

The Sounds of Physical Shapes*

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Abstract

We propose a general framework for the simulation of sounds produced by colliding physical objects in a virtual reality environment. The framework is based on the vibration dynamics of bodies. The computed sounds depend on the material of the body, its shape, and the location of the contact.

This allows the user to obtain important auditory clues about the objects in the simulation, as well as about the locations on the objects of the collisions.

Specifically, we show how to compute (1) the spectral signature of each body (its natural frequencies), which depends on the material and the shape, (2) the “timbre” of the vibration (the relative amplitudes of the spectral components) generated by an impulsive force applied to the object at a grid of locations, (3) the decay rates of the various frequency components which correlates with the type of material, based on the its internal friction parameter and finally (4) the mapping of sounds on to the object’s geometry for real time rendering of the resulting sound.

The framework has been implemented in a Sonic Explorer program, which simulates a room with several objects such as a chair, tables, and rods. After a preprocessing stage, the user can hit the objects at different points to interactively produce realistic sounds.

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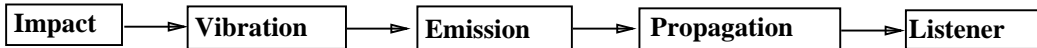


Figure 1: Sound Pipeline.

1 Introduction

What information is conveyed by the sound of a struck object? Before reading further, you may want to try the following informal experiment. Tap on the physical objects around you like tables and file cabinets and listen to the sounds produced. First tap an object lightly and then try hitting it harder. Tap on wooden objects and metal objects. Tap on small objects like cups and telephones and large objects like tables and doors. Finally, for each object, try tapping it near the center, around the edges, from the side, and at other locations on the object. Most people can hear clear differences between the sounds in each of these cases.

When an object is struck, the energy of impact causes deformations to propagate through the body, causing its outer surfaces to vibrate and emit sound waves. The resulting sound field propagates through and also interacts with the environment before reaching the inner ear where it is sensed. Real sounds therefore provide an important “image” of various physical attributes of the object, its environment and the impact event, including the force (or energy) of the impact, the material composition of the object, the shape and size, the place of impact on the object, and finally the location and environment of the object.

In this paper we show how to synthesize realistic sounds from physical models of the geometry and material properties of objects.

The cognitive importance of realistic sounds is well known in the entertainment industry where sampled sound effects are added to the scene to enhance realism. As simulations become more interactive, for instance in large architectural walkthroughs [2] and virtual reality, synthesizing realistic object sounds directly from physical models and rendering them in real time will be increasingly important.

The generation of sounds can be characterized as shown in Figure 1, which depicts the process as a pipeline similar to the sound rendering pipeline of [24]. While this is a simplification, it indicates the major computational tasks in going from a collision event to the sound heard by a human ear.

The focus of the paper is the initial stage of this pipeline: the computation of the sounds produced by vibrations of the object, which depend on the geometry of the object, its material properties, and the characteristics of the impact. For completeness we also briefly describe other parts of the pipeline such as impact dynamics and environment modeling.

1.1 Related Work

A review of the scientific and technological issues of auditory displays can be found in [5]. An overview of the physical factors involved in producing natural sounds was presented in

[10]. Several synthesis methods for impact, scraping, and composite sounds were described in [9]. However, no method was given to compute the free parameters of the synthesis methods, such as the set of eigenfrequencies, the relative amplitudes of the partials, and the bandwidths of the frequencies. With the methods described in this paper, the parameters of these synthesis methods can be computed.

Takala and Hahn introduced the concept of sound rendering for computer animation [24]. They associated a characteristic sound with each object which could then be rendered after filtering the sound to model the environmental effects. Recently [12] they proposed “Timbre Trees,” which, like shade trees, provide a scene description language for sounds. While [24] indicated that the collision sounds could, in principle, be generated from vibration analysis, they were concerned mainly with the modulation of sound due to material properties. They did not synthesize sounds which account for the shapes of the colliding objects or the location of the collision on the objects.

Much progress has been made recently with the simulation of the filtering of sound by the human ear and head, giving the illusion of sound coming from various directions. Off-the-shelf audio hardware is already available to “place” a sound in space, using the “head related transfer function”. For a review of this topic we refer to [3].

Offline computation of acoustical properties of performance halls, in the context of graphical visualization techniques was investigated in [22].

In [26, 15] the problem of recovering the material type from impact sounds was investigated, and it was proposed to use the internal friction parameter, which is an approximate material property, as a characteristic signature of the material. In this paper we invert this approach, by relating the material properties of the synthesized sounds to the decay rates of the partials with the internal friction parameter.

For a more mathematically oriented example of the relation between shape and sound for membranes, we refer to the long standing open problem “Can one hear the shape of a drum?”, which was posed in 1966 [14]. Recently counterexamples have been found [11].

A standard work on acoustics is [17]. For a book on vibration analysis we refer to [6]. For an application of vibration analysis to animation, see [18]. A survey of the use of the auditory channel in virtual reality is given in [5, Chapter 3]. More general treatises on sound and hearing are [16, 4].

1.2 Overview

In this article we investigate the computation and rendering of sounds emitted by colliding bodies. When we strike an object such as a metal bar, we hear a brief transient or click, with a complex frequency spectrum, followed by a more or less sustained sound, which decays. In Figure 1.2 we show the waveform of a sound of a daf, which is a large drum. It shows the noisy onset of the sound, followed by a smoother part. The click or onset has some role in identifying the sound. For example, try listening to a recording of a flute played backwards. The sound is no longer as clearly recognizable as a flute, even though the sustained part of the sound is unchanged. See also [4, 16].



Figure 2: Waveform of a daf.

Nevertheless, most information about the nature of the object is present in the sustained part. To obtain this, we need to compute the vibrations of an object when it is struck, and compute the resulting sound emitted.

The sound made by a struck object depends on many factors, of which we consider the following:

1. *The shape of the object.* The propagation of vibrations in the object depends on its geometry. This is why a struck gong sounds very different from a struck piano string, for example. Shape and material together determine a characteristic frequency spectrum.
2. *The location of the impact.* The timbre of the sound, i.e. the amplitudes of the frequency components, depends on where the object is struck. For example, a table struck at the edges makes a different sound than when struck at the center.
3. *The material of the struck object.* The harder the material, the brighter the sound. We also relate the material to the decay rate of the frequency components of the sound through the internal friction parameter, see below.
4. *The force of the impact.* Typically, the amplitude of the emitted sound is proportional to the square root of the energy of the impact.

All these factors give important cues about the nature of an object and about what is happening to an object in the simulation.

Based on material and shape properties, we do a precomputation of the relevant characteristic frequencies of each object in Section 2. In Section 3 we then divide the boundary of the object into small regions and determine the amplitudes of the excitation modes if an impulsive force is applied to a point in this region.

This is similar to the tessellation of a surface for graphics rendering. The whole procedure is analogous to assigning a color to a surface and rendering it with some shading model. Although the role of sound synthesis differs in many aspects from the role of graphics, there are some useful analogies that can be drawn between the two. We show one possible

Sound	Graphics
Material	Color
Spatialization	Perspective projection
Shape	Shape
Impact	Light Ray
Reverberation	Raytracing and radiosity

Table 1: Graphics-Audio analogies.

correspondence in Figure 1.2. Shape, impact location, and material are the focus of this paper.

In Section 4, we normalize the energies of the vibrations associated with the different impact points to some constant value, and scale them proportional to the impact energy when rendered.

The decay rate of each mode is assumed to be determined by the internal friction parameter, which is an approximate material property [26, 15]. In effect, the decay rate of a component is assumed to be proportional to the frequency, with the constant determined by the internal friction parameter.

Besides the natural frequencies there is a brief transient, a “click”, mentioned before, which we model by a short burst of white noise.

After the preprocessing, a sound map is attached to an object, which allows us to render sounds resulting from impacts on the body. We discuss the structure of this map and a possible approach to reduce its storage requirements in Section 5.

We have constructed a testbed application, called the “Sonic Explorer”, which demonstrates the level of reality that can be achieved within this model. The Sonic Explorer is currently set up to precompute the impact sounds of several types of objects, incorporate them in a real time interactive simulation, and render them in real time, using the audio hardware. This is described in Section 6. A picture of a virtual room environment is given in Figure 3.

2 Vibrating Shapes from Impact

We now introduce the framework for modeling vibrating objects. We will illustrate it with a rectangular membrane, but the framework is quite general; we have used it to generate sounds of strings, bars, plates and other objects. The framework is based on the well developed models in the literature on vibration or acoustics, for example [17] – for the calculus involved we refer to [23].

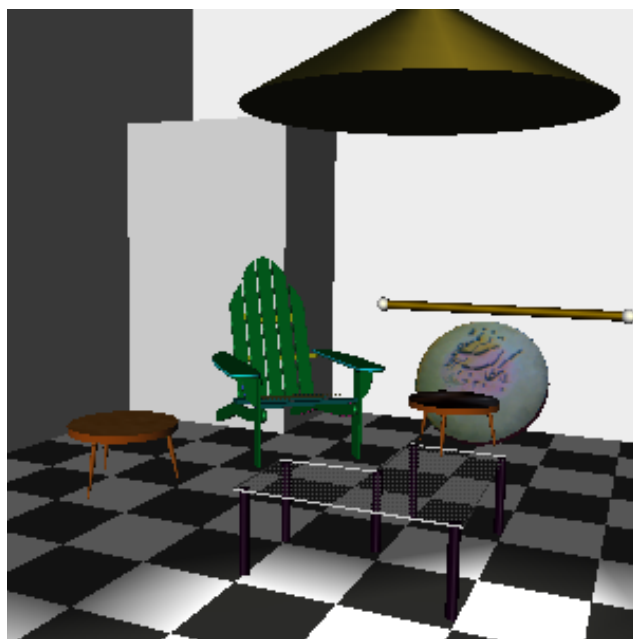


Figure 3: A room modeled with the Sonic Explorer

2.1 Vibration Modes from Shape

The vibration of the object is described by a function $\mu(\mathbf{x}, t)$, which represents the deviation from equilibrium of the surface, defined on some region \mathcal{S} , which defines the shape of the object. We assume that μ obeys a wave equation of the form

$$\left(A - \frac{1}{c^2} \frac{\partial^2}{\partial t^2}\right) \mu(\mathbf{x}, t) = F(\mathbf{x}, t) \quad (1)$$

with c a constant (related to the speed of sound in the material), and A is a self-adjoint differential operator, under the boundary conditions on $\partial\mathcal{S}$. In the following we shall assume that the external force, $F(\mathbf{x}, t)$, is zero.

Example: For the rectangular membrane we consider a rectangle $[0 - L_x, 0 - L_y]$ spanned by a membrane under uniform tension. For this case the operator A is given by

$$A = \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2}$$

The boundary conditions are that $\mu(x, y, t)$ is fixed on the boundary of the membrane, i.e. the membrane is attached to the rectangular frame. \square

We will take the following initial value conditions.

$$\mu(\mathbf{x}, 0) = y_0(\mathbf{x}),$$

i.e. the surface is initially in configuration $y_0(\mathbf{x})$, and

$$\frac{\partial \mu(\mathbf{x}, 0)}{\partial t} = v_0(\mathbf{x}),$$

where $v_0(\mathbf{x})$ is the initial velocity of the surface.

The solution to Equation 1 is written as

$$\mu(\mathbf{x}, t) = \sum_{n=1}^{\infty} (a_n \sin(\omega_n ct) + b_n \cos(\omega_n ct)) \Psi_n(\mathbf{x}), \quad (2)$$

where a_n and b_n are arbitrary real numbers, to be determined by the initial value conditions. The ω_n are related to the eigenvalues of the operator A under the appropriate boundary conditions (which we specify below), and the functions $\Psi_n(\mathbf{x})$ are the corresponding eigenfunctions. That is, we have

$$(A + \omega_n^2) \Psi_n(\mathbf{x}) = 0. \quad (3)$$

The spectrum of a self-adjoint operator A is discrete, and the eigenfunctions are orthogonal. Their norm is written as

$$\alpha_n = \int_{\mathcal{S}} \Psi_n^2(\mathbf{x}) d^k x.$$

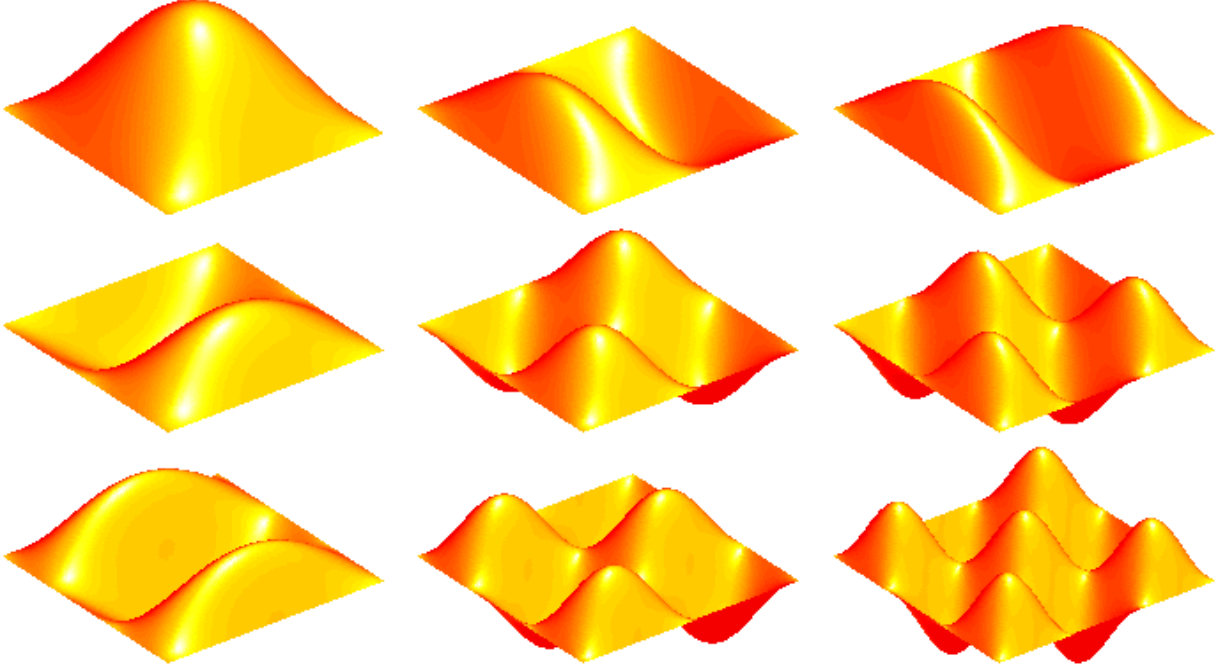


Figure 4: First nine eigenfunctions of a square membrane.

Example: For the rectangular membrane, the eigenfunctions and eigenvalues are most naturally labeled by two positive integers n_x and n_y and are given by

$$\Psi_{n_x n_y}(x, y) = \sin(\pi n_x x / L_x) \sin(\pi n_y y / L_y),$$

and

$$\omega_{n_x n_y} = \pi \sqrt{\left(\frac{n_x}{L_x}\right)^2 + \left(\frac{n_y}{L_y}\right)^2},$$

In Figure 2.1, we show the first 9 eigenfunctions on a square membrane. \square

As Equation 3 is linear, we can normalize the eigenfunctions $\Psi_n(\mathbf{x})$ such that α_n is independent of n , which often simplifies some of the algebra. Using the orthogonality of the eigenfunctions we can find the coefficients in the expansion given in Equation 2 as

$$a_n = \int_S \frac{v_0(\mathbf{x}) \Psi_n(\mathbf{x})}{c \alpha_n \omega_n} d^k x, \quad (4)$$

and

$$b_n = \int_S \frac{y_0(\mathbf{x}) \Psi_n(\mathbf{x})}{\alpha_n} d^k x. \quad (5)$$

The time averaged energy of the vibration is given by

$$E = \text{constant} \times \left\langle \int_S \left(\frac{\partial \mu(\mathbf{x}, t)}{\partial t} \right)^2 \rho(\mathbf{x}) d^k x \right\rangle, \quad (6)$$

where $\rho(\mathbf{x})$ is the mass density of the vibrating object. The $\langle \rangle$ indicates an average over time. If the mass is distributed uniformly, we have

$$E = \text{constant} \times \sum_{n=1}^{\infty} \alpha_n \omega_n^2 (a_n^2 + b_n^2). \quad (7)$$

2.2 Mode Amplitudes from Impact Location

Next we compute the vibrations resulting from an impact at some point \mathbf{p} , when the body is initially at rest.

The initial value conditions are taken to be

$$y_0(\mathbf{x}) = 0, \quad (8)$$

and

$$v_0(\mathbf{x}) = \delta(\mathbf{x} - \mathbf{p}), \quad (9)$$

with $\delta(\mathbf{x})$ the k -dimensional Dirac delta function.

We note that Equation 9 is not strictly correct as an initial value condition. The reason is that the expression for the energy, given in Equation 6 involves the square of the time derivative of $\mu(\mathbf{x}, t)$. But the integral of the square of the Dirac delta function is infinite. One symptom of this is that the infinite sum appearing in Equation 2 does not converge. A mathematically more correct method would replace the delta function in the initial value conditions by some strongly peaking external force function, representing the impact on a small region of the object over a finite region and over a small but finite extension in time. However, this would complicate things quite a bit, and we would gain little in terms of more realistic sounds. Therefore we shall just assume an appropriate frequency cutoff in the infinite sum appearing in equations 7 and 2. Typically, we will only use the frequencies in the audible range. For more details and a more rigorous treatment of this problem for the special cases of the ideal string and the circular membrane, see [17].

Using equations 8 and 9, and substituting them in equations 4 and 5 we obtain the amplitudes of the vibration modes as a function of the impact location as

$$a_n = \frac{\Psi_n(\mathbf{p})}{c\alpha_n\omega_n}, \quad (10)$$

and

$$b_n = 0.$$

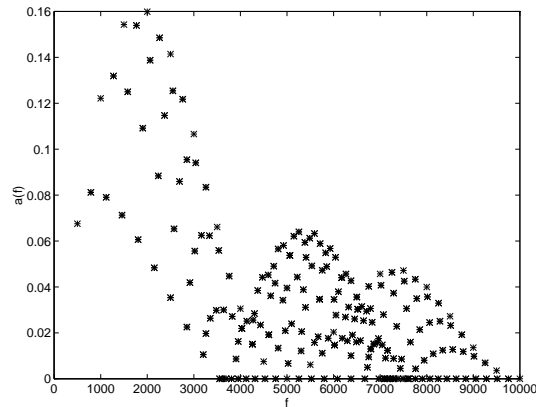


Figure 5: Square membrane struck at $(0.1, 0.1)$.

The energy of the vibration is determined by the impact strength. It will be used to scale the amplitudes of Equation 10. The energy is given by

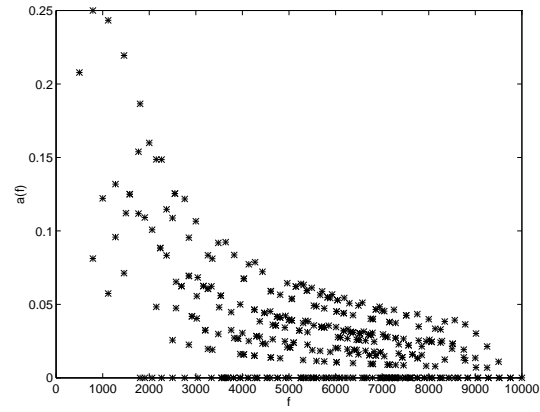
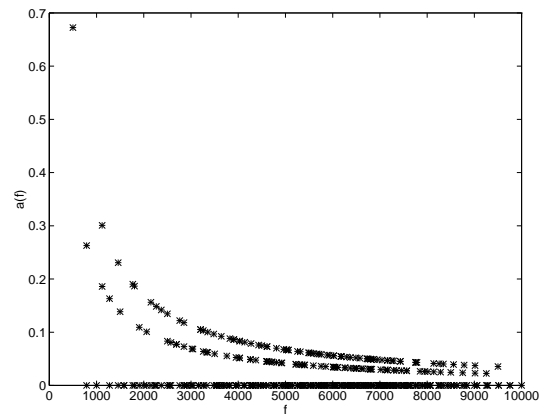
$$E = \text{constant} \times \sum_{n=1}^{n_f} \frac{\Psi_n^2(\mathbf{p})}{\alpha_n},$$

where n_f is determined by the frequency cutoff mentioned above.

Example: In Figures 2.2 to 2.2 we show the amplitudes a_n , graphed against the frequency of the modes (i.e. ω_n) for a square membrane struck at the points $(0.1, 0.1)$, $(0.1, 0.4)$, and $(0.5, 0.4)$. We have taken the lowest frequency to be 500 Hz and taken the first 400 modes into account. We can see clearly that the higher frequencies become relatively more excited for strike points near the boundary of the membrane. In other words, the membrane sounds dull when struck near the center, and bright (or sharp) when struck near the rim. \square

The method outlined above is very general, and allows the computation of the vibrations under impact of any object governed by a differential equation of the form given in Equation 1.

The frequency spectrum ω_n and the eigenfunctions $\Psi_n(\mathbf{x})$ can be computed analytically in a number of cases. In general one has to resort to numerical methods. For membranes, the problem reduces to the solution of the Laplace equation on a given domain, which is a well studied problem. We mention the method of particular solutions [7], which we have adapted for the example of the L-shaped membrane, described below in Section 6. For plates, the operator A is fourth order, and a more general finite element method can be used. See for example [13].

Figure 6: Square membrane struck at $(0.1, 0.4)$.Figure 7: Square membrane struck at $(0.5, 0.4)$.

3 Sound Sources from Vibrating Shapes

Suppose one has obtained the frequency spectrum and the eigenfunctions, as shown in Section 2.

What is the relation between the vibration of the object and the sound emitted? In general the sound-field around a vibration body is very complicated and non-uniform. However, it is clear that the sound emitted can be described as a sum of monochromatic components with frequencies $\omega_n c$, and amplitudes a_n^S , which will depend on the location of the observer with respect to the object, as well as on the environment.

As a first approximation, we will identify the coefficients a_n^S with the vibration amplitudes a_n , scaled with the inverse of the distance to the observer, as the amplitude decays inversely proportional to the distance.

This is not strictly correct, but we argue that it is reasonable as follows. Consider a vibrating plate. At some point above the plate, waves emerging from all locations on the plate arrive at this point. Some will be in phase, and some will be out of phase. This interference will depend very sensitively on the location of the observation point. However, in most real situations, the sound will not only arrive directly from the source, but also from reflections from the walls and other objects in the room. The total effect of this is to average out the phase differences, making the sound-field less sensitive to the locations of the listener.

As a heuristic, we assume that the intensity (i.e. the energy) of the sound emitted in frequency ω_n , I_n , is given by

$$I_n = E_n \int_{\mathcal{S}} \Psi_n^2(\mathbf{x}) = \text{constant} \times \Psi_n^2(\mathbf{p}).$$

This seems reasonable, as it integrates the intensity of the vibration, but not the phase. This means, we can identify the a_n^S , which are the amplitudes of the heard sound, with the a_n given in Equation 10, omitting the factor α_n . Note that since we assumed that the eigenfunctions are normalized so that the α_n are independent of n , this does not matter.

Finally, we obtain the amplitudes a_n^S as

$$a_n^S = \frac{E_{\text{impact}} \Psi_n(\mathbf{p})}{\omega_n Q(\mathbf{p}) d}, \quad (11)$$

with d the distance from the sound source, E_{impact} the energy of the impact, and

$$Q(\mathbf{p}) = \sqrt{\sum_{i=1}^{n_f} \Psi_n^2(\mathbf{p})},$$

with n_f a suitable frequency cutoff. Of course, the a_n^S are only defined up to a multiplicative constant (corresponding to the volume setting of the audio hardware).

For a more detailed treatment of the radiation of vibrating plates, we refer to books on vibration analysis [19, 20, 6].

4 Sounds and Material Properties

When the object is struck, each frequency mode is excited with an initial amplitude a_i , which depends on where the object is struck. The relative magnitudes of the amplitudes a_i determines the “timbre” of the sound. Each mode is assumed to decay exponentially, with decay time

$$\tau_i = \frac{1}{\pi f_i \tan \phi}, \quad (12)$$

where ϕ is the internal friction parameter. The internal friction parameter is roughly invariant over object shape, and depends on the material only. In [26] a method was proposed to identify the material type from the sound emitted by a struck object, by extracting the internal friction parameter of the material via Equation 12. Such a model is also used in [24] to simulate object sounds. Some experiments were reported in [15], where it was concluded that a rough characterization of material was indeed possible. However, the internal friction parameter is only approximately invariant over object shape. See also [25].

To emulate external damping of the object, we add an overall decay factor of e^{-t/τ_0} . This also allows us to adjust the length of the emitted sound, while maintaining its “material character”, which is determined by ϕ .

So we assume the sound-wave $p_S(t)$ to be given for $t \geq 0$ (for $t < 0$ it is zero) by

$$p_S(t) = e^{-t/\tau_0} \sum_{i=1}^{n_f} a_i^S e^{-t f_i \pi \tan \phi} \sin(2\pi f_i t), \quad (13)$$

with the amplitudes a_i^S given in Equation 11, and

$$f_i = \frac{\omega_n c}{2\pi},$$

with the ω_n determined by Equation 1.

5 The Sound Map

In the preprocessing stage we first compute the frequency spectrum f_i , and then the excitation spectrum a_i under a suitably normalized impact (i.e. with fixed energy) for a number of locations on the surface. We can then compute digital samples of the sound-wave $p_S(t) + p_C(t)$ for these locations and store them for playback during the real time simulation. This is somewhat analogous to texture mapping in computer graphics. Alternatively, if appropriate real time sound-synthesis hardware is available, only the model parameters need to be stored, as the sound can be computed on the fly. An interpolation of the timbre spectrum a_i^S between precomputed locations is also obvious to implement.

As digital sound samples take a lot of space we do not want to store any more than we need. So one may ask how many points on the surface need to be computed. In general, the timbre of the sound changes non-uniformly over the surface. For example, a string sounds

“dull” when plucked near the center, and becomes dramatically brighter when excited near the endpoints. In this case, one would need a denser set of points near the ends.

Given two sounds S_1 and S_2 , a measure $d(S_1, S_2)$ is needed, that tells us how different sound S_1 “sounds” from sound S_2 , such that if $d(S_1, S_2) < d_0$, with d_0 a threshold (depending on the individual), S_1 and S_2 can not be distinguished. Perception of timbre is a complex subject, see for example [4, 16] for a discussion, so we can not expect to be able to formulate such a sound-distance measure easily and accurately. A complication is that the principal distinguishing factor between pitched sound is the perceived pitch, which is usually the same in our case, so our timbre measure depends on subtle and poorly understood aspects of audio psychology.

As an initial proposal we take the sonic distance $d(S_1, S_2)$ between two sounds to be

$$d^2(S_1, S_2) = \sum_{i=1}^{n_f} S(f_i) (H(\log(E_i^1/E_0)) - H(\log(E_i^2/E_0)))^2,$$

where E_i^r denotes the energy contribution of the i -th mode of sound r ($= 1, 2$), i.e. $E_i^r = (a_i^{S_r})^2 f_i^2$. We take the logarithm of the energy, as the human ear is sensitive to the logarithm of intensity (measured in decibels). The function $H(x)$ is zero for $x < 0$, and x otherwise. The constant E_0 represents the lowest sound-level that can be heard, so the term $H(\log(E_i^r/E_0))$ vanishes if $E_i^r < E_0$. The function $S(f)$ models the sensitivity of the ear to frequency. Without loss of generality we take $0 \leq S(f) \leq 1$. The function $S(f)$ has to be determined psychoacoustic experiments.

We have ignored the “masking” effect, which changes the sensitivity curve of the ear in the presence of other stimuli. One could also argue that the threshold energy E_0 depends on frequency.

We leave a refinement of the measure d as a topic for future research.

6 Results

For a number of cases, the vibration equations can be solved exactly, and the sound-model parameters can be found in analytic form. Some of these models are already very useful in giving a realistic “feel” of the collision sounds.

We have solved a number of configurations, and computed the sounds for some instances of these problems. They are:

1. **The taut string.** This is the simplest example of a vibrating system. The eigenfunctions are simple sine functions. The sound becomes brighter for impacts near the ends of the string. The frequency spectrum is harmonic, i.e. all frequencies are integer multiples of the lowest (fundamental) frequency. The amplitudes a_n are inversely proportional to n , for large n , in contrast to a plucked string, considered in [24], where they decay as $1/n^2$. This is one factor accounting for the difference between a piano and a guitar sound, for example.

2. **The rigid bar.** For the rigid bar the operator A appearing in Equation 1 is given by

$$A = -\frac{\partial^4}{\partial x^4}.$$

As A is a fourth order operator, we need to specify 4 boundary conditions. We have computed a clamped-clamped bar, i.e. the bar is rigidly attached at both ends. The boundary conditions are

$$\Psi_n(0) = \Psi_n(1) = \left(\frac{d\Psi_n}{dx}\right)_{x=0} = \left(\frac{d\Psi_n}{dx}\right)_{x=1} = 0. \quad (14)$$

The frequency spectrum is less dense than for the string, and not harmonic. This is due to the different nature of the restoring forces on a bar.

3. **The rectangular membrane.** This is the simplest two-dimensional geometry. The sound spectrum is extremely dense, giving a rich complex sound.
4. **The circular membrane.** This corresponds to the vibrations of a drum, ignoring the effects of the surrounding air on the drum membrane. The eigenfunctions are Bessel functions, and the eigenfrequencies can be computed as the zeros of Bessel functions.
5. **The circular plate.** This is one of the few cases where the two-dimensional plate equations can be separated, which allows an analytic solution. The eigenfunctions are a combination of Bessel functions and modified Bessel functions. We have considered a plate clamped rigidly at the boundary. The spectrum is much less dense than for the circular membrane. This is due, as for the bar, to the larger restoring forces in a plate, compared to a membrane.
6. **The L shaped membrane.** A membrane supported by a domain consisting of three unit squares in the shape of an L does not allow an analytic solution of the wave equation. This problem has received some attention in the literature, as the resulting boundary value problem requires some refined numerical methods. We have computed the eigenfunctions and the spectrum with an adaptation of the method of partial solutions, [7]. As an aside, we note that the first eigenfunction features prominently on the cover of the MATLAB reference guide [1].

We have implemented a Sonic Explorer, which allows us to create a graphical scene with objects of the above types. The sounds associated with a grid of points on each object are precomputed and stored as digital samples. By clicking on a point on a surface, a drumstick hits the object at the specified point and the sound is rendered. The purpose of this Explorer is to investigate the realism of the sounds by integrating them in a graphics environment, so the user can integrate visual and audio cues. Our implementation allows the optional use of a set of HRTF filters to spatialize the sounds completely in three dimensions using the public domain Kemar HRTF filters [8]. However, as we have no specialized hardware, this introduces unacceptable delays. A simple left-right localization based on interaural delays [3] does perform in real time.

7 Discussion and Conclusions

We have developed a framework to add an auditory component to real time simulation environments. We have focused on aspects of sounds that enhance the level of realism and on effects that provide the user with useful auditory clues about the simulated environment. Within our framework different materials such as wood or metal have a recognizable signature, determined through the internal friction parameter, which determines the decay rate of the different frequency components.

The shape of the object and its structure (such as a plate versus a membrane) determines a characteristic frequency spectrum. This frequency signature facilitates the recognition of an object by its sound. A metal bar, for example, rings with a sparse non-harmonic spectrum, of which the higher modes decay rapidly. This is how we recognize its sound.

The sound of an impact also depends on where an object is hit, and this also provides useful information about the environment. Though the frequency signature is the same over the object, the relative amplitudes change. Generally, an object sounds brighter (i.e. more upper partials are excited) when struck near an edge, than when struck near the center. Recall for example Sherlock Holmes, who taps on the walls to find a secret compartment. By precomputing a grid of sounds for each object, we incorporate this location information.

We have derived some general formulas to determine the spectrum from the shape and material and the amplitudes as a function of the impact site. We have considered systems that can be described by a linear wave equation on some domain, which covers many systems.

We have not taken the directionality of the sound emitted into account. To do so involves radiation theory, see for example [6], but this falls in the next stage of the pipeline depicted in Figure 1.

These ideas were implemented in a Sonic Explorer, which allows the user to explore the environment by hitting various objects with a virtual drumstick. We find that it is essential to listen to the synthesized sounds in a visual and tactile context, to judge their realism. So the Sonic Explorer is intended both as a research tool for the creation of synthesized sounds, as well as a demonstration of the enhanced realism that can be achieved by adding an auditory component to the scene that consists of more than the playback of canned sounds.

An interesting direction for future research is to integrate the Sonic Explorer with a haptic interface [5, Chapter 4]. We expect that a virtual reality environment with three sensory feedback channels (sight, hearing, and touch) will provide a significant enhancement.

As digital samples tend to take large amount of storage, the question of how many sounds need to be stored for each object comes to mind. For this we need to have some criterion to determine if two similar sounds can be distinguished by the user. The sounds associated with different impact sites are very similar and differ only in the relative amplitudes of their frequencies, and it is not clear how to construct such a measure. We have made a tentative proposal, which needs to be refined with psychoacoustic experiments before it can be used to optimize the sound-grids associated with the bodies. It is also possible to store just the model parameters (the partials, their decay rates, and the amplitudes as a field on the object surface) and use these to synthesize the sounds in real time.

Continuous sounds such as scraping, sliding and rolling can be obtained with a generalization of our method, as the relevant quantities, the eigenfrequencies, the amplitudes as a function of location, and the decay rates of the partials determine the response to such interactions in principle. Taking into account the finite duration in time, and the extension over a finite space, of impacts is another important topic for further research. We are currently investigating such a generalization.

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