



Tamara Munzner

Viewing/Projections IV

Week 4, Fri Feb 2

<http://www.ugrad.cs.ubc.ca/~cs314/vjan2007>

Reading for Today

- FCG Chapter 7 Viewing
- FCG Section 6.3.1 Windowing Transforms
- RB rest of Chap Viewing
- RB rest of App Homogeneous Coords

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Reading for Next Time

- RB Chap Color
- FCG Sections 3.2-3.3
- FCG Chap 20 Color
- FCG Chap 21 Visual Perception

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News

- my office hours reminder (in lab): today 11-12
- homework 1 due 3pm in box marked 314
 - same hallway as lab
- project 1 due 6pm, electronic handin
 - no hardcopy required
 - demo signup sheet going around again
 - Mon 1-12; Tue 10-12:30, 4-6; Wed 10-12, 2:30-4
 - arrive in lab 10 min before for your demo slot
 - be logged in and ready to go at your time
 - note to those developing in Windows/Mac
 - your program **must** compile and run on lab machines
 - test before the last minute, no changes after handin

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Homework 1 News

- don't forget problem 11 (on back of page)
- Problem 3 is now extra credit
 - Write down the 4x4 matrix for shearing an object by 2 in y and 3 in z.

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Correction (Transposed Before): 3D Shear

- shear in x
 - shear due to x along y and z axes
- shear in y
- shear in z
- general shear

$$\begin{matrix}
 \begin{bmatrix} 1 & sy & sz & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} & \text{xshear}(hsx, hsz) = & \begin{bmatrix} 1 & 0 & 0 & 0 \\ hsy & 1 & 0 & 0 \\ hsz & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \\
 \begin{bmatrix} 1 & 0 & 0 & 0 \\ sx & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} & \text{yshear}(hsx, hsz) = & \begin{bmatrix} 1 & hsy & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & hsz & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \\
 \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ sx & sy & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} & \text{zshear}(hsx, hsz) = & \begin{bmatrix} 1 & 0 & hsz & 0 \\ 0 & 1 & hsy & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \\
 \begin{bmatrix} 1 & sy & sz & 0 \\ sx & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} & \text{shear}(hsx, hsz, hsy, hsz, hsz, hsz) = & \begin{bmatrix} 1 & hsy & hsz & 0 \\ hsy & 1 & hsz & 0 \\ hsz & hsz & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}
 \end{matrix}$$

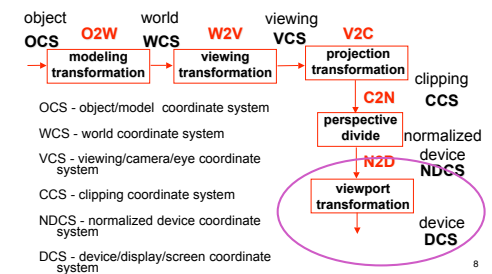
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News

- midterm Friday Feb 9
 - closed book
 - no calculators
 - allowed to have one page of notes
 - handwritten, one side of 8.5x11" sheet
 - this room (DMP 301), 11-11:50
- material covered
 - transformations, viewing/projection

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Projective Rendering Pipeline

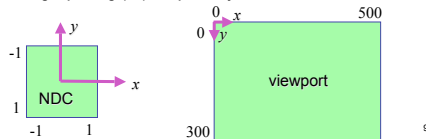


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NDC to Device Transformation

- map from NDC to pixel coordinates on display
 - NDC range is $x = -1...1$, $y = -1...1$, $z = -1...1$
 - typical display range: $x = 0...500$, $y = 0...300$
 - maximum is size of actual screen
 - z range max and default is (0, 1), use later for visibility

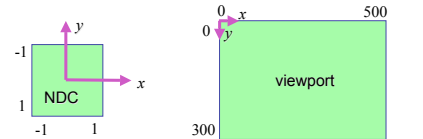
```
glViewport(0,0,w,h);
glDepthRange(0,1); // depth = 1 by default
```



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Origin Location

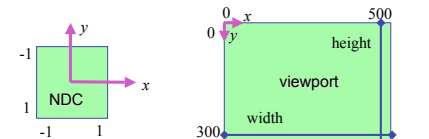
- yet more (possibly confusing) conventions
 - OpenGL origin: lower left
 - most window systems origin: upper left
- then must reflect in y
- when interpreting mouse position, have to flip your y coordinates



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N2D Transformation

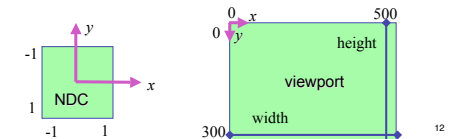
- general formulation
 - reflect in y for upper vs. lower left origin
 - scale by width, height, depth
 - translate by width/2, height/2, depth/2
 - FCG includes additional translation for pixel centers at (.5, .5) instead of (0,0)



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N2D Transformation

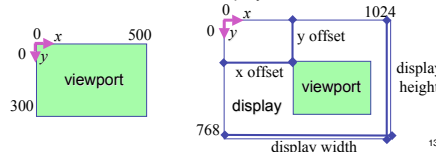
$$\begin{bmatrix} x_p \\ y_p \\ z_p \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & \frac{width}{2} \\ 0 & 1 & 0 & \frac{height}{2} \\ 0 & 0 & 1 & \frac{depth}{2} \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \frac{width}{2} \\ \frac{height}{2} \\ \frac{depth}{2} \\ 1 \end{bmatrix} + \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x_n \\ y_n \\ z_n \\ 1 \end{bmatrix} = \begin{bmatrix} \frac{width(x_n+1)-1}{2} \\ \frac{height(-y_n+1)-1}{2} \\ \frac{depth(z_n+1)}{2} \\ 1 \end{bmatrix}$$



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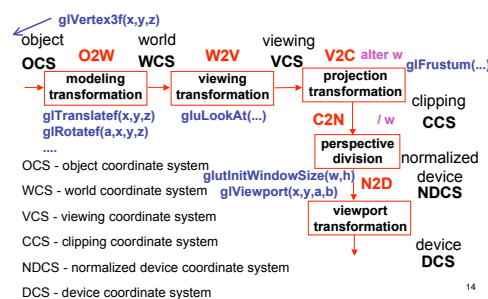
Device vs. Screen Coordinates

- viewport/window location wrt actual display not available within OpenGL
 - usually don't care
 - use relative information when handling mouse events, not absolute coordinates
 - could get actual display height/width, window offsets from OS
- loose use of terms: device, display, window, screen...



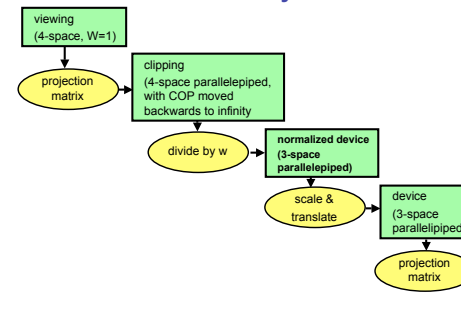
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Projective Rendering Pipeline



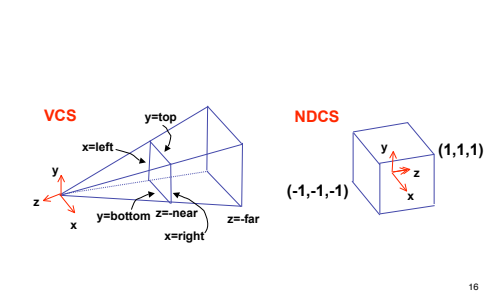
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Coordinate Systems



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Perspective To NDCS Derivation



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Perspective Derivation

simple example earlier:
$$\begin{bmatrix} x' \\ y' \\ z' \\ w' \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 1/d & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

complete: shear, scale, projection-normalization

$$\begin{bmatrix} x' \\ y' \\ z' \\ w' \end{bmatrix} = \begin{bmatrix} E & 0 & A & 0 \\ 0 & F & B & 0 \\ 0 & 0 & C & D \\ 0 & 0 & -1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

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Perspective Derivation

earlier:
$$\begin{bmatrix} x' \\ y' \\ z' \\ w' \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 1/d & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

complete: shear, scale, projection-normalization

$$\begin{bmatrix} x' \\ y' \\ z' \\ w' \end{bmatrix} = \begin{bmatrix} E & 0 & A & 0 \\ 0 & F & B & 0 \\ 0 & 0 & C & D \\ 0 & 0 & -1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

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Perspective Derivation

earlier:
$$\begin{bmatrix} x' \\ y' \\ z' \\ w' \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 1/d & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

complete: shear, scale, projection-normalization

$$\begin{bmatrix} x' \\ y' \\ z' \\ w' \end{bmatrix} = \begin{bmatrix} E & 0 & A & 0 \\ 0 & F & B & 0 \\ 0 & 0 & C & D \\ 0 & 0 & -1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

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Perspective Derivation

$$\begin{bmatrix} x' \\ y' \\ z' \\ w' \end{bmatrix} = \begin{bmatrix} E & 0 & A & 0 \\ 0 & F & B & 0 \\ 0 & 0 & C & D \\ 0 & 0 & -1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

$x' = Ex + Az$
 $y' = Fy + Bz$
 $z' = Cz + D$
 $w' = -z$

$x = \text{left} \rightarrow x'/w' = 1$
 $x = \text{right} \rightarrow x'/w' = -1$
 $y = \text{top} \rightarrow y'/w' = 1$
 $y = \text{bottom} \rightarrow y'/w' = -1$
 $z = \text{-near} \rightarrow z'/w' = 1$
 $z = \text{-far} \rightarrow z'/w' = -1$

$$y' = Fy + Bz, \quad \frac{y'}{w'} = \frac{Fy + Bz}{-z}, \quad 1 = \frac{Fy + Bz}{-z}, \quad 1 = \frac{Fy + Bz}{-z}$$

$$1 = F \frac{y}{-z} + B \frac{z}{-z}, \quad 1 = F \frac{y}{-z} - B, \quad 1 = F \frac{\text{top}}{-(-\text{near})} - B,$$

$$1 = F \frac{\text{top}}{\text{near}} - B$$

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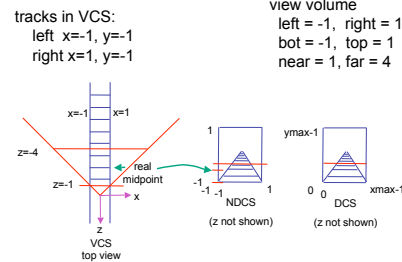
Perspective Derivation

- similarly for other 5 planes
- 6 planes, 6 unknowns

$$\begin{bmatrix} 2n & 0 & r+l & 0 \\ r-l & 0 & r-l & 0 \\ 0 & 2n & t+b & 0 \\ 0 & 0 & t-b & 0 \\ 0 & 0 & -(f+n) & -2fn \\ 0 & 0 & f-n & f-n \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

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Perspective Example



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Perspective Example

view volume
left = -1, right = 1
bot = -1, top = 1
near = 1, far = 4

$$\begin{bmatrix} 2n & 0 & r+l & 0 \\ r-l & 0 & r-l & 0 \\ 0 & 2n & t+b & 0 \\ 0 & 0 & t-b & 0 \\ 0 & 0 & -(f+n) & -2fn \\ 0 & 0 & f-n & f-n \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

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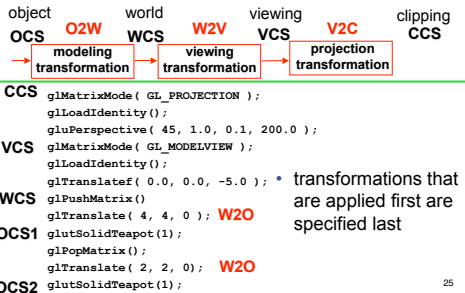
Perspective Example

$$\begin{bmatrix} 1 \\ -1 \\ -5z_{VCS}/3 - 8/3 \\ -z_{VCS} \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ -5/3 & -8/3 \\ -1 \end{bmatrix} \begin{bmatrix} 1 \\ -1 \\ z_{VCS} \\ 1 \end{bmatrix}$$

$x_{NDCS} = -1/z_{VCS}$
 $y_{NDCS} = 1/z_{VCS}$
 $z_{NDCS} = \frac{5}{3} + \frac{8}{3z_{VCS}}$

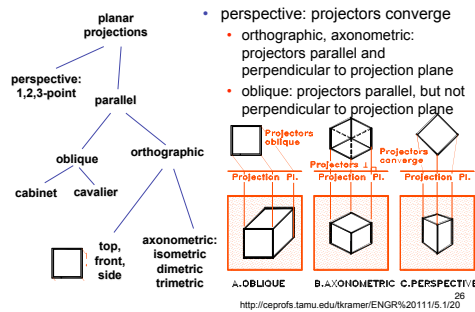
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OpenGL Example



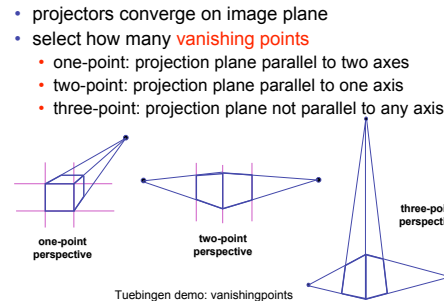
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Projection Taxonomy



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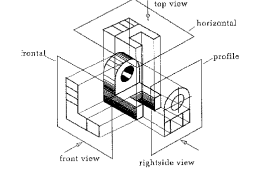
Perspective Projections



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Orthographic Projections

- projectors parallel, perpendicular to image plane
- image plane normal parallel to one of principal axes
- select view: top, front, side
- every view has true dimensions, good for measuring

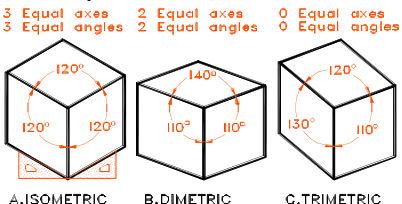


<http://www.cs.fsu.edu/~wds/classes/cse5255/thesis/images/proj/orthoProj.gif>

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Axonometric Projections

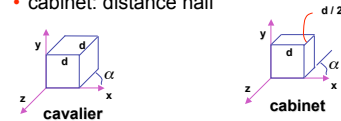
- projectors parallel, perpendicular to image plane
- image plane normal not parallel to axes
- select axis lengths
- can see many sides at once



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Oblique Projections

- projectors parallel, oblique to image plane
- select angle between front and z axis
 - lengths remain constant
- both have true front view
 - cavalier: distance true
 - cabinet: distance half



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