Question 4 1

1.1

$$P(B_2 = G) = \sum_{B_1 \in \{G, M, A\}} P(B_2 = G, B_1)$$

$$= \sum_{B_1 \in \{G, M, A\}} P(B_2 = G|B_1)P(B_1)$$
(2)

$$= \sum_{B_1 \in \{G, M, A\}} P(B_2 = G|B_1)P(B_1) \tag{2}$$

$$= 0.8 \times 0.5 + 0.1 \times 0.4 + 0.2 \times 0.1 \tag{3}$$

$$=0.46\tag{4}$$

1.2

$$P(B1 = G|B2 = G) = \frac{P(B_2 = G|B_1 = G)P(B_1 = G)}{P(B_2 = G)}$$

$$= \frac{0.8 \times 0.5}{0.46}$$
(5)

$$=\frac{0.8 \times 0.5}{0.46} \tag{6}$$

$$=0.87\tag{7}$$