m** and the **maximum branching factor b** .

Def. (space complexity) : The **space complexity** of a search algorithm is an expression for the **worst-case** amount of memory that the algorithm will use (*number of nodes*),

- Also expressed in terms of **m and b** .

Lecture Overview

- **Recap**
- Criteria to compare Search Strategies
- Simple (Uninformed) Search Strategies
 - **Depth First**
 - Breadth First

Depth-first Search: DFS

- **Depth-first search** treats the frontier as a stack
- It always selects one of the last elements added to the frontier

Example:

- the frontier is $[p_1, p_2, \dots, p_r]$
- neighbors of last node of p_1 (its end) are $\{n_1, \dots, n_k\}$
- What happens?
 - p_1 is selected, and its end is tested for being a goal. If not...
 - New paths are created attaching $\{n_1, \dots, n_k\}$ to p_1
 - These “replace” p_1 at the beginning of the frontier
 - Thus, the frontier is now $[(p_1, n_1), \dots, (p_1, n_k), p_2, \dots, p_r]$. K new paths
 - NOTE: p_2 is only selected when all paths extending p_1 have been explored.

push ↑ pop ↓

order in which these are added is not specified in pure DFS

If not...

K new paths

Depth-first Search: Analysis of DFS

- Is DFS complete?



- Is DFS optimal?



Depth-first Search: Analysis of DFS

iclicker.

- What is the **time complexity** if the maximum path length is m and the maximum branching factor is b ?

$O(b^m)$

$O(m^b)$

$O(bm)$

$O(b+m)$

iclicker.

- What is the **space complexity**?

$O(b^m)$

$O(m^b)$

$O(bm)$

$O(b+m)$

Depth-first Search: Analysis of DFS Summary

Is DFS **complete**?

- Depth-first search isn't guaranteed to halt on graphs with cycles.
- However, DFS *is* complete for finite acyclic graphs.

Is DFS **optimal**?

What is the **time complexity** if the maximum path length is m and the maximum branching factor is b ?

- The time complexity is $O(b^m)$? must examine every node in the tree.
- Search is unconstrained by the goal until it happens to stumble on the goal.

What is the **space complexity**?

- Space complexity is $O(mb)$? the longest possible path is m , and for every node in that path must maintain a fringe of size b .

Analysis of DFS

Def. : A search algorithm is **complete** if whenever there is at least one solution, the algorithm is guaranteed to find it within a finite amount of time.

Is DFS complete?

No

- If there are cycles in the graph, DFS may get “stuck” in one of them
- see this in AISpace by adding a cycle to “Simple Tree”
 - e.g., click on “Create” tab, create a new edge from N7 to N1, go back to “Solve” and see what happens



Analysis of DFS

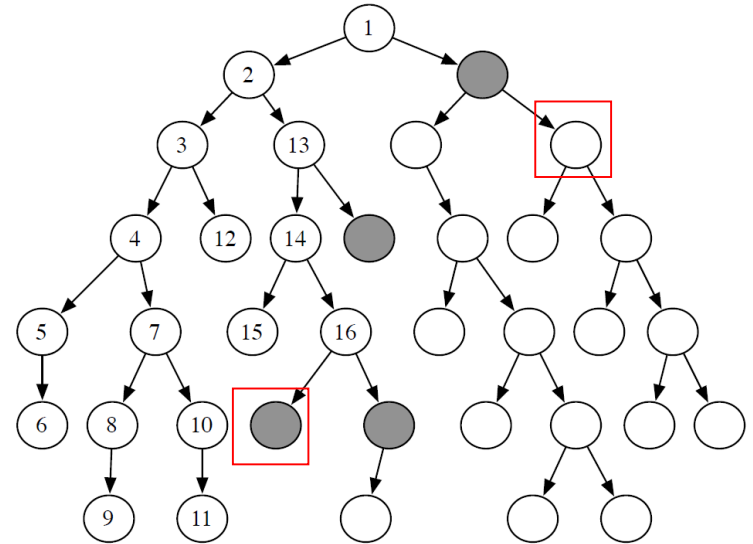
Def.: A search algorithm is **optimal** if when it finds a solution, it is the best one (e.g., the shortest)

Is DFS optimal?

Yes

No

- E.g., goal nodes: red boxes



Analysis of DFS

Def.: The **time complexity** of a search algorithm is the **worst-case** amount of time it will take to run, expressed in terms of

- maximum path length m
- maximum forward branching factor b .

- What is DFS's **time complexity** in terms of m and b ?

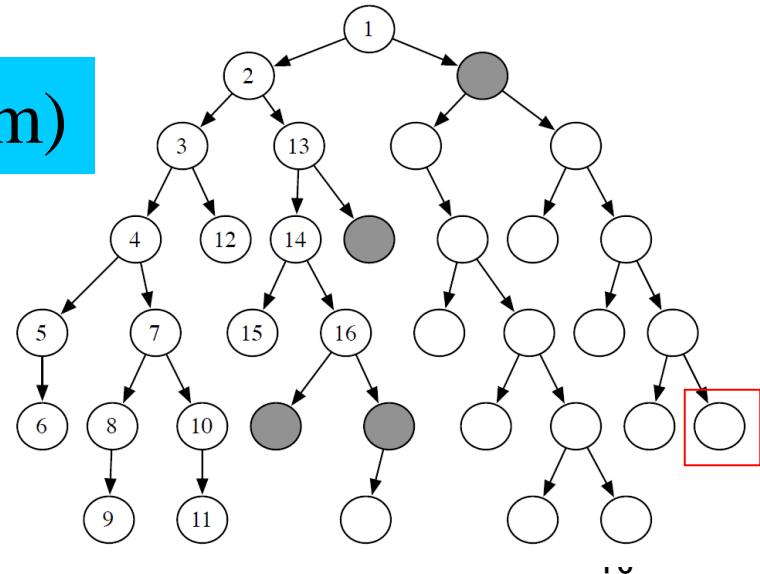
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$O(m^b)$

$O(bm)$

$O(b+m)$

- E.g., single goal node \rightarrow red box



Analysis of DFS

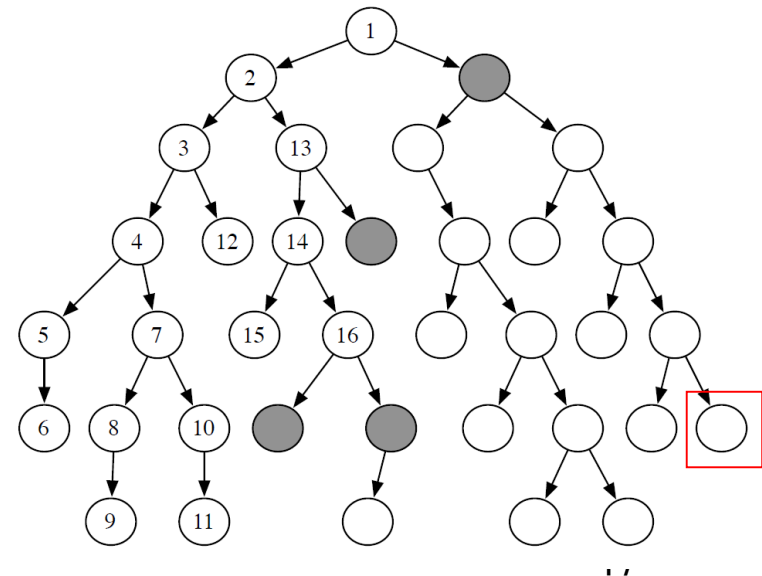
Def.: The **time complexity** of a search algorithm is the **worst-case** amount of time it will take to run, expressed in terms of

- maximum path length m
- maximum forward branching factor b .

- What is DFS's **time complexity**, in terms of m and b ?

$$O(b^m)$$

- In the worst case, must examine every node in the tree
 - E.g., single goal node \rightarrow red box



Analysis of DFS

Def.: The **space complexity** of a search algorithm is the **worst-case** amount of memory that the algorithm will use (i.e., the maximal number of nodes on the frontier), expressed in terms of

- maximum path length m
- maximum forward branching factor b .

- What is DFS's **space complexity**, in terms of m and b ?

$O(b^m)$

$O(m^b)$

$O(bm)$

$O(b+m)$

See how this works in



Analysis of DFS

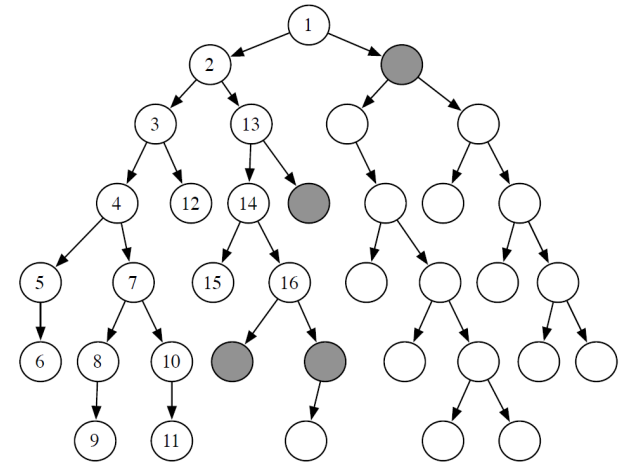
Def.: The **space complexity** of a search algorithm is the **worst-case** amount of memory that the algorithm will use (i.e., the maximum number of nodes on the frontier), expressed in terms of

- maximum path length m
- maximum forward branching factor b .

- What is DFS's **space complexity**, in terms of m and b ?

$O(bm)$

- for every node in the path currently explored, DFS maintains a path to its unexplored siblings in the search tree
 - Alternative paths that DFS needs to explore
- The longest possible path is m , with a maximum of $b-1$ alternative paths per node



See how this works in





Depth-first Search: When it is appropriate?



- A. There are cycles
- B. Space is restricted (complex state representation e.g., robotics)
- C. There are shallow solutions
- D. You care about optimality

Depth-first Search: When it is appropriate?

Appropriate

- Space is restricted (complex state representation e.g., robotics) 
- There are many solutions, perhaps with long path lengths, particularly for the case in which all paths lead to a solution 




clicker question?

Inappropriate

- Cycles
- There are shallow solutions
- if you care about optimality!

Why DFS need to be studied and understood?

- It is simple enough to allow you to learn the basic aspects of searching (When compared with breadth first)

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- It is the basis for a number of more sophisticated / useful search algorithms

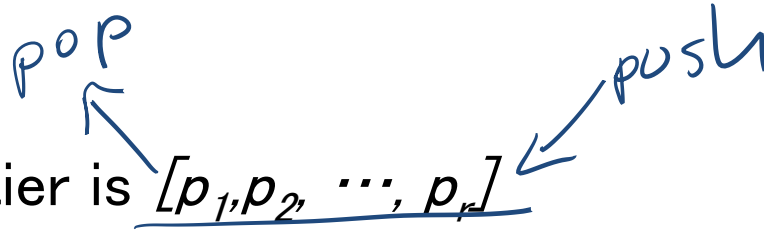
Lecture Overview

- **Recap**
- **Simple (Uninformed) Search Strategies**
 - Depth First
 - Breadth First

Breadth-first Search: BFS

- Breadth-first search treats the frontier as a **queue**
 - it always selects one of the earliest elements added to the frontier

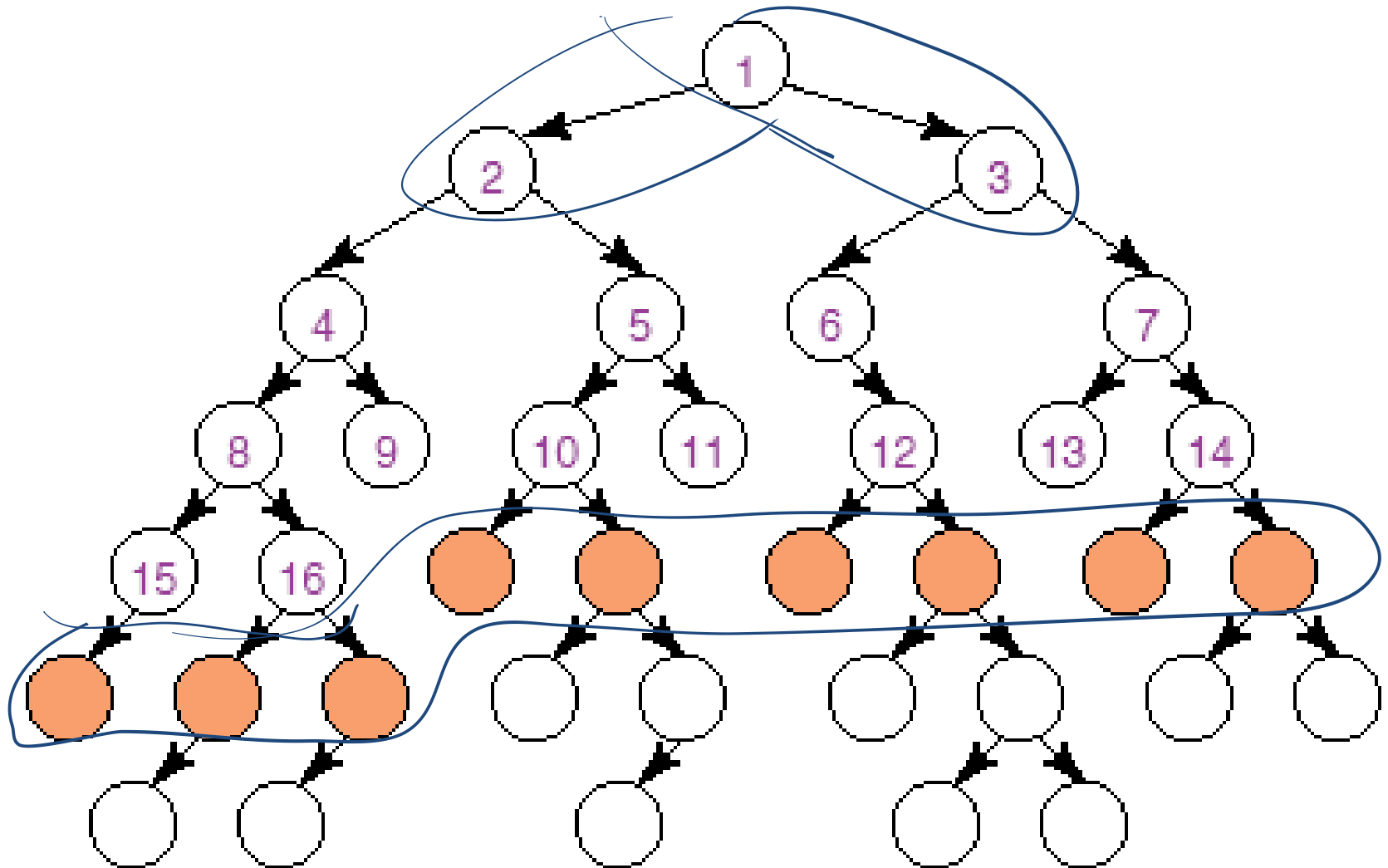
Example:



- the frontier is $[p_1, p_2, \dots, p_r]$
- neighbors of the last node of p_1 are $\{n_1, \dots, n_k\}$
- What happens?
 - p_1 is selected, and its end tested for being a path to the goal.
 - New paths are created attaching $\{n_1, \dots, n_k\}$ to p_1
 - These follow p_r at the end of the frontier
 - Thus, the frontier is now $[p_2, \dots, p_r, (p_1, n_1), \dots, (p_1, n_k)]$.
 - p_2 is selected next.



Illustrative Graph – Breadth-first Search



Breadth-first Search: Analysis of BFS

- Is BFS complete?



- Is BFS optimal?



Breadth-first Search: Analysis of BFS

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- What is the **time complexity** if the maximum path length is m and the maximum branching factor is b ?

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iclicker.

- What is the **space complexity**?

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$O(bm)$


$O(b+m)$

Analysis of Breadth-First Search

- Is BFS complete?

- Yes



- In fact, BFS is guaranteed to find the path that involves the fewest arcs (why?) 

- What is the time complexity if the maximum path length is m and the maximum branching factor is b ?



- The time complexity is $O(b^m)$? must examine every node in the tree.



- The order in which we examine nodes (BFS or DFS) makes no difference to the worst case: search is unconstrained by the goal.

- What is the space complexity?

- Space complexity is $O(b^m)$?

Using Breadth-first Search

- When is BFS **appropriate**?
 - space is not a problem 
 - it's necessary to find the solution with the fewest arcs *optimality*
 - although all solutions may not be shallow at least some are


- When is BFS **inappropriate**?
 - space is limited
 - all solutions tend to be located deep in the tree 
 - the branching factor is very large 

What have we done so far?

GOAL: study search, a set of basic methods underlying many intelligent agents

AI agents can be very complex and sophisticated

Let's start from a very simple one, **the deterministic, goal-driven agent** for which: the sequence of actions and their appropriate ordering is the solution

We have looked at two search strategies DFS and BFS:

- To understand key properties of a search strategy
- They represent the basis for more sophisticated (heuristic / intelligent) search

Learning Goals for today's class

- Apply basic properties of search algorithms: completeness, optimality, time and space complexity of search algorithms.

	Comp	opt	time	Space
<u>DFS</u>	→ False	False	b^m	$\begin{matrix} mb \\ b^m \end{matrix}$
<u>BFS</u>	→ True	True	b^m	

- Select the most appropriate search algorithms for specific problems.

- BFS vs DFS vs IDS vs BidirS-
- LCFS vs. BFS -
- A* vs. B&B vs IDA* vs MBA*

next 4 lectures

informed

To test your understanding of today's class

- Work on **Practice Exercise 3.B**
- <http://www.aispace.org/exercises.shtml>

Next Class

- Iterative Deepening
- Search with cost
(read textbook.: 3.7.3, 3.5.3)

- (maybe) Start Heuristic Search
(textbook.: start 3.6)

Recap: Comparison of DFS and BFS

	Complete	Optimal	Time	Space
DFS	\bar{N} (Y if no cycles)	Y N	$O(b^m)$	$O(b^m)$
BFS	Y	Y	$O(b^m)$	$O(b^m)$