

Focus + Context

Lecture 13 CPSC 533C, Fall 2004

1 Nov 2004

Focus + Context

Leung and Apperly taxonomy

A Review and Taxonomy of Distortion-Oriented Presentation Techniques, Y.K. Leung and M.D. Apperly, ACM Transactions on Computer-Human Interactions, Vol. 1, No. 2, June 1994, pp. 126-160. <http://www.acm.edu/journals/jimmy/leung/papers/leung94.pdf>

Nonlinear Magnification Fields

Nonlinear Magnification Fields, Alan Sotonyi, Proc. InfoVis '99. <http://daseer.nyu.ac.com/teaching/infomvis99.html>

2D Hyperbolic Trees

The Hyperbolic Browser: A Focus + Context Technique for Visualizing Large Hierarchies, John Lamping and Ramona Rub, Proc. SIGCHI '95. <http://daseer.nyu.ac.com/lamping95focuscontext.html>

3D Hyperbolic Graphs

H3: Laying Out Large Directed Graphs in 3D Hyperbolic Space, Tamara Munzner, Proc. InfoVis 97. <http://graphics.stanford.edu/papers/h3/>

Treeluxtaposer

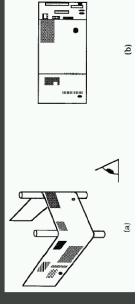
Treeluxtaposer: A Focus + Context System with Guaranteed Visibility, Munzner, Gumbelstein, Tarride, Zhang, and Zhou, SIGGRAPH 2003. <http://www.cs.cmu.edu/~tamara/papers/tj03/>

hyperbolic geometry background, if time

2

Intuition

move part of surface closer to eye

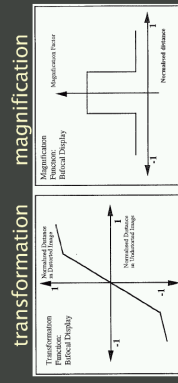


stretchable rubber sheet borders tacked down

merge overview and detail into combined view

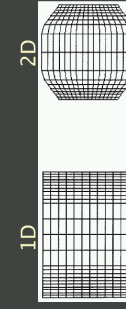
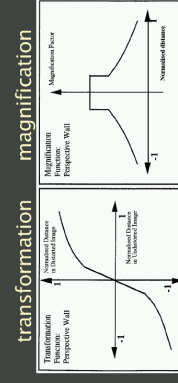
3

Bifocal



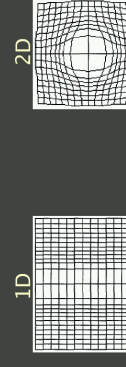
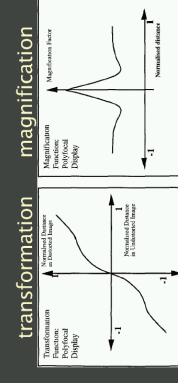
4

Perspective Wall



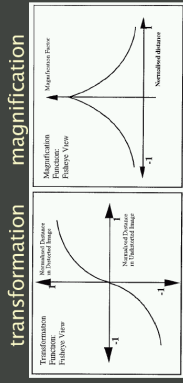
5

Polyfocal: Continuous Mag transformation magnification



6

Fisheye Views: Continuous Mag

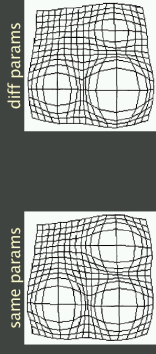


1D 2D rect polar norm polar

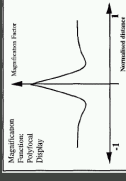


7

Multiple Foci



polyfocal magnification function dips allow this



8

Nonlinear Magnification Functions

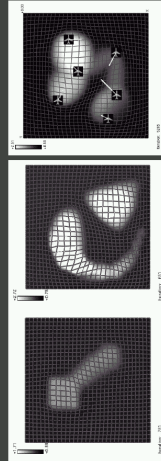
- transformation
 - distortion
- magnification
 - derivative of transformation
- directionality
 - easy: compute transformation given magnification derivative
 - hard: compute magnification given transformation integration
- new mathematical framework
 - approximate integration, iterative refinement
 - minimize "error mesh"

9

Expressiveness

magnification is more intuitive control

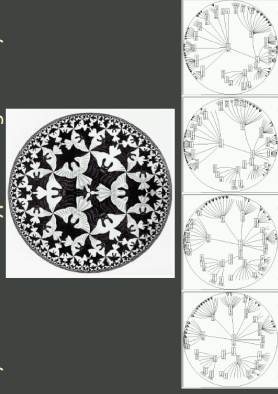
- allow expressiveness, data-driven expansion



10

2D Hyperbolic Trees

fisheye effect from hyperbolic geometry



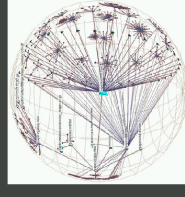
[video]

11

3D Hyperbolic Graphs: H3

task

- browsing large quasi-hierarchical graphs



[Munzner 1997, 1998a, 1998b]

12

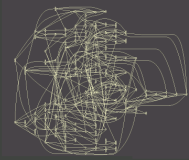
Previous work: graph drawing

scalability bottleneck
layout
avoiding disorientation

13

Previous work: graph drawing

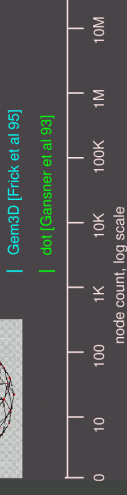
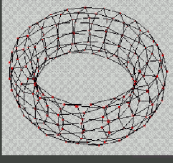
scalability bottleneck
layout
avoiding disorientation



14

Previous work: graph drawing

scalability bottleneck
layout
avoiding disorientation



15

Graph layout criteria

minimize
· crossings, area, bends/curves



maximize

· angular resolution, symmetry



16

Graph layout criteria

minimize
· crossings, area, bends/curves



maximize

· angular resolution, symmetry



most criteria NP-hard
· edge crossings [Garey and Johnson 83]

17

Graph layout criteria

minimize
· crossings, area, bends/curves



maximize

· angular resolution, symmetry



most criteria NP-hard
· edge crossings [Garey and Johnson 83]

18

Graph layout criteria

- minimize**
 - crossings, area, bends/curves
- maximize**
 - angular resolution, symmetry
- most criteria NP-hard**
 - edge crossings [Garey and Johnson 83]
- incompatible**
 - [Brandenburg 88]

bad

bad

edge crossing

good

good

symmetry

19

Layout

- problem**
 - general problem is NP-hard



20

Layout

- problem**
 - general problem is NP-hard
- solution**
 - tractable spanning tree backbone
 - match mental model
 - "quasi-hierarchical"
 - use domain knowledge to construct
 - select parent from incoming links



21

Layout

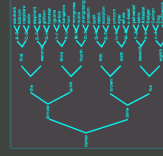
- problem**
 - general problem is NP-hard
- solution**
 - tractable spanning tree backbone
 - match mental model
 - "quasi-hierarchical"
 - use domain knowledge to construct
 - select parent from incoming links
 - non-tree links on demand



22

Avoiding disorientation

- problem**
 - maintain user orientation when showing detail
 - hard for big datasets
- exponential in depth: node count, space needed**



global overview

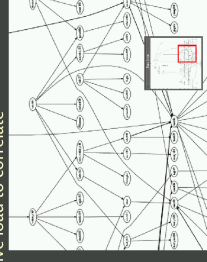


local detail

23

Overview and detail

- two windows: add linked overview**
 - cognitive load to correlate



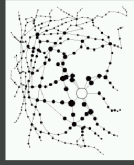
solution

- merge overview, detail
- "focus+context"

24

Previous work: focus+context

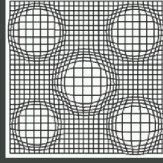
fish-eye views [Furnas 86], [Sarkar et al 94]



25

Previous work: focus+context

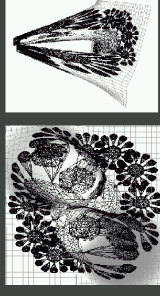
fish-eye views [Furnas 86], [Sarkar et al 94]
nonlinear magnification [Keahey 96]



26

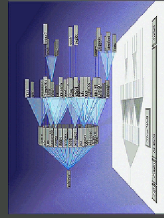
Previous work: focus+context

fish-eye views [Furnas 86], [Sarkar et al 94]
nonlinear magnification [Keahey 96]
pliable surfaces [Carpendale et al 95]



27

Previous work: focus+context trees



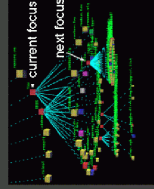
| H3 [Munzner 97,98]

| Cone Trees [Robertson et al 91]



28

Previous work: focus+context trees



| H3 [Munzner 97,98]

| Fractal trees [Koike & Yoshihara 93]

| Cone Trees [Robertson et al 91]



29

Previous work: focus+context trees

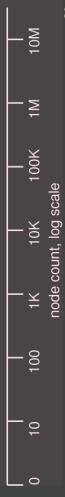


| H3 [Munzner 97,98]

| 2D Hyp Trees [Lamping et al 94,95]

| Fractal trees [Koike & Yoshihara 93]

| Cone Trees [Robertson et al 91]

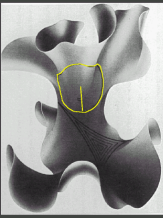


30

Hyperbolic space background

geometry with exponential "amount of room"
· good match for exponential node count of trees

2D hyperbolic plane



hemisphere area

hyperbolic: exponential
 $2\pi \sinh^2(r)$

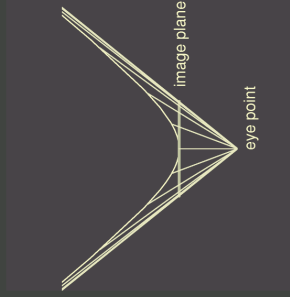
euclidean: polynomial
 $2\pi r^2$

[Thurston and Weeks 84]

31

1D hyperbolic space

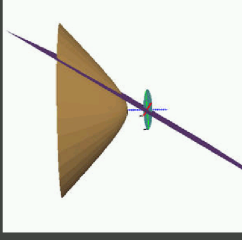
hyperbola projects to line



32

2D hyperbolic space

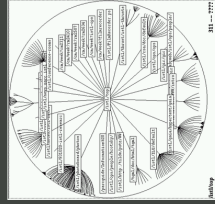
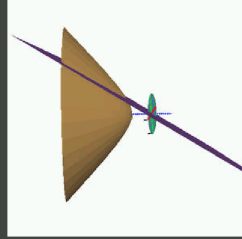
hyperboloid projects to disk



33

2D hyperbolic space

hyperboloid projects to disk



Huber

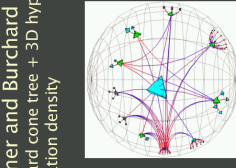
811-12222

[Lamping et. al 95]

34

3D hyperbolic space

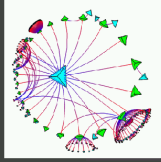
3-hyperboloid projects to solid ball



webviz [Munzner and Burchard 95]
· straightforward cone tree + 3D hyperbolic space
· poor information density

36

Contribution: focus+context graphs



- | H3 [Munzner 97,98]
- | webviz [Munzner & Burchard 95]
- | 2D Hyp Trees [Lamping et al 94,95]
- | Fractal trees [Kojke & Yoshitara 93]
- | Cone Trees [Robertson et al 91]



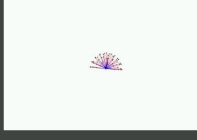
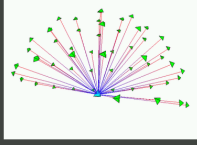
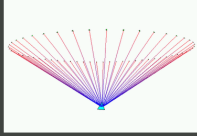
37

3D hyperbolic space

3-hyperboloid projects to solid ball

H3 layout

- circumference → hemisphere



38

3D hyperbolic space

3-hyperboloid projects to solid ball

H3 layout

- bottom-up: allocate space for nodes
- top-down: place child on parent hemisphere

Formula	Euclidean	Hyperbolic
right-angle triangle	$\tan \theta = \frac{op}{adj}$	$\tan \theta = \frac{\sinh(op)}{\sinh(adj)}$
right-angle triangle	$\sin \theta = \frac{opp}{hyp}$	$\sin \theta = \frac{\sinh(op)}{\sinh(hyp)}$
circle area	πr^2	$2\pi(\cosh(r) - 1)$
hemisphere area	$2\pi r^2$	$2\pi \sinh^2(r)$
spherical cap area	$2\pi r^2(1 - \cos \phi)$	$2\pi \sinh^2(r(1 - \cos \phi))$

39

Progressive rendering

want fast update during user interaction

- fill in details when user is idle

problem

- dataset too big to draw in single frame

solution

- guaranteed frame rate algorithm

progressive refinement

- gradually improve image vs. standard Z-buffer
- common in graphics [Bergman et al 86]
- far less attention in infovis

40

H3 video (excerpts)

42

H3viewer algorithm

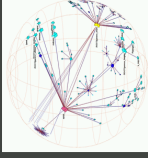
drawing queue for nodes

graph-theoretic

- add parent, child nodes to queue

view-dependent

- sort queue by screen area



41

H3 results

- scalability
- performance
- information density

43

H3 results: scalability

performance

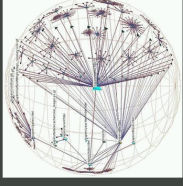
- layout
110K edges, 12 seconds (1997: SGI IR2)
300K edges, 16 seconds (2002: Intel P3)
- drawing
constant time: guaranteed frame rate
- limited by main memory size

44

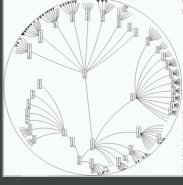
H3 results: scalability

information density: 10x better

H3



2D PARC Tree



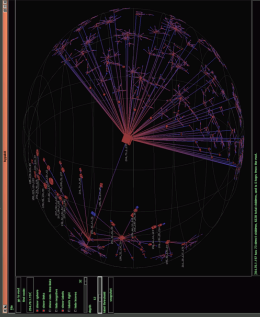
	center	fringe
3D	dozens	thousands
2D	dozens	hundreds

45

H3 discussion: scalability

focus+context layout

- success: large local neighborhood visible, 5-9 hops
- cognitive limit: if graph diameter >>> visible area



46

TreeJuxtaposer

extend cognitive limit

- move from local F+C to global F+C

47

Noneuclidean geometry

Euclid's 5th Postulate

- exactly 1 parallel line

spherical

- geodesic = great circle
- no parallels

hyperbolic

- infinite parallels

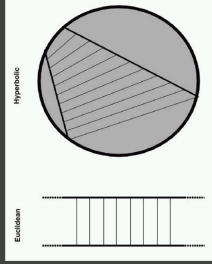


<https://www.math.uic.edu/~jms/jmsw/graphics/here>

48

Parallel vs. equidistant

euclidean: inseparable
hyperbolic: different

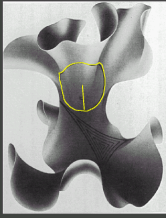


49

Exponential "amount of room"

good match for exponential node count of trees

2D hyperbolic plane
embedded in 3D space



[Thurston and Weeks 84]

hemisphere area

hyperbolic: **exponential**
 $2\pi \sinh^2(r)$

euclidean: **polynomial**
 $2\pi r^2$

50

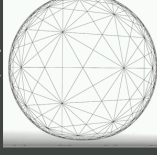
Models, 2D

not just round!

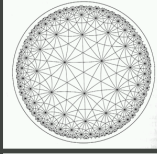


Minkowski

Klein/projective



Poincare/conformal



Upper Half Space

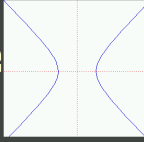


51

[Three Dimensional Geometry and Topology, William Thurston, Princeton University Press]

Minkowski

1D



2D



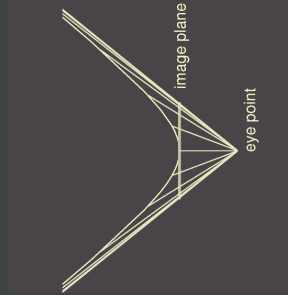
[www.gis.gov.au/arcuser/arcuserhelp/arcuserhelp.htm#hyperbolic_geometry]

the hyperboloid itself
embedded one dimension higher

52

1D Klein

hyperbola projects to line

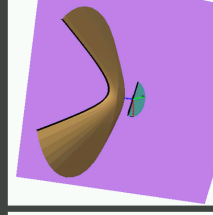
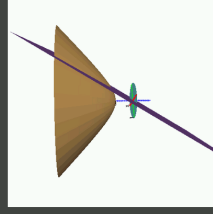


53

2D Klein

hyperboloid projects to disk

[demo: [Corti's view](http://www.geom.uiowa.edu/~crobles/hyperbolic/hypr/lham/mbb/M2K.mpg)]
[video: www.geom.uiowa.edu/~crobles/hyperbolic/hypr/lham/mbb/M2K.mpg]



[graphics.stanford.edu/papers/munzner_thesis/html/node8.html#hyp2Dfig]

54

Klein vs Poincare

stereographic projection

- transparent sphere
- plane at south pole
- light at north pole

[demo: torus.math.uiuc.edu/jms/java/stereop/]

transformation from Klein to Poincare

- vertically project disc to hemisphere
- stereographically project hemisphere to Poincare disc

[video: www.geom.umn.edu/~crobbles/hyperbolic/hypr/lbm/mkb/k2p.mpg]

graphics

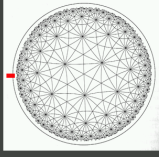
- Klein: 4x4 real matrix
- Poincare: 2x2 complex matrix

55

Upper Half Space

"cut and unroll" Poincare

- one point on circle goes to infinity

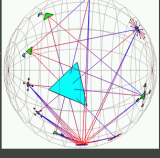


[demo: www.geom.umn.edu/~crobbles/hyperbolic/hypr/mod/uhp/uhpjava.html]

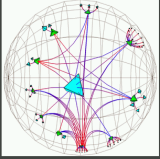
56

Models, 3D

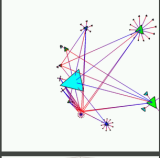
Klein/projective



Poincare/conformal



"insider"



[<http://graphics.stanford.edu/papas/webviz/>]

· Upper Half Space

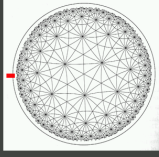
· Minkowski

57

Upper Half Space

"cut and unroll" Poincare

- one point on circle goes to infinity



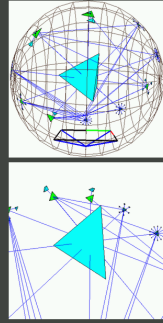
[demo: www.geom.umn.edu/~crobbles/hyperbolic/hypr/mod/uhp/uhpjava.html]

56

3D Insider

insider: camera also moves by hyperbolic rules

- cool, but limited visibility



[demo]

58

3D Klein

3-hyperboloid projects to solid ball



59

3D Minkowski

3-hyperboloid embedded in 4D space

light cone: special relativity

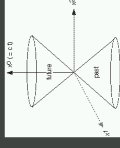
- diagrams in 2D for clarity

timelike: inside cone, speed < c

lightlike: on cone, speed = c

spacelike: outside cone, speed > c

- can't affect



[applearee.ma.ca/courses/physics/4701/ETex/LightCone.html]